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# eDNAPlus: A unifying modelling framework for DNA-based biodiversity monitoring

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13 Abstract

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DNA-based biodiversity surveys, which involve collecting physical samples from survey sites and assaying them in the laboratory to detect species via their diagnostic DNA sequences, are increasingly being adopted for biodiversity monitoring and decision-making. The most commonly employed method, metabarcoding, combines PCR with high-throughput DNA sequencing to amplify and read 'DNA barcode' sequences, generating count data indicating the number of times each DNA barcode was read. However, DNA-based data are noisy and error-prone, with several sources of variation, and cannot alone estimate the species-specific amount of DNA present at a surveyed site (DNA biomass). In this paper, we present a unifying modelling framework for DNA-based survey data that allows estimation of changes in DNA biomass within species, across sites and their links to environmental covariates, whilst for the first time simultaneously accounting for key sources of variation, error and noise in the data-generating process, and for between-species and between-sites correlation. Bayesian inference is performed using MCMC with Laplace approximations. We describe a re-parameterisation scheme for crossed-effects models designed to improve mixing, and an adaptive approach for updating latent variables, which reduces computation time. Theoretical and simulation results are used to guide study design, including the level of replication at different survey stages and the use of quality control methods. Finally, we demonstrate our new framework on a dataset of Malaise-trap samples, quantifying the effects of elevation and distance-to-road on each species, and produce maps identifying areas of high biodiversity and species DNA biomass.

 $Keywords:\ crossed$ -effects model, environmental DNA, joint species distribution modelling, observation error, occupancy modelling

## $_{33}$ 1 Introduction

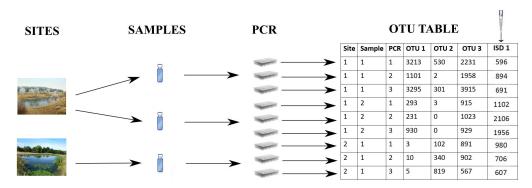
Ecology is undergoing a technology revolution that is making it possible to rapidly 39 generate species inventories via automated and high-throughput DNA sequencers and via 40 electronic sensors, such as drones, satellites, camera traps, and acoustic recorders. These 41 techniques can, if coupled with appropriate algorithms and databases, simultaneously identify large numbers of target species, including those that are cryptic, difficult-to-access, tiny, 43 and low-abundance (Bush et al., 2017; Besson et al., 2022; Piper et al., 2019; Ley, 2022). So far, the most efficient method for generating species-resolution inventories is DNA-based surveys, which rely on reading DNA barcodes: short, standardized sections of the genome 46 that can be compared to a reference library to enable taxonomic identifications without the need to examine organism morphologies (Ratnasingham and Hebert, 2007). DNA barcoding refers to the identification of single species (Hebert et al., 2003), and 49 DNA metabarcoding refers to the detection of large numbers of species from environmental DNA (eDNA), which is the collective name for DNA isolated from environmental samples (Taberlet et al., 2018). These environmental samples include water (Thomsen and Willerslev, 2015), soil (Frøslev et al., 2019), air (Clare et al., 2022), and bulk tissue (i.e. mass-trapped organisms) (Ji et al., 2013). For instance, Thomsen and Sigsgaard (2019) demonstrated that traces of eDNA on flower petals could be analysed to describe the diversity of arthropods that visit wildflowers, including pollinators, parasitoids, predators, and herbivores. Ji et al. (2022) used the trace amounts of residual vertebrate blood left in 30,468 blood-sucking leeches to map vertebrate wildlife across a  $677 \text{ km}^2$  nature reserve in 58 China. Finally, Abrego et al. (2021) sequenced 542 mixed-species, bulk-tissue samples of arctic arthropods captured over 14 years and showed that species richness in the study site had declined by 50% during a time period in which local mean temperature had increased by 2C. The potential of DNA-based surveys for monitoring and managing biodiversity comes 63

with a number of statistical challenges. Firstly, species-specific absolute abundances can-

not be estimated using DNA data alone. Secondly, DNA-based surveys yield data that
are overdispersed (including zero-inflation) relative to a Poisson distribution due to several
types of error and noise (see Section 1.1), some of which are species-specific. The framework
presented in this paper addresses these challenges by developing a novel model and corresponding efficient inferential tools. Using our framework, we model within-species change
in DNA biomass across sites (described in Section 1.1), which under certain conditions can
be considered as a proxy for change in abundance, hence addressing the first challenge. To
address the second challenge, we propose a hierarchical crossed-effects model that expresses
key sources of variation, error and noise in the data collection and analysis pipeline, whilst
accounting for correlation across species and across sites, and for covariate effects on DNA
biomass. We also model frequently employed controls at the PCR stage and evaluate their
effect on inference.

#### 77 1.1 DNA-based surveys and associated challenges

Each individual of a species sheds tissue and waste products, and thus its DNA, into 78 the environment. We will refer to this as DNA biomass. As we explain in Section 2, the estimates of species DNA biomass obtained from DNA-based surveys alone are only 80 meaningful in comparison between sites, and for that reason, in this paper we focus on modelling changes in DNA biomass within species, across sites, referred to as changes in 82 DNA biomass throughout. We achieve this by assuming that the processes are standardised across sites, samples, and PCR replicates and that any differences in the efficiencies of the processes are explained by covariates that can be included in the model. We highlight that, theoretically, the overall amount of DNA biomass for each species is proportional to the species' abundance at that site, but the rate at which each species sheds DNA into 87 the environment is unknown and not estimable using eDNA data alone. Additionally, the relationship between DNA biomass and abundance can vary between species and sites due to environmental conditions, such as DNA degradation rates, and we return to this point in Section 6. Under the assumption that this relationship does not vary with sites then we



**Figure 1:** Representation of the DNA biomass collection stage (Stage 1, Sites to Samples) and the DNA biomass analysis stage (Stage 2, Samples to PCR to OTU table). Each of the selected sites to be surveyed hosts a community of species, and hence a certain amount of DNA biomass for each species. One or more physical samples are collected from each surveyed site, and a 'spike-in' or 'internal standard' ISD, can be added to each sample (last column). Each sample is PCR'd one or more times and then sequenced. This process gives rise to the OTU table.

can interpret changes in species DNA biomass as corresponding changes in abundance.

DNA-based surveys comprise two stages (Figure 1): the sample collection stage (Stage 1), taking place in the field, and the sample analysis stage (Stage 2), taking place in the lab.

In Stage 1, physical samples are collected from each surveyed site. However, the amount 96 of DNA biomass of each species collected in each sample is the result of a noisy and errorprone process (see Table 1). Specifically, the sampling method inevitably favours some species over others, and as a result, DNA biomass collection rates, conditional on the 99 available DNA biomasses, are species-specific (Stage 1 species effect). The amount of DNA 100 biomass collected for each species also varies between samples collected at the same site 101 (Stage 1 noise). Finally, there are non-negligible probabilities that (a) no DNA biomass 102 is collected for a species even if there was DNA biomass of that species at the site (false 103 negative error) and (b) the DNA biomass in the sample is not the result of species presence, 104 but instead reflects contamination or deposition from elsewhere (false positive error) (Stage 105 1 false negative and false positive errors are jointly referred to as Stage 1 error). 106

In Stage 2, the physical samples are assayed in the lab. The most frequently used method for reading DNA barcodes from eDNA samples is 'amplicon sequencing' (see Lindahl et al.,

2013, for an excellent review). In short, from each sample, all DNA is extracted and purified. After extraction, a small aliquot of DNA from each sample is subjected to Polymerase Chain 110 Reaction (PCR), which selectively amplifies (makes many copies of) just the DNA-barcode 111 sequences. It is common practice in Stage 2 for a sample to be PCR-assayed multiple times, known as technical replicates to distinguish them from sample replicates in Stage 1. The 113 PCR outputs ('amplicons') from all the samples and their technical replicates are pooled 114 and read on a high-throughput DNA sequencer. This procedure ultimately leads to a list 115 of many millions of individual DNA sequences (known as reads), which are processed in a 116 bioinformatic pipeline that removes low-quality reads, groups the remainder into clusters of 117 similar reads that are species hypotheses known as OTUs (Operational Taxonomic Units), 118 and apportions each OTU's reads back to its original samples and PCRs. The resulting 119 OTU table dataset indicates the number of reads for each OTU in each PCR in each sample 120 in each site (Figure 1), with columns representing the species and rows representing the 121 PCR runs. For simplicity, we hereafter use the terms OTUs and species interchangeably. 122 A real-world complication in DNA-based laboratory pipelines is that samples are typ-123 ically 'normalised' one or more times. For instance, after the samples are enzymatically 124 digested to break down cells and release their DNA into their 'lysis-buffer' solutions, each 125 sample constitutes a larger volume of liquid than can be used for DNA extraction. The 126 samples are thus normalised by taking a fixed volume from each sample for processing. 127 Another normalisation step happens after PCR, because different PCR replicates can gen-128 erate different amounts of product. In this case, the PCR products are normalised by 129 taking a certain amount of liquid from each PCR output, either inversely proportional to 130 their concentration, or fixed across PCRs. In the first (lysis buffer) normalisation step, 131 the numerator (amount of lysis buffer taken for extraction) is fixed, while the denominator 132 (total volume of lysis buffer) varies. In the second (PCR product) normalisation step, the 133 numerator (amount of PCR liquid taken for sequencing) varies, while the denominator (to-134 tal volume of PCR liquid) is fixed. It is standard procedure to record these normalisation

fractions, and in Section 2, we show how this information is incorporated into the model.

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Generally, we should expect a positive relationship between the DNA biomass of a

species in a sample and the count of reads obtained for that species in that sample (Luo 138 et al., 2022), but this relationship is imperfect, due to noise and error (see Table 1). First, 139 even given best practice, there are small but non-negligible probabilities (a) that a species' 140 DNA in a sample fails to be amplified or sequenced, leading to false-negative error and (b) 141 that a species' DNA cross-contaminates other samples and is amplified, leading to false-142 positive error (Stage 2 false negative and false positive errors are jointly referred to as Stage 143 2 error). We say that a PCR yields non-negligible reads for a species when the PCR product 144 of that species is successfully read by the DNA sequencer (i.e. the PCR is successful), and 145 otherwise, a PCR yields zero or non-zero but negligible reads, in which case we say that the PCR is not successful for that species. We note that a PCR can be successful, that 147 is, yield non-negligible reads, not only when the biomass is present in the sample but also 148 when it is not, in the latter case because of contamination. Additionally, PCR amplification 149 also inevitably favours some species over others, due to PCR primer mismatch, resulting 150 in species-specific amplification rates (Stage 2 species effect, equal within columns of the 151 OTU table), and PCR and sequencing stochasticity results in different total numbers of 152 reads across all species, even for the same sample (Stage 2 pipeline effect, equal within rows 153 of the OTU table). Finally, due to the inherent stochasticity of the PCR and sequencing 154 process, there is added noise in the resulting reads in each cell of the OTU table (Stage 2 155 noise). 156 In Stage 2, in addition to recording the normalisation fractions, different approaches 157 are employed to understand and monitor some of the noise and error. One such approach 158 is the so-called internal standard or *spike-in*, during which a known amount of DNA of a 159

are employed to understand and monitor some of the noise and error. One such approach is the so-called internal standard or *spike-in*, during which a known amount of DNA of a synthetic sequence or of a species that is known to be absent from all surveyed sites, is added to each sample. In addition, negative controls, which are samples that are known to not include DNA of any species, can be introduced in Stage 1 and Stage 2 (Ficetola et al.,

<sub>63</sub> 2015).

**Table 1:** Description of noise, error, and species/pipeline effects in the two stages of DNA-based surveys.

Stage 1 - DNA biomass collection	
Species effect	Every sample contains a certain amount of DNA biomass of each species,
	with the amount proportional to the DNA biomass available at the site.
	However, the proportionality constant is unknown and species-specific,
	since the DNA of different species can be collected at different rates.
Noise	The amount of DNA biomass collected for each species varies stochasti-
	cally between samples collected at the same site and time.
Error	It is possible for the DNA of a target species that is present at a site not
	to be sampled (false negative error), or traces of DNA from one sample
	to contaminate another sample (false positive error).
Stage 2 - DNA biomass analysis	
Species effect	As a result of differences in gene copy number, DNA extraction efficiency,
	and PCR amplification efficiency, the correspondence between the source
	sample DNA biomass and the number of amplicon reads is species-specific
	(each column of the OTU table).
Pipeline effect	PCR stochasticity and the passing of small aliquots of liquid along the
	laboratory pipeline affects the total number of reads per technical repli-
	cate for all species (each row of the OTU table).
Noise	In addition to the species and pipeline effect, there is added noise in the
	number of reads per OTU and PCR (each cell of the OTU table).
Error	It is possible for the DNA of a target species that is present in the sample
	not to be amplified in the lab (false negative error), or traces of DNA
	of one sample to contaminate and be detected in other samples (false
	positive error), due to the high species-detection power of amplicon se-
	quencing.

## 1.2 Existing approaches

A common approach for modelling metabarcoding data is to convert them to detection/nondetection data by thresholding the number of reads in the OTU table, with user-specified
criteria. This allows the use of a generalized linear model (GLM) framework (Saine et al.,
2020), which has also been extended to account for species correlation, for example using
joint species distribution models (JSDMs) (Ovaskainen and Abrego, 2020). However, this
approach does not account for the two stages or the noise and error inherent in DNA-based
surveys (Table 1).

To that end, several different but related approaches have been proposed. A common approach applies occupancy models that account for false negative observation error to

the binary detection/no detection data (Ficetola et al., 2015). More recently, multi-scale extensions of these occupancy models have been proposed to account for false negative 175 error in both stages (Mordecai et al., 2011; Schmidt et al., 2013) and for false positive 176 error (Guillera-Arroita et al., 2017; Griffin et al., 2020) for a single species. However, the 177 occupancy model framework disregards the information in the reads and relies on arbitrary 178 thresholds about what constitutes a detection. Alternatively, the reads have also been 179 modelled within a GLM framework (Takahara et al., 2012; Carraro et al., 2018) but without 180 considering the errors in each stage. A joint model of species occupancy and corresponding 181 reads was developed by Fukaya et al. (2022) but without considering the direct link between 182 species DNA biomass at the site and species reads, or the correlation between species. 183

Finally, we note that an area of research similar to DNA-based biodiversity surveys 184 is microbiome biology, which is the genetic material of all microbial life in an abiotic 185 substrate (e.g. soil) or in a living host (e.g. the human microbiome). When modelling 186 microbiome data, analysis has usually focused on understanding changes in the relative 187 composition of each taxon across different samples. As a result, modelling approaches in 188 this field have revolved around the Dirichlet-Multinomial, which allows inference of the 189 changes, across samples, of the proportions of the species DNA biomasses (Fordyce et al., 190 2011; Coblentz et al., 2017; McLaren et al., 2019; Clausen and Willis, 2022), although 191 within-species changes in DNA biomass are argued to be informative (Tkacz et al., 2018). 192 A more detailed comparison between the model we introduce in this paper and models for 193 microbiome data is given in Section 2.1. 194

## 1.3 Structure of the paper

In this paper, we present a unifying hierarchical modelling framework for OTU reads
that considers key sources of variation, noise, and error at both stages of DNA-based
biodiversity surveys (Table 1), while also modelling correlation between species and between
sites. The model allows us to infer changes in DNA biomass and to link these changes to
site-specific covariates.

We use state-of-the-art MCMC (Markov chain Monte Carlo) methods that build on recent work for hierarchical and crossed-effects models (Zanella and Roberts, 2021) as well as adaptive MCMC techniques (Andrieu and Thoms, 2008). In particular, we develop a novel sampling technique to improve mixing in the special case of a multivariate crossed-effect model with PCR-specific random effects, and we use adaptive updates of latent variables to focus sampling effort. This allows us to fit our model (with many latent variables across the different stages of DNA surveys) to data from large numbers of sites, samples per site, PCRs per sample, and species.

The new model, its properties, and links to existing models are presented in Section 2. Details on our approach to inference are given in Section 3. Issues of study design are explored and corresponding simulations are presented in Section 4. A case study of a large Malaise-trap metabarcoding dataset is presented in Section 5, and the paper closes with a discussion in Section 6.

## 214 **2** Model

We assume that  $M_i$  physical samples are collected from site i, i = 1, ..., n, and  $K_{im}$ PCR replicates are performed on the m-th sample from site i. We denote by  $y_{imk}^s$  the
number of DNA reads of the s-th species, s = 1, ..., S in the k-th PCR replicate of the m-th sample collected at the i-th site. We have  $n_z$  site covariates and  $X_i^z$  represents their
value at site i and  $n_w$  sample covariates, represented as  $X_{im}^w$  for the m sample at the i-th
site. In what follows, i indexes sites, m samples, k PCR replicates, and s species.

Our proposed model (see Figure 2) is hierarchical, with three levels. The first level models the amount of DNA biomass of each species at the surveyed sites, which is a function of environmental and landscape covariates as well as between-species and between-sites correlation (**DNA** biomass availability). The second level models the amount of DNA biomass collected for each species in each physical sample from each site (**DNA** biomass collection). Lastly, the third level models the number of reads obtained for each species in each physical sample (**DNA** biomass analysis). Data are

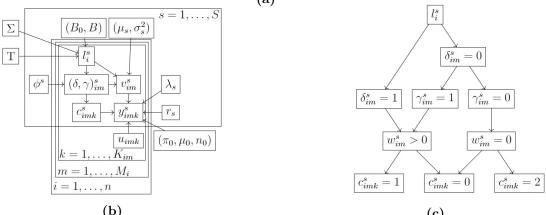
observed only at the third level, as the result of Stage 2 of the survey, with levels one and

229 two corresponding to latent states.

DNA biomass availability 
$$L = \{l_i^s\} \sim \text{MN}(B_0 + X_z B, \Sigma, T), \qquad T^{-1} \sim \text{GH}$$
  
DNA biomass collection

$$\begin{aligned} & \operatorname{logit}(\theta_{im}^s) = \phi_0^s + \phi_1^s l_i^s + X_{im}^w \phi^s \\ & \mathbb{P}(\delta_{im}^s = 1) = \theta_{im}^s, \\ & \mathbb{P}(\gamma_{im}^s = 1 \mid \delta_{im}^s = 0) = \zeta^s, \end{aligned} \quad v_{im}^s \sim \left\{ \begin{array}{ll} \operatorname{N}(\eta_s + l_i^s + X_{im}^w \beta_s^W, \sigma_s^2) & \text{if } \delta_{im}^s = 1 \\ \operatorname{N}(\mu_s, \nu_s^2) & \text{if } \delta_{im}^s = 0, \gamma_{im}^s = 1 \end{array} \right.$$

#### DNA biomass analysis



**Figure 2:** (a): Model summary, (b): Directed acyclic graph representing the relationships between the variables in the model. (c) Graphical representation of the latent indicator variables in the model.

DNA biomass availability We denote the logarithm of the amount of DNA biomass of species s in site i available for collection by  $l_i^s$  and denote the  $n \times S$  matrix L by  $\{L\}_{is} = l_i^s$ . We model DNA biomass correlation between species and spatial correlation between sites by assuming that L follows a matrix normal distribution,  $L \sim \text{MN}(B_0 + X^z B, \Sigma, T)$  (Dawid, 1981), where  $B_0$  is an  $n \times S$  matrix with columns  $1_n \beta_0^s$ , with  $\beta_0^s$  a species-specific intercept,  $X^z$  is a design matrix whose rows are  $X_i^z$ , B is an  $n_z \times S$  matrix of regression coefficients,  $\Sigma$  is an  $\Sigma$  matrix modelling the correlation across sites, and  $\Sigma$  is an  $\Sigma$  matrix modelling the correlation across species. We note that, within this framework, the amount

of DNA biomass of a species at the surveyed site cannot be exactly 0, but can be negligible for modelling purposes as we describe below. We employ a graphical horseshoe (GH) prior (Li et al., 2019) for the inverse species covariance matrix  $Q = T^{-1}$ , which is defined by specifying the following *a priori* independent distributions on each element

$$Q_{ss} \propto \operatorname{Exp}\left(\frac{\lambda}{2}\right), \ s = 1, \dots, p, \quad Q_{ts} = Q_{st} \sim \operatorname{N}(0, \lambda_{st}^2 \tau^2), \ \lambda_{st} \sim C^+(0, 1), \quad s < t \le S$$

subject to the constraint  $T \in \Omega_S$ , where  $\Omega_S$  is the space of the positive definite  $S \times S$ 

matrices,  $C^+$  represents the half-Cauchy distribution (Gelman, 2006), and  $\tau \sim C^+(0,1)$ . Unlike Li et al. (2019) who specified a flat prior  $Q_{ss} \propto 1$ , we follow Wang (2012) and 244 define a proper prior  $Q_{ss} \sim \text{Exp}(\frac{\lambda_{GH}}{2})$ , ensuring that T, which is latent, has a proper 245 posterior. We model the spatial correlation matrix  $\Sigma$  using an exponential kernel function, 246 so that  $\Sigma_{i_1i_2} = \sigma^2 \exp\left\{-\frac{(x_{i_1}-x_{i_2})^2}{l^2}\right\}$ , where  $x_{i_1}$  and  $x_{i_2}$  are the locations of site  $i_1$  and  $i_2$ , 247 respectively. We note that we have accounted for species correlations in the DNA biomass 248 availability stage, but any residual correlations of this type could also be the result of 249 species correlations in the collection or analysis stages, discussed below. It is not possible, 250 with metabarcoding data alone, to identify the source of these inferred correlations, and 251 therefore, species correlations should be interpreted with caution. 252 **DNA biomass collection** We denote by  $w_{im}^s$  the amount of DNA biomass of species s collected in sample m from site i and  $v_{im}^s := \log(w_{im}^s)$ . To account for Stage 1 false negative 254 error at this stage, we introduce the latent variable  $\delta^s_{im}$  that is equal to 1 if DNA biomass 255 for species i has been collected in the m-th physical sample from site i, and 0 otherwise. 256 We assume that  $\delta_{im}^s = 1$  with probability  $\theta_{im}^s$ , which is a function of covariates  $X_{im}^w$ , and 257 of  $l_i^s$ , since higher amounts of DNA biomass are expected to lead to a higher probability 258 of collecting DNA biomass in the sample, leading to logit( $\theta_{im}^s$ ) =  $\phi_0^s + \phi_1^s l_i^s + X_{im}^w \phi^s$ . We 259 note that as  $l_i^s$  tends to  $-\infty$ ,  $\theta_{im}^s$  tends to 0, and therefore the species becomes practically 260 impossible to detect. If the amount of DNA biomass collected is greater than 0 ( $\delta_{im}^s = 1$ ), 261 we model  $v_{im}^s \sim N(\eta_s + l_i^s + X_{im}^w \beta_s^w, \sigma_s^2)$ , where  $\eta_s$  models Stage 1 species effects on the 262 DNA biomass collection rate and  $\sigma_s^2$  models the species-specific Stage 1 noise in the DNA

biomass collection rate. To account for Stage 1 false positive error, we introduce latent 264 variable  $\gamma_{im}^s$ , which is equal to 1 with probability  $\zeta^s$  if the collected DNA biomass is the 265 result of contamination and 0 otherwise. We assume that  $\gamma_{im}^s$  can be 1 only if  $\delta_{im}^s = 0$ 266 and that  $v_{im}^s \sim N(\mu_s, \nu_s^2)$  if  $\gamma_{im}^s = 1$ . In this way, we assume that a sample which already 267 contains DNA biomass of a species cannot be further contaminated by the DNA of the 268 same species from another sample or site. We make this assumption as there is not enough 269 information in the data to partition the collected DNA biomass between that which was 270 truly collected from the site and that which was contamination from elsewhere. 271 **DNA** biomass analysis As mentioned above, by non-negligible reads we mean that some 272 of the PCR product is successfully read by the DNA sequencer. We introduce latent variable 273  $c_{imk}^s$  to model the success of PCR k, sample m, and site i for species s, i.e. Stage 2 error. 274 Firstly, if sample m from site i contains DNA biomass of species s ( $w_{im}^s > 0$ ), PCR run k275 can be successful, i.e. non-negligible reads (true positive),  $c_{imk}^s = 1$ , or not successful, i.e. 276 negligible reads (false negative),  $c_{imk}^s = 0$ , and we assume that  $c_{imk}^s = 1$  with probability 277  $p_s$ . We note that we have assumed here that  $p_s$  only varies by species and not across sites 278 or replicates in either stage. However,  $p_s$  could depend (negatively) on the total amount 279 of DNA biomass in the sample, particularly in cases of low DNA concentration for that species or could vary across primers or between labs. We return to these issues in Section 281 6. Secondly, if sample m from site i does not contain DNA biomass of species s ( $w_{im}^s = 0$ ), 282 PCR run k can be successful if it yields non-negligible reads due to lab contamination 283 (false positive),  $c_{imk}^s = 2$ , or not successful (again,  $c_{imk}^s = 0$ , true negative) and assume 284 that  $c_{imk}^s = 2$  with probability  $q_s$ . 285 We model the reads conditional on  $c_{imk}^s$  as follows. Conditional on  $c_{imk}^s = 1$ ,  $y_{imk}^s \sim$ 286  $NB(\exp(\lambda_s + v_{im}^s + u_{imk} + o_{imk}), r_s)$ , where  $\lambda_s$  models the Stage 2 species effect on the 287 amplification rate,  $u_{imk}$  is the Stage 2 pipeline effect, with  $u_{imk} \sim N(0, \sigma_u^2)$ ,  $o_{imk}$  is an 288 offset modeling the normalisation steps described in Section 1.1, and  $r_s$  is a species-specific 289 variance of the Stage 2 noise. If more than one normalisation step is employed, then

they can all be incorporated into the same offset as a sum. Conditional on  $c_{imk}^s = 0$ ,  $y_{imk}^s \sim \pi \delta_0 + (1 - \pi)(1 + \text{NB}(\mu_0, n_0))$ , that is, there are zero reads with probability  $\pi$ , and non-zero but negligible reads otherwise. Finally, conditional on  $c_{imk}^s = 2$ ,  $y_{imk}^s \sim \text{Pois}(\tilde{\mu}_s)$ . The negative binomial is parameterised in terms of the mean and the number of failures. A visual representation of the PCR process when  $c_{imk}^s = 1$  is shown in Figure 1 of the Supplementary material.

Stage 2 negative control samples (which are known to not contain DNA of any species)
can be easily accounted for in our model by having additional samples for which  $\tilde{\delta}_l^s =$   $\tilde{\gamma}_l^s = 0$ . Accounting for spike-ins corresponds to having  $S^*$  additional species for which  $(v_{im}^{S+1}, \ldots, v_{im}^{S+S^*})$  is known. Since the pipeline effect is shared across all species (including spike-ins), the known values of  $v_{im}^s$  for the spike-ins help to better estimate  $u_{imk}$ . We further investigate this effect in Section 4.

The model is summarised in Figure 2 (a), the directed acyclic graph of the model is 303 shown in Figure 2 (b), while a graphical representation of the latent variables introduced 304 across both stages is shown in Figure 2 (c). The model allows both zero-inflation and 305 overdispersion (even after accounting for zero-inflation) of the reads. In the case of true 306 positives (when  $c_{imk}^s = 1$ ), we allow overdispersion through the negative binomial distribu-307 tion and the introduction of the offset. The use of negative binomial is a standard choice 308 for overdispersed data, particularly in Bayesian modelling. Ver Hoef and Boveng (2007) 309 discuss the merits of negative binomial and quasi-Poisson regression modelling in ecological 310 data. Datta and Dunson (2016) discuss how a scale mixture of negative-binomial regression 311 models can be used for so-called quasi-sparse counts, which are often small, not zero. 312

The model presented in Figure 2 is not identifiable in its general form unless certain constraints are applied, as we discuss below. For example, choosing for simplicity  $\Sigma$  and T to be diagonal, if we define  $\tilde{v}_{im}^s := v_{im}^s - \eta_s - l_i^s$  and  $\tilde{l}_i^s := l_i^s - \beta_0^s$ , the model for  $\theta_{im}^s$  and  $y_{imk}^s$  conditional on  $c_{imk}^s = 1$  and all offsets  $o_{imk}$  set to 0 can be expressed as

$$\begin{cases}
\tilde{l}_{i}^{s} \sim N(X_{i}\beta_{s}^{z}, \tau_{s}^{2}) \\
\tilde{v}_{im}^{s} \sim N(X_{im}\beta_{s}^{w}, \sigma_{s}^{2}) \\
\theta_{im}^{s} = \text{logit}(\phi_{0}^{s} + \phi_{1}^{s}\beta_{0}^{s} + \phi_{1}^{s}\tilde{l}_{i}^{s} + \phi^{s}X_{im}^{s}) \\
y_{imk}^{s} \sim NB\left(\exp(\beta_{0}^{s} + \tilde{l}_{i}^{s} + \eta_{s} + \tilde{v}_{im}^{s} + \lambda_{s} + u_{imk}), r_{s}\right)
\end{cases}$$
that the model is invariant to transformations of the form

It is evident that the model is invariant to transformations of the form

$$(\beta_0^s)^* = \beta_0^s + c + d, \quad (\lambda_s)^* = \lambda_s - c, \quad (\eta_s)^* = \eta_s - d, \quad (\phi_0^s)^* = \phi_0^s - \phi_1^s(c + d).$$

The reason for this unidentifiability is that data are observed only in the third level of 317 the model, and hence the following sets of species-specific parameters are confounded: the 318 baseline amount of DNA biomass across all sites  $(\beta_0^s)$  with the baseline collection rate  $(\eta_s)$ 319 and the baseline amplification rate  $(\lambda_s)$ , and the former again with the baseline detection 320 rate  $\phi_0^s$ . However, by assuming that all these baseline rates are constant across sites, 321 samples, and PCRs, we are able to infer species-specific changes in DNA biomass across 322 sites and therefore covariate effects. 323 For inferential purposes, we reparameterise the model and set the new baseline (log) 324 amount of DNA biomass,  $(\beta_0^s)^*$ , equal to  $\beta_0^s + \eta_s$ , which means that we can only estimate

the sum of the baseline amount of available DNA biomass and the corresponding baseline 326 collection rate for the same species. Similarly, we set the new baseline (logit) collection 327 probability  $(\phi_0^s)^*$ , equal to  $\phi_0^s - \phi_1^s \eta_s$ , since the baseline collection probability is also con-328 founded with the baseline collection rate (equivalent to setting  $\phi_0^s \equiv 0$  and  $\eta_s \equiv 0$  in 329

As a result, we cannot infer the amount of available DNA biomass separately from the 331 collection rate, and hence the estimates of log DNA biomass obtained, as mentioned above, 332 are only meaningful for comparison within each species. For the same reason, comparisons 333 of absolute amount of DNA biomass across species are not meaningful. We also note that 334 depending on the survey design in terms of the number of samples collected per site and 335 the number of PCR replicates per sample, additional sets of parameters can be confounded 336 and not estimable. Specifically, the following pairs of parameters are confounded: 337

• S = 1: pipeline effect  $u_{imk}$  and PCR variance  $r_s$ ,

Equation (1).

330

- K = 1: PCR variance  $r_s$  and sample noise  $\tilde{v}_{im}^s$ ,
- M=1: sample noise  $\tilde{v}^s_{im}$  and site noise  $\tilde{l}^s_i$ .

These are pathological cases that arise when there is no replication at the site/sample/PCR levels. Replication is vital for being able to account for and to estimate the effects of the different sources of noise and error (Buxton et al., 2021), an issue to which we return in Section 4.1. Finally, we note that if the offsets  $o_{imk}$  introduced in the model due to the several normalisations occurring in the pipeline are not recorded, the link between the amount of DNA biomass in the environment and the reads is broken. However, a potential way to restore this link is the introduction of spike-ins, which contribute to the estimation of the "overall" pipeline effects  $\tilde{u}_{imk} = u_{imk} + o_{imk}$ .

## 349 2.1 Special cases

Two models available in the literature (Section 1.2) arise as special cases of our model. First, the Dirichlet-Multinomial model (DMM) (Fordyce et al., 2011) is expressed through the following hierarchy (omitting the indexes m and k to simplify notation):

$$\begin{cases} (y_i^1, \dots, y_i^S) \sim \text{Multi}(N_i, \pi_i^1, \dots, \pi_i^S) \\ (\pi_i^1, \dots, \pi_i^S) \sim \text{Dirichlet}(w\alpha^1, \dots, w\alpha^S) \end{cases}$$
(2)

where  $N_i = \sum_{s=1}^{S} y_i^s$ . The DMM can be seen as a special case of the model described in Section 2, for the Stage 2 process, conditional on  $\delta_i^s = 1$ . Specifically,  $y_i^s \sim \text{NB}(\exp(\lambda_s + 1))$ 354  $v_i^s + u_i$ ,  $r_s$ , and therefore, assuming  $\lambda_s = u_i = 0$ , if  $r_s \to \infty$ , the distribution for  $y_i^s$  con-355 verges to a Pois(exp( $v_i^s$ )). Conditional on  $N_i$ , the model is a Multi  $(N_i, \pi_i^1, \dots, \pi_i^S)$ , where  $\left(\pi_i^1, \dots, \pi_i^S\right) = \left(\frac{\exp(v_i^1)}{\sum_s \exp(v_i^s)}, \dots, \frac{\exp(v_i^S)}{\sum_s \exp(v_i^s)}\right)$ . Next, assuming  $\exp(v_i^s) \sim \operatorname{Gamma}(w\alpha_s, \theta)$ , we 357 obtain  $(\pi_i^1, \dots, \pi_i^S)$  ~ Dirichlet $(w\alpha_1, \dots, w\alpha_S)$ . Finally, as the DMM does not take errors 358 into account, the equivalence with our model can be obtained by setting  $p_s \equiv 1$ . 359 McLaren et al. (2019) propose to account for the Stage 2 species effect in the DMM 360 framework by modelling the probabilities  $(\pi_i^1, \dots, \pi_i^S)$  as  $(\frac{e^1 \tilde{\pi}_i^1}{\sum_s e^s \tilde{\pi}_i^s}, \dots, \frac{e^S \tilde{\pi}_i^S}{\sum_s e^s \tilde{\pi}_i^s})$ , where  $e_s$ 361 models the species-specific efficiencies, which in our model is achieved by using a species-362 specific  $\lambda_s$ . The DMM can be extended hierarchically if nested treatments are considered (Coblentz et al., 2017) by defining a nested prior  $(\alpha^1, \dots, \alpha^S) \sim \text{Dirichlet}(\alpha^1_0, \dots, \alpha^S_0)$  for each level. In our model, this is achieved by a hierarchy of normal priors. This highlights a key difference between the DMM approach and the approach we introduce in this paper, since we model the propagation of the *absolute* amount of DNA biomass across the different stages, while the DMM models the propagation of the *relative* amount of DNA biomass.

Secondly, the occupancy model of Griffin et al. (2020), in the simple case of no covariates,

$$\begin{cases} z_i \sim \text{Be}(\psi) \\ w_{im} \sim \text{Be}(z_i \xi_1 + (1 - z_i) \xi_0) \\ y_{imk} \sim \text{Be}(w_{im} p + (1 - w_{im}) q) \end{cases}$$
(3)

designed for (single-species) qPCR, can be seen as a special case of our model when the information in the counts is not considered. Specifically, letting  $l_i$  be binary, with  $l_i \in \{-\infty, 0\}$ , and defining  $z_i = \exp(l_i)$ , we obtain  $\theta_{im}|(l_i = -\infty) = 0$  and  $\theta_{im}|(l_i = 0) = \log t(\phi_0)$ . Hence, the model for  $\delta$  and c becomes

$$\begin{cases} \delta_{im} \sim \text{Be}(z_i(\text{logit}(\phi_0) + (1 - \text{logit}(\phi_0))\zeta) + (1 - z_i)\zeta) \\ c_{imk} \sim \text{Be}(\delta_{im}p + (1 - \delta_{im})q) \end{cases},$$

which is identical to the Griffin et al. (2020) model after defining  $\xi_1 = \text{logit}(\phi_0) + (1 - \log \operatorname{it}(\phi_0))\zeta$  and  $\xi_0 = \zeta$ .

## 3 Inference

369

Samples can be drawn from the posterior distribution of the parameters using a Gibbs sampler. Posterior sampling is greatly helped by representing the negative binomial distribution as a Gamma-Poisson mixture, which allows many parameters to be updated in closed form from their full conditional distribution.

For the parameters  $\sigma_s$ ,  $\mu_s$ , B and  $B_0$ , the full conditional distribution is available in

For the parameters  $\sigma_s$ ,  $\mu_s$ , B and  $B_0$ , the full conditional distribution is available in closed form, and therefore posterior sampling is straightforward. We use simple random walk Metropolis-Hastings steps for parameters  $\pi$ ,  $\mu_0$ ,  $n_0$ , and  $r_s$  and Metropolis-Hastings steps with a Laplace approximation proposal for the parameters  $l_i^s$ ,  $\lambda_s$ ,  $v_{im}^s$ ,  $u_{imk}$  and  $r_s$ . However, on its own, this naive Gibbs sampler will mix slowly since we have a complex hierarchical model with crossed-effects and many latent variables. We address this by updating parameters in blocks using re-parameterisation and an adaptive updating scheme for the discrete latent variables.

To illustrate our approach to blocking and re-parameterisation, we consider the errorfree version of our model

$$\begin{cases} l_i^s \sim \mathcal{N}(0, \tau_s^2) \\ v_{im}^s \sim \mathcal{N}(l_i^s, \sigma_s^2) \\ u_{imk} \sim \mathcal{N}(0, \sigma_u^2) \\ y_{imk}^s \sim \mathcal{N}(0, \sigma_u^2) \end{cases}$$

$$(4)$$
which improves the properties from its full conditional leads to pro-

A naive Gibbs sampler updating each parameter from its full conditional leads to pro-391 hibitively slow mixing, due to the form of the likelihood where  $\lambda_s$ ,  $v_{im}^s$  and  $u_{imk}$  appear as 392 a sum. To address the slow mixing in the nested effects,  $\lambda_s$  and  $v_{im}^s$ , the use of a centred 393 parameterisation (Papaspiliopoulos et al., 2007) has been suggested, which corresponds to 394 defining  $\bar{v}_{im}^s := \lambda_s + v_{im}^s$  and  $\bar{l}_i^s := \lambda_s + l_i^s$ . However, issues of slow mixing still exist between 395  $\bar{v}_{im}^s$  and  $u_{imk}$  and, as noted by Zanella and Roberts (2021), re-parameterisation does not 396 improve mixing in the case of crossed-effects models. In a classic crossed-effect model of the 397 form  $y_{jkl} \sim N(\lambda + v_j + u_k, \sigma^2)$ , Papaspiliopoulos et al. (2020) propose a collapsed Gibbs sam-398 pler by first jointly sampling  $\lambda$  with  $v_j$  and then  $\lambda$  jointly with  $u_k$ . However, this approach 399 does not scale well in our setup, since it would involve sampling all the  $\lambda_s$  and  $u_{imk}$  jointly, 400 which have dimensions S and the total number of PCR technical replicates  $\sum_{i,m} K_{im}$  re-401 spectively. Zanella and Roberts (2021) propose the use of identifiability constraints on 402 the model, which in Equation (4) correspond to assuming  $\sum_{s} v_{im}^{s} = \sum_{k} u_{imk} = 0$ . Since 403 sampling conditionally on constraints can be challenging, we propose a simpler strategy to 404 improve mixing that is more suited to our framework. We consider re-parameterising to 405 the factor averages  $\hat{v}_{im} = \frac{1}{S} \sum_{s=1}^{S} \bar{v}_{im}^{s}$  and  $\hat{u}_{im} = \frac{1}{K} \sum_{k=1}^{K} u_{imk}$  and the factor increments 406  $\tilde{v}_{im}^s = \bar{v}_{im}^s - \hat{v}_{im}$  and  $\tilde{u}_{imk} = u_{imk} - \hat{u}_{im}$  and performing an update by first sampling jointly the factor means conditional on the increments, that is, from  $(\hat{v}_{im}, \hat{u}_{im} | \tilde{v}_{im}^s, \tilde{u}_{imk})$  and next 408 using the standard updates  $(u_{imk}|v_{im}^1,\ldots,v_{im}^S)$  and  $(v_{im}^j|u_{im1},\ldots,u_{imK})$ . In our simula-409 tions, we have found that jointly updating the factor means considerably improves mixing.

The sampling scheme for the complete model is presented in the Supplementary material. The indicator variables  $(\delta^s_{im}, \gamma^s_{im}, c^s_{imk})$  can be updated directly from their full condi-412 tional distributions but, since there are  $nMS(\bar{K}+2)$  (where  $\bar{K}$  is the average number of 413 PCR replicates) of these variables and often one value of  $(\delta_{imk}, \gamma_{imk}, c_{imk})$  has probability 414 very close to 1, evaluating every full conditional distribution in every iteration can be very 415 time-consuming and computationally wasteful. Therefore, we use a cheap approximation as 416 a proposal in a Metropolis-Hastings step. Specifically, every B iterations, we update the approximation  $\hat{p}((\delta_{im}^s, \gamma_{im}^s, c_{imk}^s) = (\epsilon_1, \epsilon_2, \epsilon_3)) = \frac{1}{T} \sum_{t=1}^T \mathbf{I}\left((\delta_{im}^s)^{(t)}, (\gamma_{im}^s)^{(t)}, (c_{imk}^s)^{(t)}\right) = (\epsilon_1, \epsilon_2, \epsilon_3),$ 418 where  $(\delta_{im}^s)^{(t)}$ ,  $(\gamma_{im}^s)^{(t)}$ ,  $(c_{imk}^s)^{(t)}$  is the value of  $(\delta_{im}^s, \gamma_{im}^s c_{imk}^s)$  at the t-th iteration, I(A) is 419 the indicator function, which takes the value 1 if A is true and 0 otherwise, and T is the number of current iterations. Using this update scheme, we only need to evaluate the 421 likelihood if the state is proposed to change. If the probability of one state is close to 422 one, the adaptive scheme often proposes the current state, which can be accepted without 423 computation. The adaptive scheme does not affect convergence of the MCMC algorithm 424 since the approximation clearly has diminishing adaptation, and the state space of the 425 indicator variables is discrete (see e.g. Roberts and Rosenthal, 2009, for more discussion of 426 conditions for convergence of adaptive MCMC schemes).

## 428 4 Study design

In this section, we use a simplified version of the model to investigate the properties of our modelling approach under different study designs in terms of the number of sites, samples per site, and PCRs per sample, as well as the number of spike-ins. In each section, we consider the estimates of the differences in log DNA biomass, when log DNA biomass is not a function of site-specific covariates (no covariate case), and the estimates of the covariate coefficients when log DNA biomass is a function of a single continuous covariate (regression case). In Section 4.1 we present theoretical results using a continuous version of our model that does not account for error in either stage. In Section 4.2 we fit our model as presented in Section 2 under different scenarios for study design by varying the number

of sites, number of samples per site, and number of PCRs per sample. Finally, in Section
439 4.3, we explore the effect of spike-ins for different levels of noise in each stage of the process
440 and different study designs.

## 4.1 Theoretical results for a simplified version of the model

We consider a normal approximation of the model presented in Section 2, which assumes no species or site correlations, that both stages are error-free by setting  $\theta_{im}^s = p_s = 1$ , and that the variances of the distributions of the noise at each stage are the same across species. As mentioned in Section 2, the use of spike-ins corresponds to the presence of species in the sample for which  $(v_{im}^{S+1}, \ldots, v_{im}^{S+S^*})$  is known. We assume, without loss of generality, that  $v_{im}^{S+j} = 0$  for  $j = 1, \ldots, S^*$ . We have the following proposition.

**Proposition 4.1.** Consider the model  $\lambda_s \sim N(0, \sigma_{\lambda}^2)$  for  $s = 1, ..., S + S^*$  and, for i = 1, ..., n, k = 1, ..., K, m = 1, ..., M,

$$u_{imk} \sim N(0, \sigma_u^2), \quad v_{im}^s \begin{cases} \sim N(l_i^s, \sigma^2), & s = 1, \dots, S \\ = 0, & s = S + 1, \dots, S + S^* \end{cases},$$
$$y_{imk}^s \sim N(u_{imk} + \lambda_s + v_{im}^s, \sigma_y^2), \quad s = 1, \dots, S + S^*$$

where  $\sigma^2$ ,  $\sigma_u^2$  and  $\sigma_y^2$  are known.

(a) If we assume  $p(l_i^s) \propto 1$  and  $\sigma_{\lambda}^2 \in (0, \infty)$  is known, then

$$\operatorname{Var}(l_1^s - l_2^s | y) = \frac{1}{M} \left( \sigma^2 + \frac{\sigma_y^2}{K} \left( 1 + \frac{\frac{\sigma_u^2}{\sigma_y^2}}{\frac{\sigma_u^2}{\sigma_y^2} S^* + 1} \right) \right). \tag{5}$$

<sup>449</sup> (b) If we observe a single covariate  $X_i \stackrel{i.i.d.}{\sim} N(0,1)$  for the i-th site and assume  $l_i^s \sim N(X_i\beta_s,\tau^2)$  with  $\sigma_{\lambda}^2 = \infty$  (i.e.  $p(\lambda_s) \propto 1$ ) and  $p(\beta_s) \propto 1$ , then

$$\operatorname{Var}(\beta_s|y) = \frac{1}{n-1} \left( \tau^2 + \frac{1}{M} \left( \sigma^2 + \frac{\sigma_y^2}{K} \right) \right) \times (1+C) \tag{6}$$

where  $C = \frac{\sigma_u^2}{\sigma_y^2 + (M\tau^2 + \sigma^2)K(1 + S^* \frac{\sigma_u^2}{\sigma_y^2}) + \sigma_u^2(S + S^* - 1)}$ .

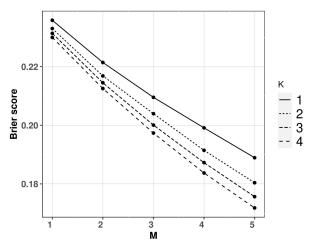
Here  $\sigma_y^2$  models the variance of the noise in Stage 2, as was the case for  $r_s$  in the original model. Equations (5) and (6) show the contributions of the variances at each stage to the posterior variance of the corresponding estimates (changes in biomass between sites, on the log scale, and covariate coefficients, respectively) in this special case.

The results for this special case suggest that, for both  $Var(l_1^s - l_2^s|y)$  and  $Var(\beta|y)$ , 455 increasing replication at a given stage decreases the contribution of the error variance at 456 that stage and all downstream stages. For example, increasing the number of samples Mper site reduces the contribution of the noise variance  $\sigma^2$  at Stage 1 and at all downstream 458 stages, i.e.  $\sigma_y^2$  and  $\sigma_u^2$  in Stage 2. Whereas, increasing the number of PCR replicates, K, 459 only reduces the contribution of the Stage 2 variances ( $\sigma_u^2$  and  $\sigma_y^2$ ). Additionally, the benefit 460 of the spike-in is greater as the ratio of variances  $\frac{\sigma_u^2}{\sigma_u^2}$  increases. Moreover, in the case of 461  $Var(\beta|y)$ , if  $\sigma^2$  is much greater than  $\sigma_y^2$ , the benefit of the spike-in is negligible, as the noise 462 induced by  $\sigma^2$  greatly outweighs the noise that can be mitigated via the use of spike-ins. 463

## 4.2 Simulated results for the full model; varying n, M, and K

We turn our attention to the full model in Fig. 2 and again consider two cases: no 465 covariates and a single covariate,  $X_i \sim N(0,1)$ . In the no covariate case, we consider the 466 model's ability to estimate the correct sign of the difference of species log DNA biomasses at two sites. We use the Brier score  $b(i_1, i_2, s) := (\bar{p}(l_{i_1}^s > l_{i_2}^s) - \delta_{i_1, i_2})^2$ , where  $\bar{p}(l_{i_1}^s > l_{i_2}^s)$  is 468 the posterior probability of  $l_{i_1}^s > l_{i_2}^s$  and  $\delta_{i_1,i_2}$  is 1 if the true value of  $l_{i_1}^s$  is greater than the 469 true value of  $l_{i_2}^s$  and 0 otherwise. We generate  $l_i^s \sim \begin{cases} N(1, \tau_s^2) & i \text{ odd} \\ N(0, \tau_s^2) & i \text{ even} \end{cases}$  which separates 470 the sites between those with "high" DNA biomass and those with "low" DNA biomass. We 471 use S=40 species, n=300 sites,  $M\in\{1,2,3,4,5\}$  samples per site and  $K\in\{1,2,3,4\}$ 472 PCR replicates. The values of the other parameters are reported in the Supplementary 473 Material. We have performed 50 replications for each combination of values of the design parameters, M and K. We report the average  $b(i_1, i_2, j)$  spanning  $i_1$  across the sites with 475 low DNA biomass,  $i_2$  across the sites with high DNA biomass, and s across all species

and across the replicates. As expected, the Brier score decreases, and hence the ability to distinguish between sites with low and high DNA biomass increases, as M and K increase (Figure 3). However, the benefit of increasing K decreases with M, which highlights the greater importance of multiple sample replicates per site in Stage 1.



**Figure 3:** Brier score for distinguishing high and low DNA biomass sites, as a function of the number of samples (M) and number of PCR replicates (K). We have only considered  $M \leq 5$ , since greater M is unrealistic, and set n = 300.

In the regression case, we consider the absolute error and posterior standard deviation of the covariate coefficient  $\beta_s$ . We use  $n \in \{50, 100, 200\}$  sites,  $M \in \{1, 2, 3\}$  samples per site and  $K \in \{1, 2, 3\}$  PCR replicates per sample and S = 40 species. The values of the other parameters are reported in the Supplementary Material. We performed 50 replicates for each combination of values of the design parameters and averaged results across all replicates and species. Results are shown in Figure 4.

As expected, absolute error and posterior standard error both decrease with more sites n, samples per site M, and PCRs per sample K. Doubling the number of sites from 50 to 100 has a bigger effect than doubling them again from 100 to 200, suggesting that the benefit of increasing the number of sampled sites decreases as the number of sites gets large. Collecting two samples per site instead of one drastically decreases both absolute error and posterior standard deviation, whereas the effect is less pronounced when the number of samples is further increased to three compared to two, and the same can be said about the number of PCRs.

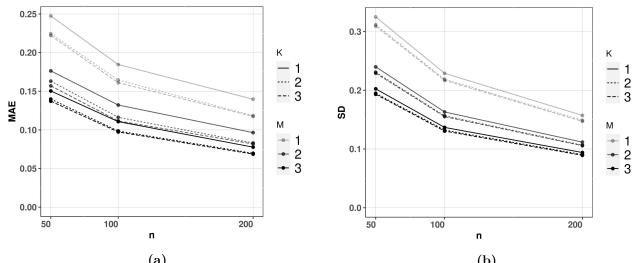


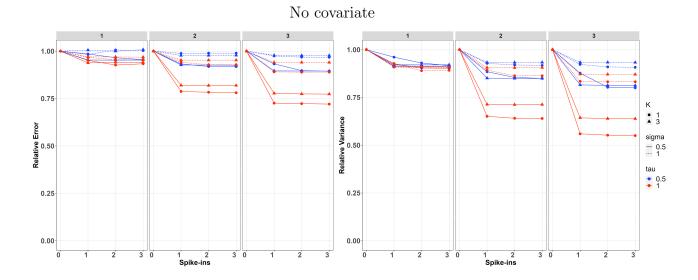
Figure 4: Mean absolute error, (a), and posterior standard deviation, (b), averaged across all species and all simulations, of the covariate coefficient  $\beta^s$  for varying numbers of sites (n), samples per site (M), and numbers of PCR replicates per sample (K).

## 4.3 Spike-ins

In this section, we consider the improvement in inference when  $S^*$  spike-ins are employed in Stage 2. The effect of the spike-ins is maximised in the case of no false negative/positive errors, otherwise the benefit of the spike-ins is lower, and dependent upon the level of error. Therefore, in this section we consider data and corresponding model with no false positive/negative errors.

We simulated data on n = 300 sites,  $M \in \{1, 2, 3\}$  samples per site, and  $K \in \{1, 3\}$ PCR replicates per sample on S = 10 species. For each setting of M and K, we have fitted the model when  $S^* \in \{0, 1, 2, 3\}$  and report in each case the posterior relative error and posterior relative variance of the estimates, which are calculated by dividing the posterior error/variance by the corresponding error/variance when using  $S^* = 0$  (which is the case with the greatest error/variance).

Results of the simulation study are presented in Figure 5. In both cases, improvements diminish for  $S^* \geq 2$ , and in most cases  $S^* = 1$  already provides most of the improvement, suggesting that the benefit of more than one spike-ins is minimal. The no covariate case is shown in the first row of Figure 5. Spike-ins contribute more to reducing biomass-



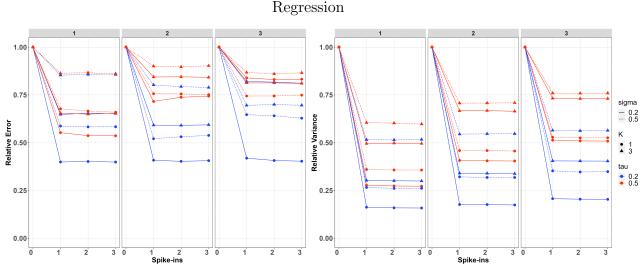


Figure 5: Effect of spike-ins on inference. The three facets per figure represent simulations with M=1/2/3 samples per site. The between-samples standard deviation,  $\sigma$ , is represented by the line type, the between-sites standard deviation,  $\tau$ , is represented by the color, the number of PCR replicates, K, is represented by the symbols. The first column represents the posterior relative error of the estimates and the second column represents the posterior relative variance.

improvements for any setting considered in the simulation. When M > 1, improvement is more pronounced when K = 1 instead of K = 3, because in the latter case, thanks to this replication at Stage 2, there is already increased information for estimating the pipeline effect. This is particularly true when  $\tau$  is 1 instead of 0.5, because in this case, the differences between sites are more pronounced. For both values of  $\tau$ , improvements are bigger when the between-samples standard deviation  $(\sigma)$  is smaller, since otherwise, Stage 1 noise dominates the process and understanding noise in Stage 2 decreases the overall

variance proportionally less.

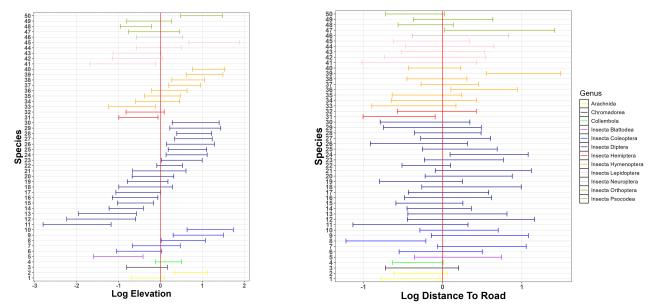
The second row of Figure 5 shows the regression case. We have chosen smaller values 520 for  $\sigma$  and  $\tau$  (.2 and .5), since the relative contribution of the spike-ins is negligible with 521 larger values. Spike-ins contribute more to reducing error and variance when the between-522 samples standard deviation  $(\sigma)$  and the between-sites standard deviation  $(\tau)$  is smaller 523 because, similar to before, the noise at early stages dominates the process, and therefore 524 the relative contribution of the spike-ins is smaller. Also similar to the no covariate case, the contribution of the spike-ins is higher for K = 1 PCR replicates compared to K = 3. 526 However, unlike that case, the contribution does not appear to increase as the number of 527 samples per site M increases.

## 529 5 Case study

We apply our model to an unpublished amplicon sequencing dataset of arthropod invertebrates collected using 121 Malaise-trap samples from 89 sample sites in the H.J. Andrews
Experimental Forest (HJA), Oregon, USA (225 km²) in July 2018 (site details are provided
in Li et al. 2024). Each trap was left to collect for seven days, and samples were transferred
to fresh 100% ethanol to store at room temperature until extraction. The management objective that motivated the collection of this dataset is to interpolate continuous species
distributions among the 89 sample points so that areas of higher and lower conservation
value at the HJA can be identified.

For each sample, the collected invertebrate samples were combined with a lysis buffer, in an amount proportional to the starting sample mass, to digest the tissue, and a fixed aliquot was then taken from the overall mixture (and recorded) for DNA extraction and subsequent three PCRs. This normalization, as described in Section 2, was accounted for in the model by setting the offset  $o_{imk}$  equal to the log ratio between the aliquot and the overall amount of liquid mixture in each case. We included 50 species in the study by selecting the species that have the most non-zero counts across all PCR replicates. Log DNA biomass is modelled as a function of two environmental covariates: log elevation and log distance-to-road.

Figure 6 presents the 95% posterior credible intervals (PCIs) for the species-specific coefficients of log elevation and log distance-to-road in the model for log DNA biomass. The effects of the covariates on species DNA biomass are not consistent within each taxonomic order, which suggests low phylogenetic inertia at this rank for response to these landscape characteristics. Elevation is a stronger predictor for species DNA biomass than distance-to-road for this ecosystem. This makes ecological sense, since distance-to-road is only expected to exert an effect over about 100 meters, via canopy openness, whereas elevation exerts a pervasive effect via its effects on temperature, precipitation, and vegetation.



**Figure 6:** Case study: 95% PCI of the species-specific coefficients of log elevation (left) and distance to road (right) in the model for log DNA biomass. Species are grouped taxonomically.

Figure 7 (a) presents the posterior mean of the between-species residual correlations.

We set  $\lambda_{GH} = 1$  in the GH prior and we emphasize that the GH prior assumes no prior structure imposed on the taxa. Species in the Diptera (flies, spp. 14-30) exhibit higher positive correlations with each other, as well as with several species in the Hymenoptera (ants, bees, and wasps) and Lepidoptera (butterflies and months). We conservatively interpret these positive residual correlations as indicative of unmeasured environmental covariates, such as canopy openness, rather than of biotic interactions. We also note that two species in

the Lepidoptera, (spp. 41, 43), one in the Hymenoptera (sp. 33), and one in the Psocodea (barklice, sp. 50) are among the few species showing strong negative residual correlation 563 with many of the other species, and again, we conservatively interpret these correlations 564 as indicative of unmeasured environmental covariates. There is a strongly positive, pair-565 wise correlation between two tabanid fly species Hybomitra liorhina and Hybomitra sp. 566 (spp. 12, 13), which might indicate the oversplitting of one biological species into two 567 OTUs during the bioinformatic pipeline. Finally, there is also a strongly positive, pairwise 568 correlation between the moth species Ceratodelia queneata (sp. 44) and the predatory fly 569 (Scathophagidae, Microprosopa sp., (sp. 20), which might indeed indicate a specialised 570 predator-prey relationship. All that said, we highlight that these inferred correlations have 571 been accounted for in the DNA availability stage of the model, but, as we discuss in Section 572 2, they can also be the result of the DNA biomass collection or analysis stages, so should 573 be interpreted with caution. 574

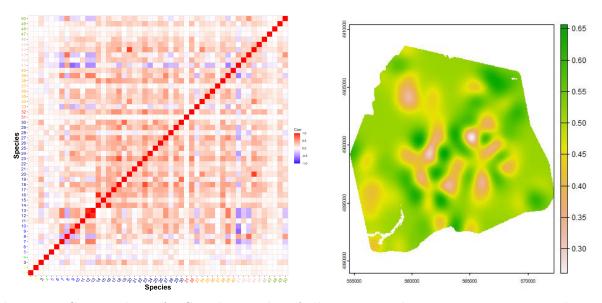


Figure 7: Case study. Left: Correlation plot of all species. Red represents positive correlations while blue represents negative correlations. Species are grouped taxonomically. Right: Posterior mean of biomass-weighted species richness across the study area. For each species, we rescale the log-biomass amount across all study sites into the range [0,1] and next we compute the species richness as the sum of all the rescaled biomasses across all species.

In Figure 7 (b), we show the biodiversity map for the area, which is useful for identifying areas of higher species richness and compositional distinctiveness, which together can be

used to identify areas of higher conservation value (i.e. higher 'site irreplaceability' sensu
Baisero et al., 2022). The predicted mean log DNA biomasses on a continuous map over
the HJA for all individual species are presented in the Supplementary Material. These can
be used to identify species with a wide spatial range, such as the click beetle (Megapenthes
caprella), or with a restricted range, such as the leafhopper (Osbornellus borealis).

Finally, Figure 8 (a) suggests that generally, there is a similar amount of variation 582 between sites and between samples for these species. As suggested by Figure 8 (b), the 583 species that we have considered have similar collection probabilities across the several sites, 584 possibly due to the fact that the most frequently detected species across PCRs have been 585 selected. Figure 8 (c) demonstrates, as expected, that the Stage 2 true positive probability 586 is close to 1 for all species. We highlight here that this probability is modelled as species-587 specific but assumed constant across all replicates. Similarly, the figure also suggests that 588 the probability of a Stage 2 false negative error is very close to 0 for all but three species. 589 One of these three (sp. 14) is in the fly family Tachinidae, which are parasitoids of other insects and thus might have been collected not only as adults but also occasionally as eggs 591 attached to the adults of other (insect) host species, with the latter case being classified as 592 false positives in Stage 2, given that an egg would contribute very low amounts of starting 593 DNA biomass. 594

elfig:cov results

595

## $_{597}^{596}$ 6 Discussion

Over the last decade, DNA-based biodiversity studies, primarily using metabarcoding, have rapidly increased in popularity, and multivariate statistical models are now starting to be deployed to analyse metabarcoding data (e.g. Lin et al., 2021; Pichler and Hartig, 2021; Abrego et al., 2021; Fukaya et al., 2022; Ji et al., 2022). Our paper provides the first unifying modelling framework that considers and quantifies key sources of variation, error and noise in metabarcoding surveys (Table 1). As a result, our modelling framework allows more reliable and more powerful biodiversity monitoring and inference on species

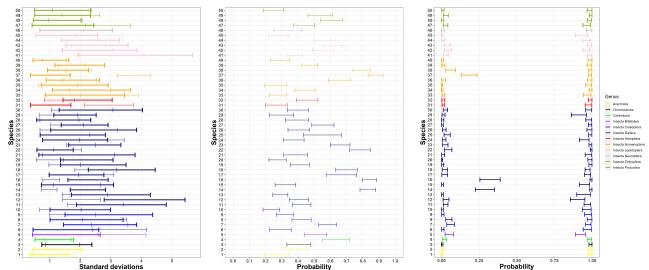


Figure 8: Case study: (left) 95% PCI of the species-specific between-samples standard deviation  $\sigma_s$  and between-sites standard deviation  $\sqrt{T_{ss}}$  (in bold). (center) 95% PCI of the species-specific average collection probability  $\theta_{im}^s$  across all sites. (right) 95% PCI of the species-specific Stage 2 false-positive probabilities  $q_s$  (on the left of the plot) and true-positive probabilities  $p_s$  (on the right of the plot). Species are grouped taxonomically.

responses to landscape characteristics than has been possible before. We have employed, extended, and developed a number of inferential tools to deal with the complexity of the 606 proposed hierarchical model, which involves two latent stages and a large number of latent 607 variables. Finally, this is the first modelling approach that accounts for spike-ins and 608 negative controls (empty tubes), which are widely used quality-control methods in DNA-609 based biodiversity surveys but rarely explicitly considered within a modelling framework. 610 We explored the benefits of spike-ins on inference and provided analytical and simulation 611 results of the effects of study design choices on parameter estimates. As is the case in all 612 models, we make certain assumptions about the data-generating process and if (any of) 613 these assumptions are violated, then inference can be biased. Below, we discuss the key 614 assumptions and corresponding model extensions, when appropriate. 615

Our new framework allows us to infer and map species DNA biomass change across surveyed sites (Figure 7 (b)), and to link these to landscape characteristics (Figure 6).

The resulting maps can be used to identify areas of high conservation value, as well as areas where particular species or groups of species are more or less prevalent, and to detect species-specific shifts, expansions, and shrinkage. We are also able to study pairwise

correlations across large numbers of species (Figure 7 (a)), which is considerably more scalable using metabarcoding data than using standard observational data. We note that, 622 as discussed in the corresponding sections of the model and the case study, we cannot 623 unambiguously identify the sources of the estimated correlations using the available data 624 alone, as factors other than the affinity between species, such as competition for primers, 625 could affect the inferred species correlations. We have shown that using spike-ins can 626 substantially increase inference accuracy for parameters of interest (Figure 5). Our results also demonstrate that the current practice of collecting a single sample from each surveyed 628 site considerably reduces our ability to infer changes in species DNA biomass and that 629 replication at both stages as well as the use of normalisation-ratio offsets or spike-ins is the 630 optimal approach to designing metabarcoding studies (Figure 3). 631

In metabarcoding data, the baseline DNA biomass of each species is confounded with its 632 species-specific collection and amplification rates. Hence, we cannot infer absolute values 633 of species-specific DNA biomass across sites using metabarcoding data alone. However, 634 by assuming that baseline species-specific collection and amplification rates are the same 635 across sites, samples, and PCR replicates, we can infer species-specific DNA biomass change 636 across sites, species-specific covariate effects, and pairwise species correlations. Finally, we model species amplification rates as independent random effects, but competition between 638 species for primers, polymerases and nucleotides during PCR amplification might violate 639 this independence assumption, and future experimental work, alongside model extensions, 640 should explore this issue further. 641

We note that we have not allowed the probability of Stage 2 species detection,  $p_s$ , to vary between samples or PCR replicates, and hence we have assumed that it does not depend on the DNA biomass of other species in the sample/PCR replicate. However, because of the PCR product normalisation step, described in Section 1.1, in PCR replicates with relatively high resulting overall DNA biomass, relatively low-DNA-biomass species might be less likely to be drawn in high enough concentration to be detected, an issue that is

often referred to as PCR dropout. Empirically, it is known that such PCR competition can be mitigated by using a lower number of PCR cycles (Yang et al., 2021) and by sequencing 649 each sample replicate more deeply. When extending the model of this paper, Stage 2 species 650 detection can be modelled as a function of DNA biomass, so that  $logit(p_{imk}^s) = \beta_0^p + \beta_p(v_{im}^s +$ 651  $o_{imk}$ ). Model extensions of this type are important but are expected to introduce further 652 identifiability issues and computational challenges and hence require careful investigation. 653 Generally, modelling changes in (proxies of) abundance, such as changes in DNA 654 biomass, is a more powerful monitoring tool than modelling changes in species presence 655 across survey sites (Joseph et al., 2006). Metabarcoding studies yield count data without 656 any consequence on associated cost, and hence overcome the time and cost implications associated with collecting count data for multiple species. Our model uses the raw count 658 data, and does not rely on ad-hoc rules about what constitutes a practically zero count for 659 converting them to binary data, which has been the standard practice thus far (Ovaskainen 660 et al., 2017; Bush et al., 2020). To model changes in (log)biomass for each species across 661 sites, we rely on the investigator being able to record any normalisation steps (or to include 662 a spike-in), otherwise the relationship between change in read counts and change in the 663 amount of biomass in the environment cannot be inferred, and instead the counts can only be used to infer composition, as is standard practice in metabarcoding studies. We have 665 allowed for over-dispersion in the count data using a negative binomial distribution, but 666 future work could consider alternative parametrisations, such as the discrete Weibull distri-667 bution. The model can also be extended to account for multiple primers or for differences 668 between labs, if samples are processed by more than one lab, by introducing regression 669 models for corresponding parameters. 670 671

Metabarcoding studies, particularly when applied to microbiomes and meiofauna (e.g. nematodes, micro-eukaryotes), can detect 1000s of species, which leads to large numbers of latent variables and coefficients in the model. There are several ways that the inferential tools presented here could be further extended to scale to these cases. Firstly, the posterior

distribution conditional on the  $u_{imk}$  is independent across species. If  $u_{imk}$  could be estimated at a first stage then inference across species could be easily parallelized. Secondly, 676 variational Bayes methods could be applied to avoid the use of sampling methods. The 677 choice of variational distribution will be important and can exploit the conditional normal-678 ity of much of the model. Alternatively, the model could be adapted by assuming that the 679 coefficient matrices such as  $\beta^z = (\beta_1^z, \dots, \beta_S^z)$ , have a low-dimensional representation. We 680 highlight that in its current format, the model assumes species-specific parameters, and 681 hence there is potentially a large number of parameters to be estimated for each species. 682 Therefore, if a species only has a few non-zero PCR reads from potentially only a few sites, 683 estimating all of these species-specific parameters is difficult. Future work should explore sharing parameters between species, making inference for rarely-observed species possible. 685 We are not modelling species presence absence and instead we have focused on mod-686 elling biomass on a continuous scale. As a result, we cannot infer whether a species is 687 absent from a particular study site, but instead only if its DNA biomass at a given site is 688 practically zero. We have assumed that a sample which already contains DNA biomass of 689 a species cannot be further contaminated by the DNA of the same species from another 690 sample or site in Stage 1. This is a reasonable but also necessary assumption, because of model identifiability issues otherwise. It is possible that there exists contamination from 692 other sites if their samples are all processed in the same laboratory, especially at the same 693 time, or that there is contamination during the collection or transfer of samples. However, 694 with only metabarcoding data to hand, it is not possible to identify the source of contami-695 nation, or to model the possibility that a sample that contains DNA of a species has been 696 further contaminated by the DNA of the same species from another sample or site in Stage 697 1. This is yet another reason to take measures that minimise contamination risk. 698 eDNA metabarcoding has revolutionised the cost-effectiveness, precision, and scale at 699 which biodiversity assessment can be performed. Nevertheless, the multiple stages at which 700

imperfect detection of DNA biomass can occur during the workflow are not insignificant. By

- facilitating estimates of within-species changes in DNA biomass as a function of covariates,
- while accounting for workflow uncertainties, our modelling framework provides a substantial
- <sup>704</sup> improvement in the design and analysis of eDNA metabarcoding data.

## $_{\scriptscriptstyle{05}}$ Data Availability

The sequence data, bioinformatic scripts, and the three sample by species tables and environmental covariates are archived on DataDryad at doi.org/10.5061/dryad.4f4qrfjjb.

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