

# A Methodology to Identify Consensus Classes from Clustering Algorithms Applied to Immunohistochemical Data from Breast Cancer Patients

Daniele Soria<sup>a</sup>, Jonathan M. Garibaldi<sup>a,\*</sup>, Federico Ambrogi<sup>c</sup>, Andrew R. Green<sup>b</sup>, Des Powe<sup>b</sup>, Emad Rakha<sup>b</sup>, R. Douglas Macmillan<sup>f</sup>, Roger W. Blamey<sup>f</sup>, Graham Ball<sup>d</sup>, Paulo J.G. Lisboa<sup>e</sup>, Terence A. Etchells<sup>e</sup>, Patrizia Boracchi<sup>c</sup>, Elia Biganzoli<sup>c</sup>, Ian O. Ellis<sup>b</sup>

<sup>a</sup>*School of Computer Science, University of Nottingham, Jubilee Campus, Wollaton Road, Nottingham, NG8 1BB, UK*

<sup>b</sup>*School of Molecular Medical Sciences, Nottingham University Hospitals and University of Nottingham, Queens Medical Centre, Derby Road, Nottingham, NG7 2UH, UK*

<sup>c</sup>*Institute of Medical Statistics and Biometry, University of Milan, Via Venezian 1, 20133 Milan, Italy*

<sup>d</sup>*School of Science and Technology, Nottingham Trent University, Clifton Campus, Clifton Lane, Nottingham, NG11 8NS, UK*

<sup>e</sup>*School of Computing and Mathematical Sciences, Liverpool John Moores University, Byrom Street, Liverpool, L3 3AF, UK*

<sup>f</sup>*The Breast Institute, Nottingham City Hospital, Hucknall Road, Nottingham, NG5 1PB, UK*

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## Abstract

Single clustering methods have often been used to elucidate clusters in high dimensional medical data, even though reliance on a single algorithm is known to be problematic. In this paper, we present a methodology to determine a set of ‘core classes’ by using a range of techniques to reach consensus across several different clustering algorithms, and to ascertain the key characteristics of these classes. We apply the methodology to immunohistochemical data from breast cancer patients. In doing so, we identify six core classes, of which several may be novel sub-groups not previously emphasised in literature.

*Key words:* breast cancer, molecular classification, clustering methods, consensus clustering, validity indices

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## 1. Introduction

Breast cancer, the most common cancer in women [1, 2], is a complex disease characterized by multiple molecular alterations. Current routine clinical management relies on availability of robust clinical and pathologic prognostic and predictive factors to support decision making. Recent advances in high-throughput molecular technologies supported the evidence of a biologic heterogeneity of breast cancer.

Following the seminal paper of Eisen and colleagues [3], in which hierarchical clustering and visual inspection of the dendrogram were performed to discover unknown pattern of gene associations, the use of clustering has become more and more popular, especially for discovering profiles in cancer with respect to high-throughput genomic data. Perou et al. [4] identified four molecular distinct breast cancer groups

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\*Corresponding author. School of Computer Science, University of Nottingham, Jubilee Campus, Wollaton Road, NG8 1BB, UK. Tel.: +44 115 95 14216

*Email addresses:* [jmg@cs.nott.ac.uk](mailto:jmg@cs.nott.ac.uk) (Jonathan M. Garibaldi)

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3 based on gene expression profiles using a hierarchical clustering algorithm: luminal epithelial/estrogen (ER)  
4 positive, HER2 positive, basal-like and normal breast-like. A subsequent study extended this by dividing  
5 the luminal/ER positive group into three subtypes: luminal-A, B, and C [5], but the luminal-C group was  
6 later eliminated [6]. Sotiriou et al. [7] showed six similar groups, with two basal-like subgroups and no  
7 normal breast-like group. Whilst numerous studies have reported these and other novel molecular subtypes,  
8 and assigned a prognostic significance to the proposed classes [8, 9, 10], they remain varied in their detailed  
9 classification [11]. An alternative approach to gene expression profiling is to use established robust laboratory  
10 technology, such as immunocytochemistry on formalin fixed paraffin embedded patient tumour samples. We  
11 and others have applied protein biomarker panels with known relevance to breast cancer, to large numbers  
12 of cases using tissue microarrays, exploring the existence and clinical significance of distinct breast cancer  
13 classes [12, 13, 14, 15, 16, 17, 18, 19]. In particular, in [12] five breast cancer classes were identified and  
14 characterised. Note that a sixth group of only four cases was also identified but considered too small  
15 for further detailed assessment. However, these studies have not addressed the stability of the proposed  
16 classifications across different case sets, assay methods and data analysis procedures. Such an issue appears  
17 of critical relevance considering the increase in the number of features involved in bioinformatics analyses.

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19 In order to deal with the stability of classifications and in particular of clustering techniques, several  
20 studies have focused on the comparison and concordance among different clustering methods defining what  
21 is now known as the ‘consensus clustering’. Monti and colleagues presented a new methodology of class  
22 discovery and clustering validation tailored to the task of analyzing gene expression data [20]. The new  
23 methodology, termed ‘consensus clustering’, provides a method, in conjunction with resampling techniques,  
24 to represent the consensus across multiple runs of a clustering algorithm and to assess the stability of the  
25 discovered clusters. The basic assumption of this method was the following: if the data represent a sample of  
26 items drawn from distinct sub-populations, and if a different sample drawn from the same sub-populations  
27 were to be observed, the induced cluster composition and number should not be radically different. Therefore,  
28 the more the attained clusters are robust to sampling variability, the more one can be confident that these  
29 clusters represent real structure.

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31 Swift and colleagues used consensus clustering to improve confidence in gene-expression analysis, on  
32 the assumption that microarray analysis using clustering algorithms can suffer from lack of inter-method  
33 consistency in assigning related gene-expression profiles to clusters [21]. To assess gene-expression cluster  
34 consistency, the use of the weighted-kappa metric was analysed. This metric rates the agreement between  
35 the classification decisions made by two or more observers. In this case the two observers are the clustering  
36 methods.

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38 Filkov and Skiena proposed a methodology for consensus clustering as an approach to integrating diverse  
39 sources of similarity clustered microarray data [22]. They proposed to exploit the popularity of cluster  
40 analysis of biological data by integrating clusterings from existing data sets into a single representative

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3 clustering based on pairwise similarities of the clusterings. Under reasonable conditions, the consensus  
4 cluster should provide additional information to that of the union of individual data analyses. The goals  
5 of consensus clustering are to integrate multiple data sets for ease of inspection, and to eliminate the likely  
6 noise and incongruencies from the original classifications. In terms of similarity the consensus partition  
7 should be close to all given ones, or in terms of distance, it must not be too far from any of them. One way  
8 to do this is to find a partition that minimises the distance to all the other partitions. So, given  $k$  different  
9 partitions, the target one was identified as the consensus partition.  
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12 In another approach [23], robust clusters were identified by the implementation of a new algorithm  
13 termed ‘Clusterfusion’. ‘Clusterfusion’ takes the results of different clustering algorithms and generates  
14 a set of robust clusters based upon the consensus of the different results of each algorithm. Firstly, an  
15 agreement matrix was generated with each cell containing the number of agreements amongst methods for  
16 clustering together the two variables represented by the indexing row and column indices. This matrix was  
17 then used to cluster variables based upon their cluster agreement. In essence, a clustering technique was  
18 applied to the clustering results.  
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21 The idea of combining and comparing the results of different clustering algorithms is particularly impor-  
22 tant in order to evaluate the stability of a proposed classification. In this paper, a methodology is presented  
23 to evaluate the stability of six breast cancer classes by comparing the clustering solutions provided by dif-  
24 ferent algorithms. In order to address the standard problem of consensus clustering in which the label of  
25 classes is arbitrary, a label was assigned using the six clusters characterised in the work of Abd El-Rehim  
26 [12], as a reference for the description of our resulting groups.  
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## 36 **2. Material and Methods**

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39 The four-step methodology for elucidating core, stable classes (groups) of data from a complex, multi-  
40 dimensional dataset was as follows:  
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- 42 1. A variety of clustering algorithms were run on the data set (see Section 2.1).
- 43 2. Where appropriate, the most appropriate number of clusters was investigated by means of cluster  
44 validity indices (see Section 2.2).
- 45 3. Concordance between clusters, assessed both visually and statistically, was used to guide the formation  
46 of stable ‘core’ classes of data.
- 47 4. A variety of methods were utilised to characterise the elucidated core classes.  
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54 The methodology was applied to a well-known set of data concerning breast cancer patients [12] (see Sec-  
55 tion 2.5) in order to obtain core classes. Once these core classes were obtained, the clinical relevance of  
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3 the corresponding patient groups were investigated by means of associations with related patient data. All  
4 statistical analysis was done using *R*, a free software environment for statistical computing and graphics [24].  
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### 7 *2.1. Clustering algorithms*

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9 Five different algorithms were used for cluster analysis:

- 10 i. Hierarchical (as per our previous study [12])
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- 12 ii. K-means (KM)
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- 14 iii. Partitioning around medoids (PAM)
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- 16 iv. Adaptive resonance theory (ART)
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- 18 v. Fuzzy c-means (FCM)
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#### 22 *2.1.1. Hierarchical clustering*

23 The hierarchical clustering algorithm (HCA) begins with all data considered to be in a separate cluster.  
24 It then finds the pair of data with the minimum value of some specified distance metric; this pair is then  
25 assigned to one cluster. The process continues iteratively until all data are in the same (one) cluster. A  
26 conventional hierarchical clustering algorithm (HCA) was utilised, utilising Euclidean distance on the raw  
27 (unnormalised) data with all attributes equally weighted.  
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#### 33 *2.1.2. K-means clustering*

34 The K-means (KM) technique aims to partition the data into  $K$  clusters such that the sum of squares  
35 from points to the assigned cluster centres is minimised. The algorithm repeatedly moves all cluster centres  
36 to the mean of their Voronoi sets (the set of data points which are nearest to the cluster centre). The  
37 objective function minimised is:  
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$$40 \quad J(V) = \sum_{j=1}^k \sum_{i=1}^{c_j} \|x_i - v_j\|^2$$

41 where  $x_i$  is the  $i$ -th datum,  $v_j$  is the  $j$ -th cluster centre,  $k$  is the number of clusters,  $c_j$  is the number of  
42 data points in the cluster  $j$  and  $\|x_i - v_j\|$  is the Euclidean distance between  $x_i$  and  $v_j$ .  
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47 The  $j$ -th centre  $v_j$  can be calculated as:

$$48 \quad v_j = \frac{1}{c_j} \sum_{i=1}^{c_j} x_i, \quad j = 1, \dots, k.$$

49 K-means clustering is dependent on the initial cluster centres setting (which, in turn, determines the  
50 initial cluster assignment). Various techniques have been proposed for the initialisation of clusters [25], but  
51 for this study we used a fixed initialisation of the cluster centres obtained with hierarchical clustering. The  
52 number of clusters is an explicit input parameter to the K-means algorithm.  
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### 2.1.3. Partitioning around medoids

The partitioning around medoids (PAM) algorithm (also known as the  $k$ -medoids algorithm) is a technique which attempts to minimise the distance between points labelled to be in a cluster and a point designated as the centre of that cluster. In contrast to the K-means algorithm, PAM chooses data points as centres (the so-called medoids) and then assigns each point to its nearest medoid. A medoid is defined as the object within a cluster for which the average dissimilarity to all other objects in the cluster is minimal, i.e. it is the most centrally located datum in the given cluster. Dissimilarities are nonnegative numbers that are small (close to zero) when two data points are ‘near’ to each other and become large when the points are very different [26]. Usually, a Euclidean metric is used for calculating dissimilarities between observations.

The algorithm consists of two phases: the *build* phase in which an initial set of  $k$  representative medoids is selected and the *swap* phase in which a search is carried out to improve the choice of medoids (and hence the cluster allocations). The algorithm is described in detail in [26], pp.102–104. The number of clusters is an explicit input parameter to the PAM algorithm.

### 2.1.4. Adaptive resonance theory

The adaptive resonance theory (ART) algorithm has three main steps [27]. First, the data are normalised to a unit hypersphere, thus representing only the ratios between the various dimensions of the data. Second, data allocated to each cluster are required to be within a fixed maximum solid angle of the group mean, controlled by a so-called ‘vigilance parameter’  $\rho$ , namely  $X_k \cdot P^i \leq \rho$ . However, even when the observation profile and a prototype are closer than the maximum aperture for the group, a further test is applied to ensure that the profile and prototype have the same dominant covariates. This is done in a third step by specifying the extent to which the nearest permissible prototype allocation for the given observation must be on the same side of the data space from the diagonal comprising a vector of ones,  $\hat{1}$ , using a pre-set parameter,  $\lambda$ :

$$X_k \cdot P^i \leq \lambda X_k \cdot \hat{1}.$$

The ART algorithm is initialised with no prototypes and creates them during each successive pass over the data set. It has some, limited, sensitivity to the order in which the data are presented and converges in a few iterations. In the ART algorithm the clusters are determined automatically: the number of clusters is not an explicit parameter, although there are parameters that can adjust the number obtained.

### 2.1.5. Fuzzy c-means

The fuzzy c-means (FCM) algorithm is a generalisation of the K-means algorithm which is based on the idea of permitting each object to be a member of *every* cluster to a certain degree, rather than an object having to belong to only one cluster at any one time. It is based upon the concept of fuzzy logic promulgated

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3 by Zadeh [28] and aims to minimise the objective function

$$4 \quad J(U, V) = \sum_{i=1}^n \sum_{j=1}^c (\mu_{i,j})^m \|x_i - v_j\|^2$$

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8 where  $n$  is the number of data points,  $x_i$  and  $v_j$  are the data points and cluster centres and  $\mu_{i,j}$  is the  
9 membership degree of data  $x_i$  to the cluster centre  $v_j$  ( $\mu_{i,j} \in [0, 1]$ ).  $m$  is called the ‘fuzziness index’ and  
10 the value of  $m = 2.0$  is usually chosen. An exhaustive description of this method can be found in [29]. As  
11 for K-means, the number of clusters is an explicit input parameter to FCM.  
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## 15 2.2. Cluster validity

16 Clustering validity is a concept that is used to evaluate the quality of clustering results. If the number of  
17 clusters is not known prior to commencing an algorithm, a cluster validity index may be used to determine  
18 the best number of clusters for the given data set. Although there are many variations of validity indices,  
19 they are all either based on considering the data dispersion in a cluster and between clusters, or considering  
20 the scatter matrix of the data points and the one of the clusters centers. In this study, the following indices  
21 were applied to those algorithms for which the number of clusters is an explicit parameter, over a range of  
22 number of clusters:  
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- 29 1. Calinski and Harabasz [30]
- 30 2. Hartigan [31]
- 31 3. Scott and Symons [32]
- 32 4. Marriot [33]
- 33 5. TraceW [34, 35]
- 34 6. TraceW<sup>-1</sup>B [35]

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37 For each index, the number of clusters to be considered was chosen according to the rule reported in Table 1  
38 where  $i_n$  is the validity index value obtained for  $n$  clusters [36].  
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42 [Table 1 about here.]  
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## 48 2.3. Derivation of classes

49 Concordance among solutions was evaluated using the Cohen’s kappa coefficient  $\kappa$  [37]. This coefficient is  
50 a statistical measure of inter-rater agreement for qualitative (categorical) items. It is generally thought to be  
51 a more robust measure than simple percent agreement calculation since  $\kappa$  takes into account the agreement  
52 occurring by chance.  
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3 To enable cluster visualisation, the original data space (consisting of a large number of dimensions) was  
4 transformed by principal component analysis (PCA) [38], and then the points plotted at their projected  
5 position on axes of the first and second principal components. As PCA transforms data such that the first  
6 principal component (PC) carries the maximum amount of variance in the data and the second PC carries  
7 the next largest variance (etc.), such a plot provides a picture in which the clusters have been ‘spread out’  
8 as much as possible.  
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12 The previously obtained clustering results from Abd El-Rehim and colleagues [12], the cluster validity  
13 indices (where appropriate), visualisation of the new clustering results themselves, and the concordance  
14 among clustering solutions were then all used heuristically to guide the formulation of a set of rules to define  
15 core class membership from the various cluster assignments.  
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## 19 20 *2.4. Characterisation of classes*

### 21 22 *2.4.1. Class characterisation by visualisation*

23 For inspection of the patient characteristics in each class, the distribution of each variable in the class was  
24 compared with its distribution in the total sample, using boxplots. A boxplot shows the median expression  
25 level (solid horizontal bar), the upper quartile and lower quartile range (shaded grey bar), the highest non-  
26 outlier and lowest non-outlier (smaller ticks joined by dashed lines), and any outliers (open circles). For a  
27 full description of boxplots, including the statistical definition of outliers see, for example, [39].  
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### 32 33 *2.4.2. Class characterisation by OSRE (orthogonal search rule extraction)*

34 Orthogonal Search Rule Extraction (OSRE) [40] is a computationally efficient algorithm to search for  
35 hypercubes in data space, since they map directly onto Boolean rules. A general description of this method  
36 is given below, while a more detailed one can be found in [40]. This methodology initially returns a rule for  
37 each data point, which triggers a pruning process to keep only those rules which represent large proportions  
38 of the data in the clusters, and do so with minimal mixing between clusters. The result is a set of low-order  
39 rules containing the covariates that characterize the sub-group of the cluster. The proposed interpretation  
40 is that these rules identify the drivers for cluster allocation, which may vary across the cluster but are, in  
41 general, well-defined.  
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47 Note that this method contrasts with widely used rule induction methods in two ways: firstly, there are  
48 no univariate cut-offs for groups of data, as in OSRE a sequential univariate search is carried out at the level  
49 of each individual data point which returns a multivariate hyperbox around that point, without the need  
50 to partition the data along a sequence of univariate covariates; and secondly, that the rules are overlapping,  
51 rather than constrained to mutual exclusivity as is usually the case in rule tree induction.  
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3 *2.4.3. Class characterisation by ANN (Artificial Neural Networks)*  
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5 A conventional multi-layer perceptron artificial neural network (MLP-ANN) model was utilised such that  
6 individual H-scores derived from the tissue microarray analysis of the clinical samples were set as inputs and  
7 the class was set as the output using Boolean notation (i.e. 1 represented membership of a given class, 0  
8 represented non-membership). This allowed the identification of markers that drive membership of a given  
9 class and that discriminate the class from the others. A three-layer MLP-ANN (featuring eight nodes in the  
10 hidden layer) with a back-propagation algorithm and a sigmoid activation function was used. The approach  
11 used in this work is similar to the ones used in [41] and [42].  
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17 *2.5. Patients and clinical methods*  
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19 A series of 1076 patients from the Nottingham Tenovus Primary Breast Carcinoma Series presenting  
20 with primary operable (stages I, II and III) invasive breast cancer between 1986-98 was used to evaluate  
21 the methodology. Immunohistochemical reactivity for twenty-five proteins, with known relevance in breast  
22 cancer including those used in routine clinical practice, were previously determined using standard immuno-  
23 cytochemical techniques on tumour samples prepared as tissue microarrays [12]. Levels of immunohisto-  
24 chemical reactivity were determined by microscopical analysis using the modified H-score (values between  
25 0-300), giving a semiquantitative assessment of both the intensity of staining and the percentage of positive  
26 cells. For the intensity, a score of 0 to 3, corresponding to negative, weak, moderate and strong positivity,  
27 was recorded. In addition, the percentage of positive cells at each intensity category was estimated. The  
28 H-score is calculated as follows [43]:  
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$$\begin{aligned} \text{H-score} = & (1 \times \% \text{ of cells stained at intensisty category 1}) \\ & + (2 \times \% \text{ of cells stained at intensisty category 2}) \\ & + (3 \times \% \text{ of cells stained at intensisty category 3}). \end{aligned}$$

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41 The range of possible scores is thus 0 to 300, where 300 equals 100% of tumour cells stained strongly [44].  
42 The complete list of variables used in this study is given in Table 2, while data extracted from three patients  
43 is reported as an example in Table 3.  
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47 [Table 2 about here.]  
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49 [Table 3 about here.]  
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52 This is a well-characterised series [12] of patients who were treated according to standard clinical proto-  
53 cols. Patient management was based on tumour characteristics using Nottingham Prognostic Index (NPI)  
54 and hormone receptor status. Patients with an NPI score  $\leq 3.4$  received no adjuvant therapy, those with a  
55 NPI score  $> 3.4$  received hormone therapy if oestrogen receptor (ER) positive or classical cyclophosphamide,  
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3 methotrexate and 5-fluorouracil (CMF) if ER negative and fit enough to tolerate chemotherapy. Hormonal  
4 therapy was given to 420 patients (39%) and chemotherapy to 264 (24.5%). This study was approved by the  
5 *Nottingham Research Ethics Committee 2* under the title ‘Development of a molecular genetic classification  
6 of breast cancer’.  
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### 10 11 **3. Results**

#### 12 13 *3.1. Clustering results*

##### 14 15 *3.1.1. HCA, K-means, PAM and ART*

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17 The HCA results from Abd El-Rehim et al. [12] were utilised, unaltered. Both the K-means and PAM  
18 algorithms were run with the number of clusters varying from two to twenty, as the number of clusters  
19 is an explicit input parameter of the algorithms. Given that both algorithms can be sensitive to cluster  
20 initialisation and in order to obtain reproducible results, both techniques were initialised with the cluster  
21 assignments obtained by hierarchical clustering. For the ART algorithm, the parameters were set in order to  
22 obtain six clusters in order to match the number of clusters previously obtained by HCA. The best validity  
23 index obtained for repeated runs of the algorithm with 20 random initialisations was used to select the final  
24 clustering assignment.  
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##### 30 31 *3.1.2. Fuzzy c-means*

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33 The fuzzy c-means algorithm did not perform as hoped. When the number of clusters was set as two and  
34 three, it appeared that reasonable results were obtained. However, from examination of the membership  
35 function of each point assigned to these clusters, it could be seen that it was very close to either  $1/2$  or  $1/3$ ,  
36 respectively. In other words, every data point was assigned to all the clusters with the same membership.  
37 Moreover, when the number of clusters was above three, non-zero memberships were evident for only three  
38 clusters and these memberships were similar to the three cluster solution — i.e. for  $n > 3$ , the  $n = 3$  cluster  
39 solution was obtained, but with  $n - 3$  empty clusters. These results indicated that the fuzzy c-means was  
40 not able to obtain clear cluster partitions.  
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45 The fuzziness index  $m$  was altered in an attempt to improve the results obtained, but it was found that  
46 little difference in the results was observed until  $m$  was close to one. Given that when  $m = 1$  fuzzy c-means  
47 is equivalent to K-means, this result was not useful. As there are many applications for which the fuzzy  
48 c-means technique has been successful (see, for example, [45]), these results are not easy to explain, but  
49 they may have been caused by the fact that our data contains a lot of values close to the extremes of each  
50 variable. Although the fuzzy c-means algorithm is widely used in literature, we decided to drop it from  
51 further analysis due to its poor performance on our data.  
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3 *3.2. Cluster validity*  
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5 The values of the decision rule obtained for various values of the validity indices for both K-means and  
6 PAM, for 2 to 20 clusters are shown in Fig. 1; (a) shows the validity decision rule values obtained for  
7 K-means and (b) shows those obtained for PAM. The best number of clusters according to each validity  
8 index, for each clustering algorithm, corresponds to the either the maximum or minimum decision rule value  
9 (depending on the index), as indicated by the solid circle in Fig. 1.  
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13 [Figure 1 about here.]  
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16 It can be seen that, while there was not absolute agreement among the indices as to which was the best  
17 number of clusters for the K-means method, there is good agreement that the best number of clusters for the  
18 PAM method is four. Although the best number of clusters varies according to validity index for K-means,  
19 on further inspection, it can be seen from Fig. 1 that there is more agreement than might be immediately  
20 apparent. For example, the Scott and Symons index (which indicated that the best number of clusters was  
21 three) indicated that the second best number of clusters was six. Consequently, the indices were used to  
22 rank order the number of clusters and the minimum sum of ranks was examined. It was found that the  
23 minimum sum of ranks (a form of consensus among the indices) indicated that the overall best number of  
24 clusters was six for K-means and four for PAM. Furthermore, careful examination of Fig. 1(b) confirms that  
25 the six cluster solution for PAM is of relatively poor quality.  
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33 *3.3. Derivation of classes*  
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35 The correspondence of patients assigned in the six cluster solution for each of the methods was then  
36 examined. Cohen's kappa and weighted-kappa indices were computed to measure the degree of agreement  
37 among algorithms. For the weighted-kappa index, weights were set in decreasing order from one (perfect  
38 agreement) to zero (complete disagreement) with a 0.2 step between levels. Results are reported in Table 4.  
39 From this table, a better agreement between K-means and hierarchical algorithms is evident compared  
40 to that between ART and hierarchical. It is also evident that the PAM six cluster solution has lower  
41 concordance with the original HCA results than either K-means or ART, and that the concordance of PAM  
42 with K-means and ART is also correspondingly lower.  
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48 [Table 4 about here.]  
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51 The cluster numbers were aligned with those obtained previously by Abd El-Rehim et al. in [12] in order  
52 to minimise differences and to aid visualisation. Biplots of the aligned clusters are shown in Fig. 2 for the  
53 six cluster solution from each algorithm. From these plots, it can be seen that the most similar results were  
54 obtained from the Hierarchical, K-means and ART. In fact, all these three methods obtain two clusters (1  
55 & 2) split over the left-hand side of the biplots. A third cluster (cluster 6) is evident towards the bottom  
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3 of the biplot. Then various splits of remaining data into three clusters (3, 4 & 5) can be seen. The PAM  
4 algorithm, instead, obtains three clusters (1, 2 & 4) split over the left-hand side, one group is visible towards  
5 the bottom (cluster 6) and one is spread in the center of the biplot (cluster 3). PAM places all patients on  
6 the right-hand side into a single cluster (cluster 5).  
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10 [Figure 2 about here.]  
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12 The biplots further confirm that the six cluster solution obtained from the PAM algorithm was the most  
13 dissimilar among the considered techniques. Taking into account the results of validity indices analysis, the  
14 concordance analysis and the visual analysis, we decided to remove the six clusters determined by PAM  
15 from further analysis.  
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18 The cluster distributions (number of patients in each cluster) obtained for the original hierarchical  
19 clustering and those obtained for the K-means and ART methods are shown in Table 5.  
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21

22 [Table 5 about here.]  
23

24 Focusing on these cluster correspondences, we wanted to define core classes containing the biggest possible  
25 number of patients. In a first attempt, considering agreement among the three clustering techniques (HCA,  
26 KM and ART) and looking at those patients assigned to the same group by different methods, a total of 382  
27 patients were classified if hierarchical group 4 was considered and 463 if not. After that, for each labelled  
28 group, concordances between all pairs of methods were analysed. It was found that the sum of the number  
29 of patients assigned to the same group ranged between 459 (pairing HCA and ART) and 645 (pairing KM  
30 and ART). These results are again reflected in Table 4. Two principles were used to guide the definition of  
31 consensus classes: (i) to consider all the clustering techniques analysed and (ii) to get the highest number  
32 of patients assigned to any class. These principles conflict, in that strict application of the first principle  
33 leads to a decrease in the number of patients assigned to classes. Hence, a heuristic trade-off between the  
34 two was employed. As a result, hierarchical group 4 was omitted (being replaced by group 5), and the ART  
35 assignments were not considered in a strictly conjunctive manner. Consequently, a set of six core breast  
36 tumour classes was derived following the specific rules reported in Table 6, in which the resultant number  
37 of patients in each class is shown.  
38  
39

40 It was found that almost the 62% of data was assigned to these core classes; the remaining patients  
41 were placed into a ‘not classified’ (NC) group. It must be stressed that the derivation of class assignments  
42 was made on the basis of the clustering results alone (which are, obviously, based on the 25 markers only)  
43 — class assignments, although somewhat subjective, were made *blind* to all clinical and outcome data. It  
44 should be also noted that around a third (actually 38%) of all patients were not assigned to any of the core  
45 classes.  
46  
47

48 [Table 6 about here.]  
49  
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### 3.4. Characterisation of classes

Biplots of the six consensus classes were produced and are shown in Fig. 3, in order to provide a visualisation of the separation of the classes.

[Figure 3 about here.]

Fig. 3(a) shows the biplot obtained for all patients, in which the cases not assigned to any class (NC) have been coloured grey. It can be seen that these fall mainly into the centre region of the biplot. Fig. 3(b) shows the biplot obtained for only patients assigned to classes 1 – 6. It can be seen that the classes appear more spread out. The first axis was mainly determined, on the left, by luminal markers including luminal cytokeratins (CK18, CK7/8, CK19), hormone receptors (ER, AR, PgR), and MUC1 over-expression and, on the right, by basal cytokeratins (CK14 and CK5/6) and partly by p53 over-expression. The second axis is determined, on the top, partly by nuclear BRCA1 (nBRCA1) over-expression and, on the bottom, by HER2 and E-cad over-expression (also HER3 and HER4, although these are not shown as they overlap HER2).

Fig. 4 shows boxplots of all 25 markers, (a) for all cases, (b) for those cases assigned to classes 1–6, and (c-h) for each class separately. By inspection of both the biplots and the boxplots, we derived a description of each class. For example, classes 1 and 2 are characterised by strong expression of the luminal CK markers, as well as moderate to strong MUC1 expression (as per the population). However, there is a distinct difference regarding HER3 and HER4 expression. It can also be seen that classes 4 and 5 both exhibit higher expressions of the basal CKs (CK5/6 and CK14). Triple negative patients with high p53 levels are grouped in class 4, whereas class 5 consist of triple negative patients with low p53 levels. A summary of the class characteristics obtained by visual inspection of the boxplots is given in Table 7.

The results obtained from the automated characterisation methods (MLP-ANN and OSRE) are reported in Table 8.

[Figure 4 about here.]

[Table 7 about here.]

[Table 8 about here.]

A proposed summary of the essential characterisations of the classes obtained is given in Fig. 5, according to the available bio-pathological knowledge. It is worth noting that class 2, labelled as Luminal-N, and the split of the basal group into two different subgroups depending on p53 levels, appear to be novel findings not previously emphasised in literature.

[Figure 5 about here.]

## 4. Clinical Evaluation

### 4.1. Patient clinical outcome

Patient age ranged from 18 to 72 years (median 54 years). Of the available cases, 708 (66%) cases were aged 50 years or more. At the time of diagnosis, 160 (14.9%) tumours were histological grade 1, 343 (31.9%) grade 2 and 572 (53.2%) grade 3. A total of 654 (60.8%) patients had lymph node-negative disease and 419 (38.9%) had positive lymph nodes (332 cases with between one and three positive nodes, 87 cases with four or more positive). Frequencies for histological tumour types were: 649 invasive ductal carcinomas of no special type (NST), 171 tubular mixed carcinomas, 30 medullary carcinomas, 112 lobular carcinomas, 27 tubular carcinomas, 11 mucinous carcinomas, five cribriform carcinomas, three papillary carcinomas, 37 mixed NST and lobular carcinomas, 24 mixed NST and special type carcinomas and four miscellaneous tumours. A total of 736 (68.4%) had tumour size more than 1.5 cm and distant metastases was observed in 111 cases.

### 4.2. Clinical characterisation of patients by class

Significant associations, as expected, were found between the classes with respect to patient age, tumour grade, size, lymph node stage and histological tumour type (see Table 9).

[Table 9 about here.]

A boxplot of the Nottingham Prognostic Index (NPI) split by class is shown in Fig. 6. It can be seen that the NPI for classes 1 and 2 is lower than that of classes 3–6 (overall Kruskal-Wallis  $p \ll 0.001$ ). It can also be seen that classes 1 and 2 have similar NPI, and classes 3–6 have similar NPI (to each other). This is an interesting observation for two reasons. Firstly, it confirms that the NPI is providing discriminant information between classes 1 and 2, and classes 3–6. Secondly, it suggests that the class divisions are providing *additional* information to the NPI.

[Figure 6 about here.]

## 5. Discussion

This study has extended our previous work [12], with the application of different clustering techniques to address the issue of the non-existence of the ‘perfect’ clustering algorithm. In particular, in this work four different clustering methods (in addition to the hierarchical method used in [12]) were applied to a multidimensional dataset of protein biomarker data, in order to evaluate the stability of results coming from different techniques. Different clustering algorithms result in different clusters, particularly when large multi-dimensional data sets are considered.

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3 To explore the extent of the differences among different algorithms, an informal consensus clustering was  
4 used, grouping together patients that were assigned to ‘similar’ clusters by different clustering algorithms.  
5 The consensus approach was similar to the one used by Kellam et al. [23], but instead of building an  
6 agreement matrix, the previously published hierarchical clustering solution (and associated labelling) was  
7 used as a fixed reference. In this way, a set of six core classes of breast cancer was elucidated. This  
8 consensus methodology was used to combine results obtained by different clustering algorithms rather than  
9 as a comparison with previously published approaches. Another important issue that emerges when cluster  
10 analysis is performed, is the best number of clusters to consider. Several validity indices have been proposed  
11 in recent years (see, for example, [36]) to evaluate the compactness of clusters and the separation among  
12 them. For the algorithms which take an explicit number of clusters as an input parameter (i.e. K-means  
13 and PAM), cluster validity indices were used to guide the choice of the ‘best’ number of clusters. Note that  
14 cluster validity indices would have been applied to the fuzzy c-means algorithm had it not been dropped  
15 from analysis for the reasons outlined in Section 3.1.2.

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18 Furthermore, this study confirmed, as already highlighted in [13], that cluster analysis should be treated  
19 with caution, as different clustering algorithms will lead to different groupings of tumours. In particular, in  
20 our case, the PAM algorithm, when run with six clusters as an input, provided groups that were different  
21 from those obtained using the other techniques. In addition, the hierarchical algorithm, commonly used in  
22 standard bioinformatics applications of cluster analysis, such as [4] or [9], seems to provide a dissimilar and  
23 skewed classification with respect to the others, thus reducing the degree of overall concordance and the  
24 number of subjects assigned to the core classes.

25  
26  
27 In conclusion, we have clearly demonstrated that different clustering algorithms can produce quite differ-  
28 ent solutions on such multi-dimensional data. It should be noted that no feature extraction was performed  
29 in this study, so avoiding a possible cause of diverse techniques not converging into similar results. We  
30 have proposed a methodology for reaching consensus from the various results that may be obtained from  
31 clustering algorithms, and have illustrated this consensus methodology on a well-known set of breast cancer  
32 data. In doing so, we have identified possible new sub-classes of breast cancer which warrant further inves-  
33 tigation. We emphasise that this consensus methodology, by its heuristic nature, should be considered as  
34 an exploratory technique, and must not be considered as providing any form of definitive answer. Further  
35 work exploring, for example, the statistical properties of the considered algorithms may provide relevant  
36 information on the structure on this complex biological problem.

## 37 38 39 **Acknowledgement**

40  
41  
42 This study was, in part, funded by the Breast Cancer Campaign, and was supported by the BIOPAT-  
43 TERN FP6 Network of Excellence (FP6-IST-508803) and the BIOPTRAIN FP6 Marie-Curie EST Fellowship  
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## Summary

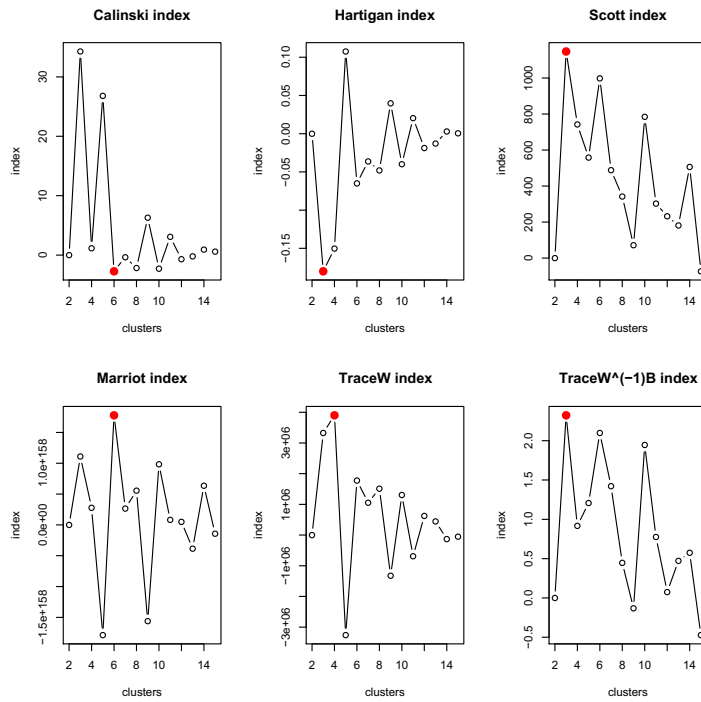
In a previous study [12], we have suggested that immunohistochemical analysis may be used to identify distinct biological classes of breast cancer. The objectives of this work were to verify the stability of groups obtained from four different unsupervised clustering algorithms, applied to the same data, and to compare and combine the different solutions with the ones available from the previous study. The clustering techniques were used to divide our dataset in six groups, which were labelled according to our previous classification [12]. Moreover, where appropriate, validity indices were used to explore the best data subdivision and to validate the obtained classification. Despite the fact that fuzzy c-means is one of the most widely used clustering techniques, results obtained from the algorithm were quite poor and were dropped from further investigation. The PAM algorithm produce somewhat different results to the other techniques, so that correspondences between classifications were also difficult. Then, only considering Hierarchical, K-means and ART methods, a set of six core classes was elucidated by a form of consensus clustering in which labels assigned to the groups were aligned to find correspondences among patients grouped in similar clusters by different techniques. It was found that around the 62% (663 patients) of the available data was assigned to classes, while the remaining 413 women (38%) presented mixed class characteristics. The use of different clustering methods has, once again, demonstrated that diverse algorithms will in general produce different clusters, particularly when large multi-dimensional data sets are considered.

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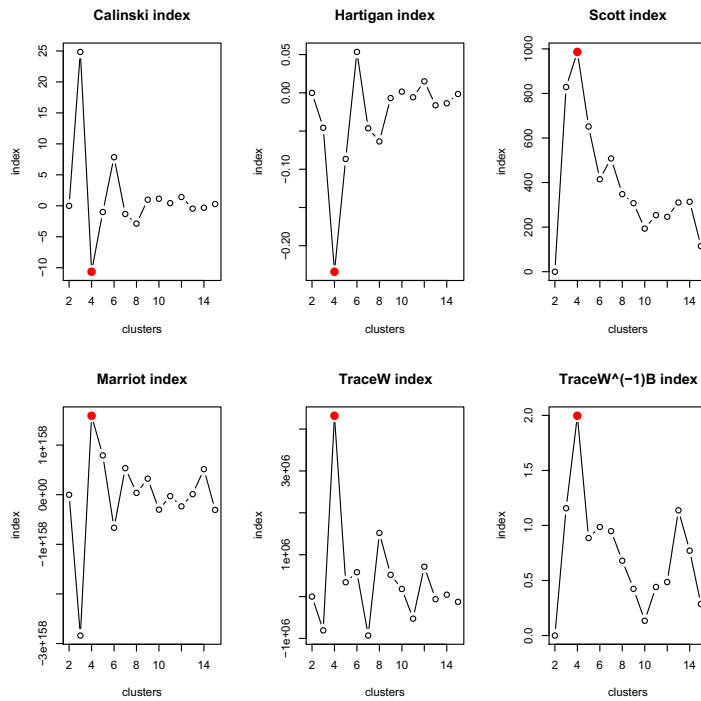
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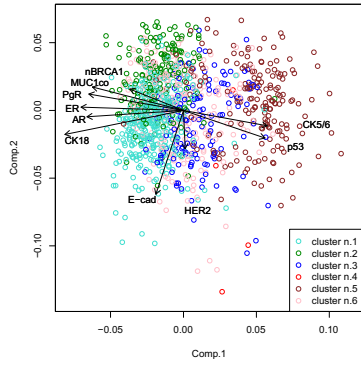


(a) K-means indices behaviors

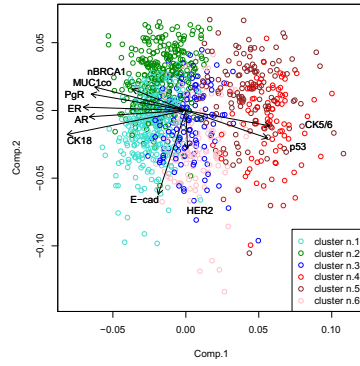


(b) PAM indices behaviors

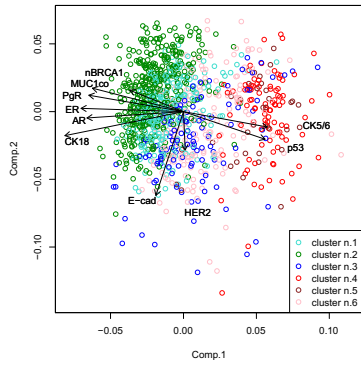
Figure 1: Cluster validity indices obtained for K-means and PAM clustering, for varying cluster numbers from 2 to 20.



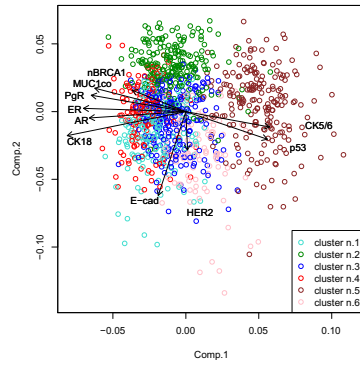
(a) Hierarchical clustering



(b) K-means clustering

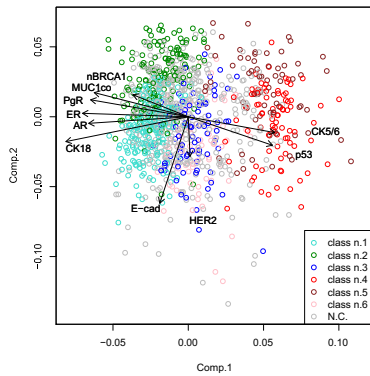


(c) ART clustering

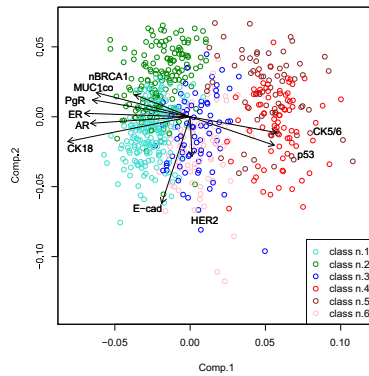


(d) PAM clustering

Figure 2: Biplots of clusters projected on the first and second principal component axes.



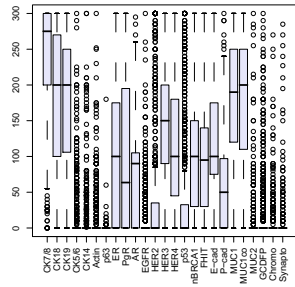
(a) For all patients



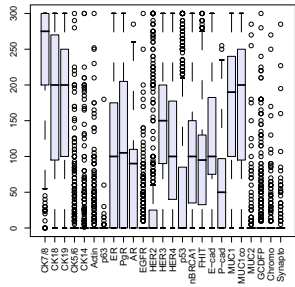
(b) For only patients in classes 1-6

Figure 3: Biplots of classes projected on the first and second principal component axes

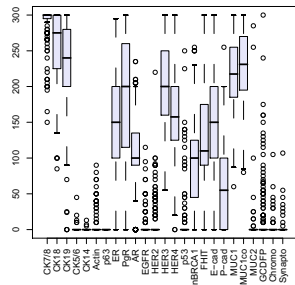
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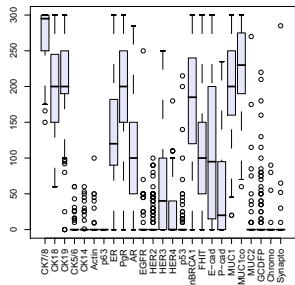
(a) For all patients



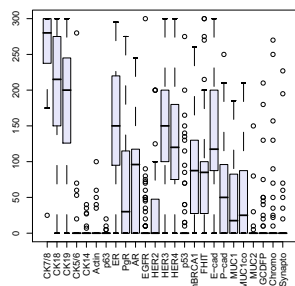
(b) For patients in classes 1-6



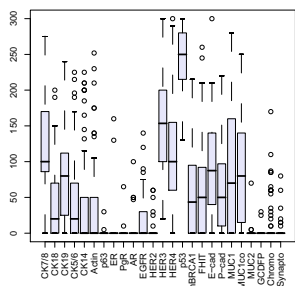
(c) Class 1



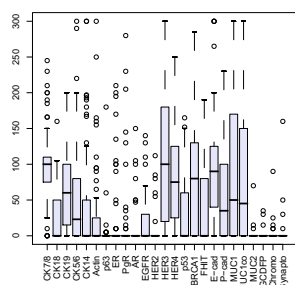
(d) Class 2



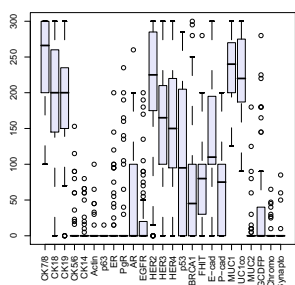
(e) Class 3



(f) Class 4



(g) Class 5



(h) Class 6

Figure 4: Boxplot for all markers, whole data and grouped by class

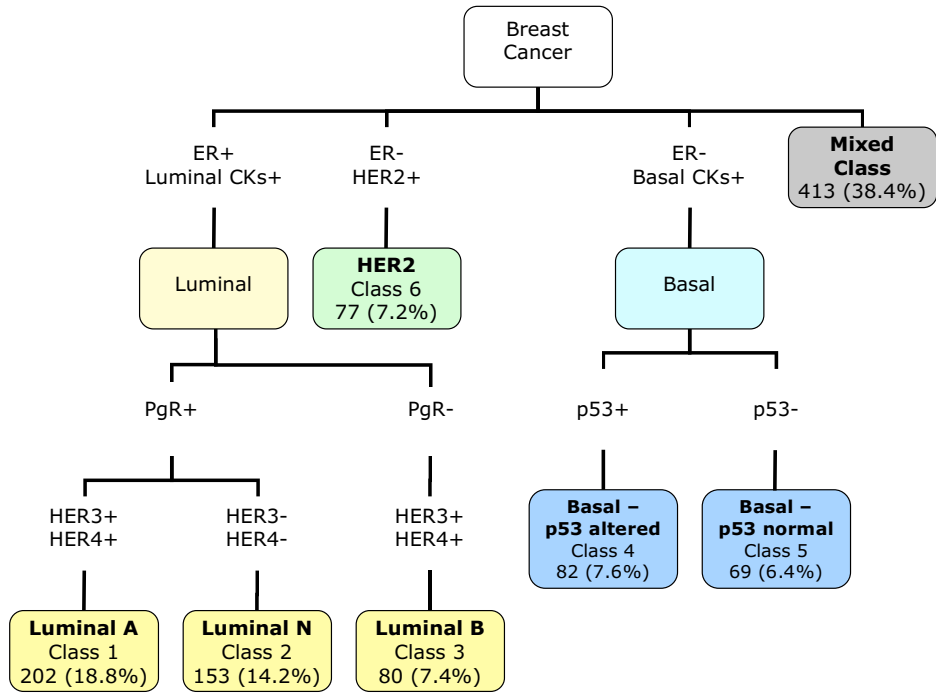


Figure 5: A summary of the classes of breast cancer obtained, with indicative class interpretations.

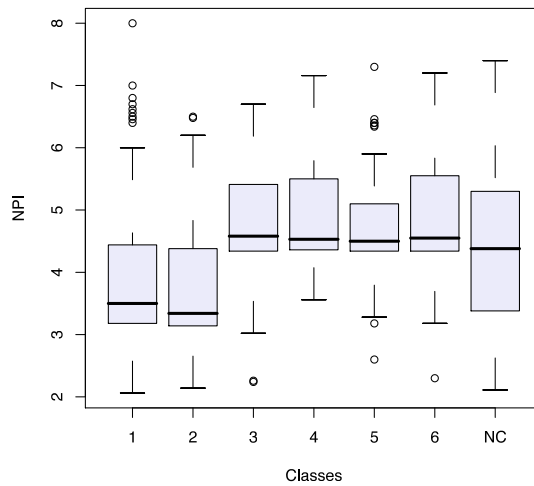


Figure 6: Boxplots of Nottingham Prognostic Index (NPI) by class.

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Table 1: Different validity indices and their associated decision rules

Index	Decision rule
Calinski and Harabasz	$\min_n((i_{n+1} - i_n) - (i_n - i_{n-1}))$
Hartigan	$\min_n((i_{n+1} - i_n) - (i_n - i_{n-1}))$
Scott and Symons	$\max_n(i_n - i_{n-1})$
Marriot	$\max_n((i_{n+1} - i_n) - (i_n - i_{n-1}))$
TraceW	$\max_n((i_{n+1} - i_n) - (i_n - i_{n-1}))$
TraceW <sup>-1</sup> B	$\max_n(i_n - i_{n-1})$

Table 2: Complete list of antibodies used and their dilutions

Antibody, clone	Short Name	Dilution
Luminal phenotype		
CK 7/8 [clone CAM 5.2]	CK7/8	1:2
CK 18 [clone DC10]	CK18	1:50
CK 19 [clone BCK 108]	CK19	1:100
Basal Phenotype		
CK 5/6 [cloneD5/16134]	CK5/6	1:100
CK 14 [clone LL002]	CK14	1:100
SMA [clone 1A4]	Actin	1:2000
p63 ab-1 [clone 4A4]	p63	1:200
Hormone receptors		
ER [clone 1D5]	ER	1:80
PgR [clone PgR 636]	PgR	1:100
AR [clone F39.4.1]	AR	1:30
EGFR family members		
EGFR [clone EGFR.113]	EGFR	1:10
HER2/c-erbB-2	HER2	1:250
HER3/c-erbB-3 [clone RTJ1]	HER3	1:20
HER4/c-erbB-4 [clone HFR1]	HER4	6:4
Tumour suppressor genes		
p53 [clone DO7]	p53	1:50
nBRCA1 Ab-1 [clone MS110]	nBRCA1	1:150
Anti-FHIT [clone ZR44]	FHIT	1:600
Cell adhesion molecules		
Anti E-cad [clone HECD-1]	E-cad	1:10/20
Anti P-cad [clone 56]	P-cad	1:200
Mucins		
NCL-Muc-1 [clone Ma695]	MUC1	1:300
NCL-Muc-1 core [clone Ma552]	MUC1co	1:250
NCL muc2 [clone Ccp58]	MUC2	1:250
Apocrine differentiation		
Anti-GCDFP-15	GCDFP	1:30
Neuroendocrine differentiation		
Chromogranin A [clone DAK-A3]	Chromo	1:100
Synaptophysin [clone SY38]	Synapto	1:30

Table 3: H-score of each variable for three different patients

Variable name	Patient 1	Patient 300	Patient 1061
CK7/8	200	280	100
CK18	300	190	0
CK19	200	145	0
CK5/6	0	0	125
CK14	0	0	210
Actin	0	0	0
p63	0	0	0
ER	60	110	0
PgR	0	0	0
AR	0	45	0
EGFR	0	0	0
HER2	300	0	0
HER3	170	72	250
HER4	100	130	150
p53	150	0	270
nBRCA1	200	45	0
FHIT	120	0	0
E-cad	100	115	0
P-cad	0	15	0
MUC1	180	255	160
MUC1co	210	210	80
MUC2	0	0	0
GCDFP	90	0	0
Chromo	0	0	0
Synapto	0	0	0

Table 4: Kappa and *weighted kappa* index among different classifications

	K-means	ART	PAM
HCA	0.497	0.296	0.325
	<i>0.548</i>	<i>0.401</i>	<i>0.332</i>
K-means	—	0.494	0.420
	—	<i>0.599</i>	<i>0.525</i>
ART	—	—	0.224
	—	—	<i>0.376</i>

Table 5: Number of cases in each cluster

Cluster	HCA	K-means	ART
1	336	301	238
2	180	282	408
3	139	138	111
4	4	97	96
5	183	124	35
6	234	134	188

Table 6: Rules for determining consensus classes

If cluster . . .	Class	No. of cases
H1 & KM1 & (ART1   ART2)	1	202
H2 & KM2 & (ART1   ART2)	2	153
H3 & KM3	3	80
H5 & KM4 & ART4	4	82
H5 & KM5	5	69
H6 & KM6 & ART6	6	77
Total number of cases assigned to classes 1–6		663
Total number of cases not classified		413

Table 7: Description of classes as determined by statistical characterisation.

Class	Over-expressed	Under-expressed	Other
1	ER, AR, PgR, HER3, HER4		
2	ER, AR, PgR, nBRCA1	HER3, HER4	
3	ER, AR	MUC1, MUC1co	PgR normal
4	p53	ER, PgR, HER2, MUC1, MUC1co, CK18, CK7/8, CK19	
5		ER, PgR, HER2, MUC1, MUC1co, CK18, CK7/8, CK19	p53 absent
6	HER2, HER3, HER4		ER, AR, PgR absent; p53 widely spread

Table 8: A summary of rules obtained from the automated methods for defining class memberships

Class	Over-expressed	Under-expressed
1 (ANN)	PgR, HER3, HER4, MUC1co	
1 (OSRE)	PgR, HER3, HER4, CK18, CK19, MUC1co	HER2
2 (ANN)	PgR, nBRCA1	HER3, HER4
2 (OSRE)	PgR, nBRCA1, MUC1co	HER3, HER4
3 (ANN)	ER	MUC1
3 (OSRE)	CK7/8, CK18	
4 (ANN)	p53	
4 (OSRE)	HER3, p53	ER, HER2
5 (ANN)	CK5/6	CK7/8
5 (OSRE)		p53; CK7/8, CK19 or HER2, HER4
6 (ANN)	HER2	
6 (OSRE)	HER2, p53, MUC1co	ER

Table 9: Breast Cancer Class distribution in relation to clinicopathological parameters (NST: No Special Type).

	Breast Cancer Class						$\phi$
	1	2	3	4	5	6	
<b>Age</b>							
≤ 50	76 (37.6)	63 (41.2)	24 (30.0)	55 (67.1)	33 (47.8)	37 (48.1)	0.209
> 50	126 (62.4)	90 (58.8)	56 (70.0)	27 (32.9)	36 (52.2)	40 (51.9)	
Total	202	153	80	82	69	77	
<b>Grade</b>							
1	58 (28.9)	43 (28.1)	2 (2.5)	0 (0)	2 (2.9)	1 (1.3)	0.660
2	81 (40.2)	89 (58.2)	18 (22.5)	1 (1.2)	7 (10.1)	12 (15.6)	
3	62 (30.8)	21 (13.7)	60 (75.0)	81 (98.8)	60 (87.0)	64 (83.1)	
Total	201	153	80	82	69	77	
<b>Size</b>							
≤ 1.5cm	79 (39.1)	65 (42.5)	20 (25.0)	12 (14.6)	15 (21.7)	16 (20.8)	0.225
> 1.5cm	123 (60.9)	88 (57.5)	60 (75.0)	70 (85.4)	54 (78.3)	61 (79.2)	
Total	202	153	80	82	69	77	
<b>Lymph Node Stage</b>							
1	132 (65.3)	108 (70.6)	39 (48.7)	50 (61.0)	52 (75.4)	36 (46.8)	0.217
2	58 (28.7)	37 (24.2)	35 (43.8)	23 (28.0)	10 (14.5)	30 (39.0)	
3	12 (5.9)	7 (4.6)	6 (7.5)	9 (11.0)	7 (10.1)	10 (13.0)	
Total	202	152	80	82	69	76	
<b>Tumour type</b>							
Invasive ductal/NST	97 (48.0)	45 (29.4)	64 (80.0)	70 (85.4)	53 (76.8)	68 (88.3)	0.622
Tubular mixed	52 (25.7)	50 (32.6)	8 (10.0)	0 (0)	1 (1.5)	5 (6.5)	
Medullary	0 (0)	0 (0)	0 (0)	10 (12.2)	5 (7.2)	2 (2.6)	
Lobular	18 (8.9)	34 (22.2)	6 (7.5)	0 (0)	4 (5.8)	1 (1.3)	
Special types	19 (9.4)	11 (7.2)	0 (0)	1 (1.2)	0 (0)	0 (0)	
Mixed NST & lobular	6 (3.0)	7 (4.6)	2 (2.5)	1 (1.2)	3 (4.3)	0 (0)	
Mixed NST & special type	9 (4.5)	5 (3.3)	0 (0)	0 (0)	1 (1.5)	0 (0)	
Miscellaneous	0 (0)	1 (0.7)	0 (0)	0 (0)	2 (2.9)	0 (0)	
Total	201	153	80	82	69	76	

## Conflict of Interest Statement

None Declared.