

Oscillation frequency measurement of gaseous diffusion flames using electrostatic sensing techniques

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Abstract

The oscillation frequency of a burner flame is closely related to the combustion conditions and flame stability. Oscillation frequency measurement is essential for optimized operation of the combustion process. In this paper, the novel use of electrostatic sensors in conjunction with power spectral analysis is presented for the oscillation frequency measurement of a gaseous laminar diffusion flame. Experimental tests carried out on a combustion rig demonstrate that the developed system realises oscillation frequency measurement with a relative deviation from the reference value from an imaging system within $\pm 6\%$ over a constant fuel flow rate from 0.60 L/min to 0.80 L/min. The oscillation frequency increases with the fuel flow rate and the oscillation frequencies in different regions of the diffusion flame are similar for each fuel flow rate. Under varying fuel flow rate conditions, the system can measure the instantaneous oscillation frequency with a relative deviation from the reference value from an imaging system mostly between -10% and 0%.

Key words: *Diffusion flame; oscillation frequency; electrostatic sensor; spectral analysis; combustion monitoring.*

27 **List of symbols:**

Δq	Transferred charge (C)	R_f	Feedback resistor (Ω)
K_c	Charging efficiency	I_s	Current from the electrode (A)
C	Capacitance of the equivalent capacitor (F)	S_i	Sensor signal (V)
V	Total potential difference between the two contacting surfaces (V)	S_{sum}	Sum of sensor signals (V)
ε_0	Absolute permittivity of air (F/m)	N	Total number of sensors
A	Contact area (m^2)	F_e	Measured oscillation frequency (Hz)
z_0	Critical gap including the geometrical factors between the contact bodies (m)	F_i	Reference oscillation frequency (Hz)
d	Distance from the electrode and the flame boundary (m)	\bar{F}_e	Mean of the oscillation frequency (Hz)
U	Signal amplitude (V)	δ	Normalized standard deviation
V_o	Voltage output of the amplifier (V)	σ	Standard deviation

28

29 **1. Introduction**

30 Oscillatory behaviour, also named as flicker or pulsation, of a burner flame originates
31 mainly from the Kelvin-Helmholtz type instability in the buoyancy-induced shear layer
32 surrounding the flame surface [1, 2]. The oscillation of a flame affects the rate of air entrainment
33 into the flame and the flame height, thus causing periodic changes in the flame structure, external
34 shape, luminous intensity, thermoacoustics, radiation, pressure field and energy efficiency [3].
35 The degree of flame oscillation in the aforementioned characteristics is represented by the
36 oscillation frequency, which is closely related to the combustion conditions and flame stability
37 [4]. Oscillation may exist even with steady supplies of fuel and oxidizer, and cause the flame
38 failure or flame extinction under extreme conditions [5]. An unstable flame may lead to many
39 problems such as low combustion efficiency, high atmospheric emissions, and vibration of the
40 furnace. Therefore, oscillation frequency measurement of a burner flame is essential for
41 optimized operation of the combustion process.

42 The oscillation frequency of a laminar diffusion flame is of interest to combustion engineers
43 as oscillations are widely encountered in small combustion systems and for the fundamental
44 understanding of turbulent flames. In order to realize the measurement of the oscillation
45 frequency of diffusion flames, various techniques have been developed to tackle this challenge
46 for a number of fuels. Cetegen and Ahmed [6] measured the oscillation frequency using multiple
47 differential pressure sensors, which detected the fluctuations in the pressure of the burner surface.
48 The radiation emitted by the flame was also measured to determine the oscillation frequency in
49 the literature. Jin *et al.* [7] used indium tin oxide thin-film thermocouples to measure the
50 temperature of the combustor in a scramjet and performed time-frequency analysis to extract the
51 combustion fluctuation features. Xu and Yan [8] adopted photovoltaic cells covering the visible
52 and infrared spectral bands to measure the oscillation frequency of flame-radiation signals.
53 Photodiodes were also employed to acquire the intensity fluctuation of the whole band of the
54 flame radiation and spectral analysis was performed to extract the flame oscillation frequency
55 [9-11]. Such detectors are simple in structure and offer online continuous measurement and can
56 detect the flame oscillation frequency over different specific wavelengths, but they have a
57 requirement for purging air to keep the photosensitive element clean. The beam deflection
58 technique has also been used to measure the flame oscillation frequency for the purpose of
59 combustion diagnosis. Gotoda *et al.* [12] used a photomultiplier to detect the light intensity
60 change as a consequence of laser beam deflection induced by flame motion and determined the
61 oscillation frequency via fast Fourier transform analysis. Albers and Agrawal [13] adopted
62 quantitative rainbow schlieren deflectometry to investigate the oscillation frequency of a gas-jet
63 diffusion flame. Ge *et al.* [14] employed a schlieren device to study periodical pulsation
64 combustion state of the methane/oxygen laminar co-flow diffusion flame.

65 There have been many studies of the digital imaging technique for the monitoring of the
66 flame oscillation frequency. Huang *et al.* [15] introduced an instrumentation system based on

67 digital imaging for on-line continuous measurement of the flame oscillation frequency. Lu *et al.*
68 [16] adopted a camera to capture flame images and processed the luminous intensity of
69 individual pixels in the images to investigate the oscillatory behaviour of pulverized coal flames.
70 Farias *et al.* [17] used a digital flame monitoring system to quantify the oscillatory behaviour of
71 bituminous coal and wood biomass flames. However, the optical probe that transmits the flame
72 images to the camera requires not only cooling but also purging air to prevent contamination of
73 the objective lens by fine dust. Li *et al.* [18] measured the flame oscillation frequency using an
74 ion current sensing method, which detected the ion generation rate in the flame. Nevertheless,
75 the size and position of the ion probe have to be considered to minimize its intrusive disturbance
76 to the flame, and the shape and stability of the flame are easily affected by the applied electric
77 field.

78 This paper reports the novel use of electrostatic sensors for measuring the oscillation
79 frequency of a gaseous laminar diffusion flame. Electrostatic phenomena are ubiquitous in a
80 range of industries. Electrostatic sensors have been applied to the monitoring of various
81 industrial processes, such as quantitative characterisation of flow in pneumatic conveyors [19]
82 and fluidized beds [20]. Electrostatic sensors have the advantages of robustness in a harsh
83 environment, passive sensing, structural simplicity and low maintenance requirements, thus
84 offering a good potential for the oscillation frequency measurement of a burner flame. The
85 presence of fine particles and dust in the combustion field, which adversely affects the operation
86 of optical monitors based on photodiodes and digital cameras, has little impact on electrostatic
87 sensors. In addition, passive electrostatic sensors have no requirement for the supply of an
88 electric field which is essential for ion probes and cause little intrusive disturbance to the flame.
89 A point to note on the developed electrostatic sensor is that it is not intended to replace other
90 sensors, such as digital cameras and photodiodes. Instead, electrostatic sensors can be used to
91 characterize electrical properties of a burner flame, which is desirable to obtain information

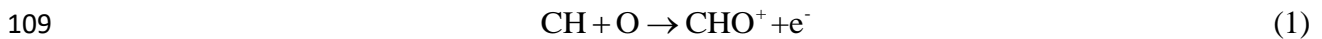
92 complementary to optical and other measurement techniques for combustion diagnosis and
93 achieve an in-depth understanding of the electrical properties of a burner flame.

94 Electrostatic sensors are, in principle, applicable to both laminar and turbulent flames
95 because all such flames have charged species in them. However, this paper focuses on the
96 measurements and their interpretations of oscillation frequencies of laminar diffusion flames
97 using the proposed electrostatic sensors, because such knowledge forms an important
98 foundation for further studies of more complex flames such as turbulent premixed flames, co-
99 firing flames, oxyfuel flames etc. The electrostatic sensor placed around the flame detects the
100 dynamic properties of the flame through electrostatic induction and charge transfer. The flame
101 oscillation frequency is determined through power spectral analysis of the sensor signal. The
102 fundamental sensing principle and sensor design are included, in addition to the implementation
103 and practical evaluation of the system under controlled laboratory conditions.

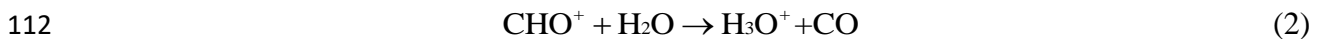
104 **2. Measurement principle and sensor design**

105 *2.1. Sensing principle*

106 Chemi-ionization reactions in a burner flame have sufficient exotherm to ionize the reaction
107 products, thereby generating ions and free electrons [21, 22]. The elementary reaction
108 responsible for ionization in the flame is [21]:



110 H_3O^+ is the dominant ionic species, which is produced by the following charge transfer reaction
111 [22]:



113 where CHO^+ is quickly consumed by H_2O . Reaction (2) is much speedier than reaction (1), i.e.
114 CHO^+ ions are destroyed faster than they are produced [23]. Some charged soot particles are
115 also produced in a flame by thermal ionization [24]. Since a burner flame contains charged
116 species such as free electrons, ions and soot, they are electrically conductive [21].

117 Fig. 1 shows the general principle of the electrostatic sensor for oscillation frequency
118 measurement. An exposed electrode is placed around the flame to detect the surface charges on
119 the electrode, and sense the flame movement through electrostatic induction and charge transfer.
120 When the free electrons, ions and charged particles around the flame are in contact with the
121 surface of the exposed electrode, charges will be transferred to the electrode. Meanwhile, with
122 the space charges moving within and around the flame, induced charges are produced on the
123 electrode surface. In previous studies [25], it was found that the unipolar signal from the
124 electrode is generated through transferred charge since the flame as an integral whole is
125 electrically neutral. The quantity of transferred charges on the electrode is dependent on various
126 factors, for example, the burner type, fuel type, types of charged species and the variation of the
127 flame shape. The change in the concentration of charged species is small for fixed test conditions.
128 However, the periodic formation, upward propagation and shedding of the toroidal vortices
129 surrounding the flame induced by buoyancy convection cause the flame oscillation and a
130 periodic change in the flame shape. The spatial charge density around the electrode varies with
131 the flame shape, i.e. the distance from the flame boundary to the electrode, which leads to the
132 variation in the amount of charge transferred on the electrode.

133 However, the process of charge transfer resulting from the contact between the charged
134 elements in the flame and the electrode is very complex. Some fundamental issues on the
135 mechanism of charge transfer remain to be resolved, such as the type of transferred charge
136 species and the prediction of direction and magnitude of charge transfer [26]. According to a
137 condenser model [27], the contact region between a particle and an electrode is taken as a
138 capacitor and the potential difference between the two contacting surfaces is the electromotive
139 force for charge transfer. In the condenser model the transferred charge Δq is represented by:

$$140 \quad \Delta q = K_c CV \quad (3)$$

141 where K_c is the charging efficiency, C is the capacitance of the equivalent capacitor, and V is the
142 total potential difference between the two contacting surfaces. The capacitance C can be
143 calculated from:

$$144 \quad C = \frac{\epsilon_0 A}{z_0} \quad (4)$$

145 where ϵ_0 is the absolute permittivity of air, A is the contact area and z_0 is the critical gap including
146 the geometrical factors between the contact bodies.

147 Although the quantity of the transferred charge is unpredictable, it depends on the distance
148 from the flame boundary to the sensor [25]. In response to the fluctuation in flame shape, the
149 exposed electrode generates a current signal. Since the original current signal from the electrode
150 is very weak, a signal conditioning module is required. The magnitude of the sensor signal
151 represents the amount of charges transferred to the electrode, also reflecting the distance from
152 the electrode to the flame boundary. Because of the complexity of the charge generation and
153 distribution, it is difficult to build the analytical relation between the signal amplitude and the
154 distance. However, the relationship between the signal amplitude and the distance can be
155 determined through a fitted equation [25] obtained through exponential regression analysis,
156 which is expressed as:

$$157 \quad d = p_1 \exp(-p_2 U) + p_3 \exp(-p_4 U) \quad (5)$$

158 where p_1 , p_2 , p_3 and p_4 are factors associated with the fuel attributes and the type of the burner,
159 U the average signal amplitude and d the distance. Therefore, the oscillatory behaviour of the
160 flame can be obtained by spectral analysis of the sensor signal. A point to note is that this paper
161 aims to measure the flame oscillation frequency, which is little dependent upon the signal
162 amplitude.

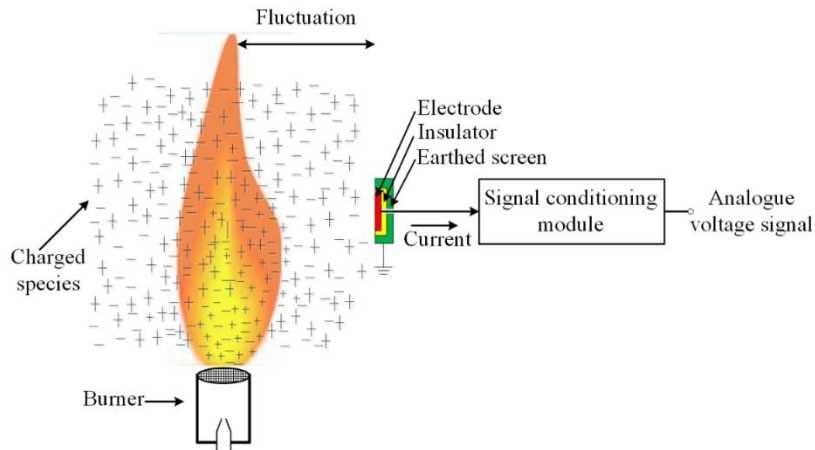


Fig. 1. General sensing principle of the electrostatic sensor.

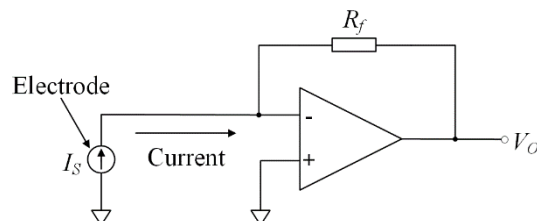
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165 2.2. Signal conditioning

166 The signal conditioning module includes three consecutive stages, which are constructed
167 with AD8604, a wideband rail-to-rail operational amplifier. The first stage of the signal
168 conditioning module is a trans-resistance amplifier, as shown in Fig. 2. The voltage output V_O
169 of the amplifier is given by:

$$170 \quad V_O = -I_s R_f \quad (6)$$

171 where R_f is the feedback resistor determining the transimpedance gain and I_s the weak current
172 from the electrode. The value of the feedback resistor is 10 M Ω . The second stage in the signal
173 conditioning module is a non-inverting amplifier with a voltage gain of 10. The main frequency
174 components of the sensor signal are no greater than 30 Hz [25, 28]. The third stage is a Sallen-
175 Key low-pass filter which cuts off unwanted noise greater than 48 Hz. Detailed information
176 about the sensors has been reported elsewhere [23].

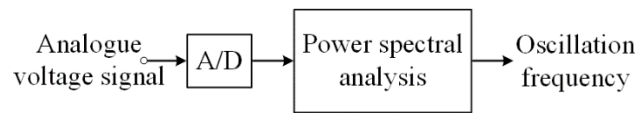


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Fig. 2. Trans-resistance amplifier.

179 Fig. 3 shows a block diagram of the signal acquisition and subsequent analysis in the
180 oscillation frequency measurement system. The signal acquisition is performed by a data

181 acquisition card and the sampling frequency is set to 250 Hz. Power spectral analysis of the
182 sensor signal is carried out to acquire its frequency components. The oscillation frequency
183 measurement of diffusion flames has been studied by many researchers through digital imaging
184 and image analysis [5, 15]. It was found that a diffusion flame contains a main frequency
185 component and the variation of the radiation intensity is primarily related to the fluctuation in
186 the flame shape. Therefore, in this paper, the dominant frequency corresponding to the
187 maximum peak in the power spectrum is regarded as the oscillation frequency of the diffusion
188 flame.



189

190 **Fig. 3.** Block diagram of the signal acquisition and subsequent analysis in the oscillation frequency
191 measurement system.

192 2.3. Sensor design

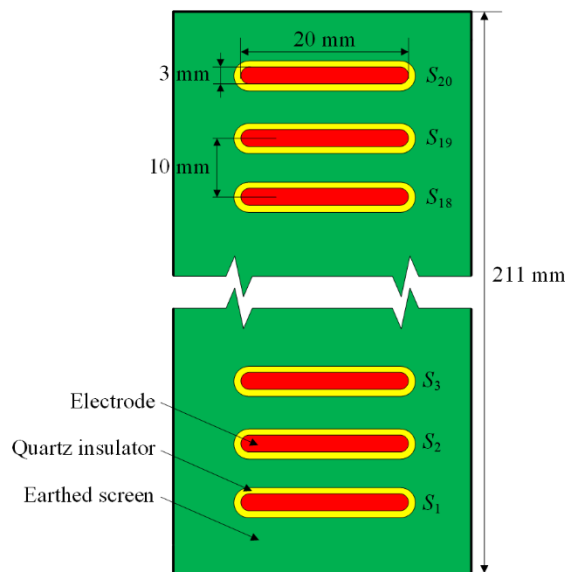
193 For many applications, a single electrostatic sensor is sufficient to measure the flame
194 oscillation frequency. For methane-fired diffusion flames, there has been limited research on
195 the measurement of oscillation frequency in different regions. The measurement of the
196 oscillation frequency in different regions of a diffusion flame is desirable for comprehensive
197 investigations into the oscillatory characteristics of the flame. In order to quantify the oscillation
198 frequencies in different regions of the diffusion flame, an array of electrostatic sensors arranged
199 linearly along the burner axis is employed in this particular study. Fig. 4 shows the design of
200 the electrostatic sensor array, an array of 20 strip-shaped electrodes with an axial width of 3 mm
201 and a length of 20 mm are housed in an earthed screen (only six electrodes are drawn in Fig. 4
202 to avoid duplication). The electrodes are evenly spaced with a spacing of 10 mm. The vertical
203 span of the sensor array is the same as the height of the flame to verify its feasibility. The
204 electrodes are supported by a grounding screen to eliminate electromagnetic interference. The

205 metal electrodes and quartz insulators meet the requirement of high-temperature resistant
 206 sensors.

207 The sum of the signals from the electrostatic sensor array can be adopted to indicate the
 208 total amount of transferred charges from the flame and thus the overall fluctuation of the flame
 209 shape, which is expressed as

$$210 \quad S_{sum} = \sum_{i=1}^N S_i(t) \quad (7)$$

211 where $S_i(t)$ ($i= 1, 2, \dots, N$) denotes the i^{th} sensor signal and N is the total number of sensors that
 212 are used to encompass the flame height. The power spectrum of S_{sum} is analysed to acquire the
 213 information about the overall movement of the flame. A comparison between the overall and
 214 local dynamic properties of the flame can be thus conducted.



215
 216 **Fig. 4.** Structure of the electrostatic sensor array.

217 3. Experiments and results

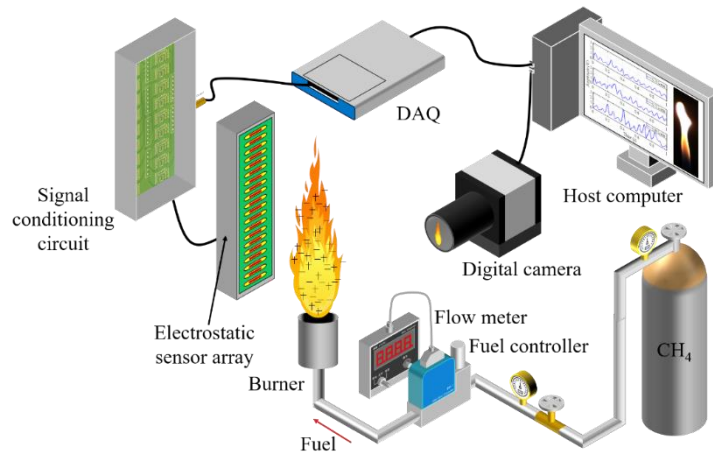
218 3.1. Experimental conditions

219 To evaluate the proposed methodology, experimental tests were carried out on a gas-fired
 220 combustion rig. Fig. 5(a) illustrates the layout of the test rig. A methane gas cylinder supplies
 221 the fuel at a maximum flow rate of 2 L/min. For a diffusion flame, the change in the fuel
 222 flowrate leads to the variation in the jet velocity of the fuel, and then affects the rate of chemical

223 reactions and buoyancy convection, and hence the oscillation of the flame. The fuel flow rate is
224 therefore varied to achieve different test conditions. The fuel flow rates are regulated by the
225 flow controller, and measured and displayed by the flow meter. A burner that has an outer
226 diameter of 24 mm is adopted to create diffusion flames in a combustion chamber with a length
227 of 800 mm and a height of 700 mm. The flame is stabilized using a mesh screen installed at the
228 burner outlet. Fig. 5(b) and (c) show the photos of the test rig together with the electrostatic
229 sensor array and signal conditioning module, respectively. The array is mounted on a support
230 frame, allowing the adjustment of the distance from the flame to the electrode. The reference
231 oscillation frequency is obtained using a digital camera (Photron, FASTCAM Mini UX50),
232 which acquires the flame images at a rate of 250 frames per second and with a resolution of
233 $1280 (H) \times 1024 (V)$. The flame intensity, which equals the sum of the pixel grey values in the
234 image, is deemed to a reference signal. The measured oscillation frequencies in different
235 regions are compared against the intensity of the flame image corresponding to each electrode,
236 which equals the sum of the pixel grey values in the segmented image and is deemed to a
237 reference signal.

238 In order to verify the proposed method, it is essential to acquire the sensor signals and
239 flame images simultaneously. Fig. 5(a) shows the arrangement of the sensor head and the
240 imaging device. The fluctuations of the signals are related to the variations in the flame shape,
241 i.e. the change in the distance from the flame boundary to the sensor head, and the camera can
242 capture precisely the change of such flame boundary. The arrangement in Fig. 5(a) is therefore
243 reasonable. The sampling frequency of flame images is the same as that of the sensor signal.
244 Synchronous acquisitions of the sensor signals and the images were realized using a digital
245 signal from the acquisition card which triggers the digital camera. Then, the sensor signals were
246 fed to a host computer for the calculation of the oscillation frequency. A standard frequency-
247 varying light source with a resolution of 1 Hz was adopted as an ideal flame light to calibrate

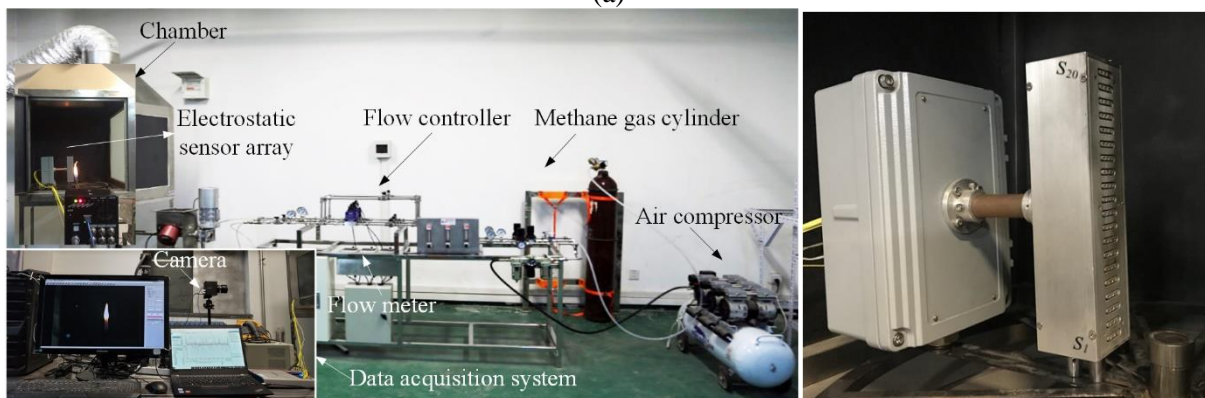
248 the digital camera [29]. The frequency varied from 10 to 60 Hz with an interval of 10 Hz. Fig.
249 6 illustrates a direct comparison between the frequency from the imaging system and the
250 reference frequency from the light source. The relative error of the measured frequency is found
251 to be within $\pm 2\%$. An important point to stress is that previous experimental tests have verified
252 that the non-reactive gas flow leads to no generation of the signal from the electrostatic sensor.



253

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(a)



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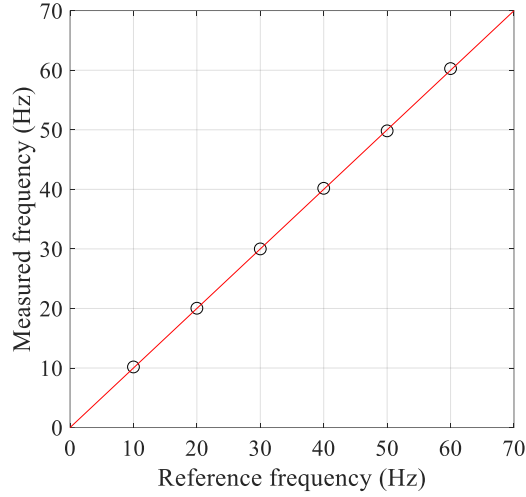
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Fig. 5. Experimental setup. (a) Layout of the test rig. (b) Photo of the test rig. (c) Photo of the

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electrostatic sensor array and signal conditioning module.

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Fig. 6. Comparison between the measured frequency from the imaging system and the reference frequency.

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In this study the accuracy of the measurement system is quantified in terms of relative deviation, i.e. the discrepancy between the measured and reference values:

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$$D_r = \frac{F_e - F_i}{F_i} \times 100\% \quad (8)$$

266

where F_e and F_i are the measured and reference oscillation frequencies, respectively. The

267

repeatability of the system is represented by the normalized standard deviation of the measured

268

oscillation frequency [19]:

269

$$\delta = \frac{\sigma}{\bar{F}_e} \times 100\% \quad (9)$$

270

where σ and \bar{F}_e are the standard deviation and mean of the oscillation frequency, respectively.

271

Since the normalized standard deviation (δ) depends on both the repeatability of the

272

measurement system and that of the test rig, the true repeatability of the measurement system

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is better than δ . A total of 25 measurements under the same test condition over a period of 100

274

s were acquired in each repeatability test.

275 3.2. Characteristics of sensor signals

276 3.2.1. Validation of the electrostatic sensing technique

277 A sequence of snapshots of a typical diffusion flame is illustrated in Fig. 7, which shows
278 the movement of the flame during one pulsation period. The instantaneous flame images in Fig.
279 7 were captured from 52 to 124 ms with an interval of 4 ms. Fig. 8 shows flame images at
280 maximum and minimum radiation intensities for four pulsation periods, which are marked as a,
281 b, ... and h. In this case, the installation distance from the sensor to the burner axis is set to 25
282 mm. The corresponding sum of signals from the electrostatic sensor array and grey levels of
283 flame images are shown in Fig. 9. It can be seen that both measurements contain a significant
284 periodic component. Scrupulous observations of such two signals and flame images in Fig. 8
285 show that, when the flame height peaks, the magnitude of the sensor signal and the grey level
286 also reach maxima (moments 'b', 'd', 'f', and 'h' in Fig. 9). Such results illustrate that the
287 electrostatic sensors can sense the change of flame shape.



288

289 **Fig. 7.** Flame snapshots during one period (fuel flow rate = 0.65 L/min).

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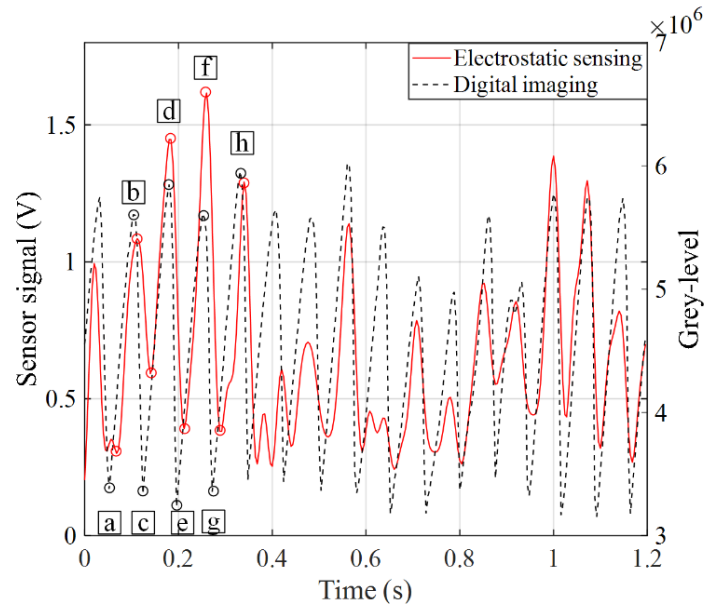


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291 (a) 52 ms (b) 104 ms (c) 124 ms (d) 180 ms (e) 196 ms (f) 252 ms (g) 272 ms (h) 332 ms

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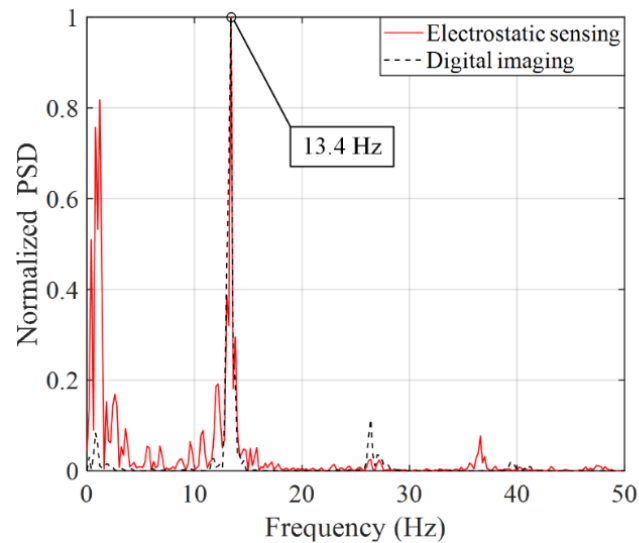
Fig. 8. Flame images at minimum and maximum radiation intensities.



293
 294 **Fig. 9.** Typical signals from the electrostatic sensor array and imaging system (fuel flow rate = 0.65
 295 L/min). (a, b, ... and h represent moments that the radiation intensities of flame images reach
 296 minimum and maximum for four pulsation periods, respectively)

297 The corresponding PSD of the sensor signal and grey levels of flame images in Fig. 9 with
 298 a duration of 5 s are depicted in Fig. 10, in which the data points are normalized to the highest
 299 peak. The frequency response of the sensor signal shows a peak at 13.4 Hz, which is identical
 300 to the result from the digital imaging system. It can be seen from Fig. 10 that there exist some
 301 frequency peaks below 2 Hz in the spectra of the two types of flame signal. Scrupulous
 302 observations of the sensor signal, flame images and grey levels show that such results are
 303 attributed to the fact that the change in the flame shape is irregular, i.e., both the peak of the
 304 sensor signal and grey level are not identical for each pulsation period. There also exist peaks
 305 located in the 20-40 Hz region in higher order harmonics of the fundamental frequency (i.e.
 306 oscillation frequency). The magnitudes of higher order harmonics are much weaker than that
 307 of the fundamental frequency. In addition, there exists a prominent spectral peak (36.2 Hz)
 308 between the 2nd and 3rd order harmonics in the PSD of the sensor signal. These frequencies
 309 peaks are much lower or higher than the measured oscillation frequency and are thus ignored

310 in this study. It can be drawn from the results that the sensors can be used to measure the flame
311 oscillation frequency.



312

313

Fig. 10. Power spectra of signals in Fig. 9.

314 3.2.2. Effect of the sensor installation on the flame behaviour

315 To evaluate the influence of the sensor installation (i.e. physical presence) on the flame
316 behaviour, a comparison between the normalized PSD of grey levels of flame images with and
317 without the installation of electrostatic sensors at the fuel flow rate of 0.65 L/min was conducted,
318 as shown in Fig. 11. The installation distance from the sensors to the burner axis is 25 mm. The
319 frequency response of the grey levels with and without the electrostatic sensors yields the
320 exactly the same peak at 13.4 Hz, illustrating that the presence of the electrostatic sensors has
321 no effect on the behaviour of the flame. Such results illustrate that the electrostatic sensing
322 method is capable of providing non-intrusive measurement of the oscillation frequency.

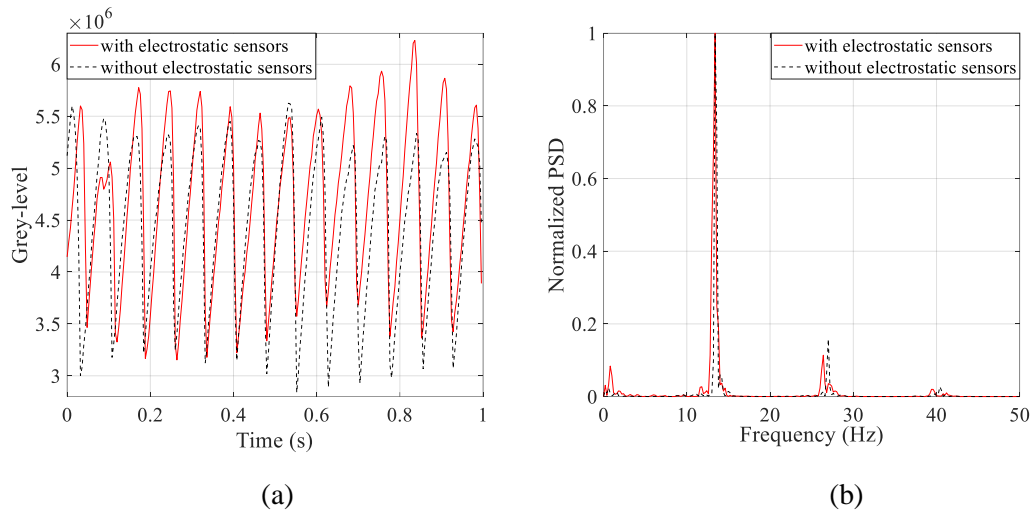


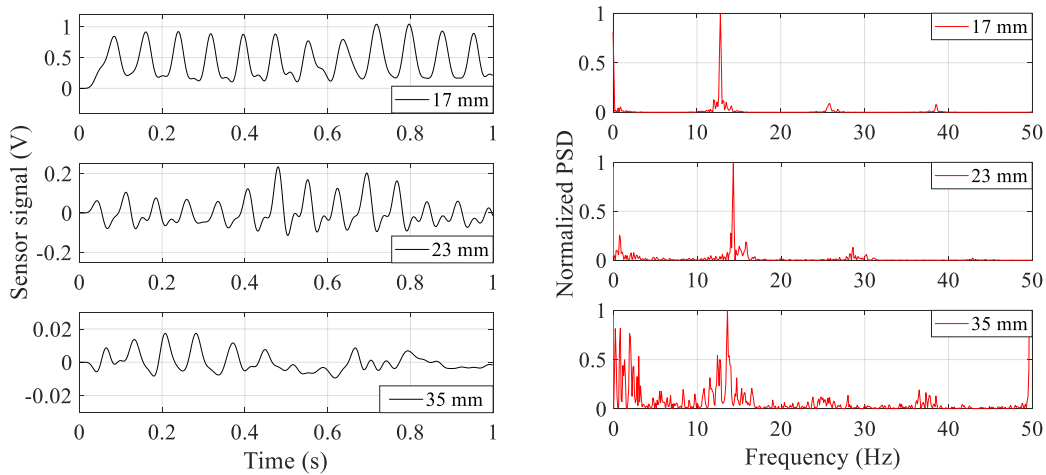
Fig. 11. Grey levels of flame images and their normalized PSD with and without the installation of electrostatic sensors (fuel flow rate = 0.65 L/min). (a) Grey levels. (b) Normalized PSD.

3.2.3. Effect of the installation distance of the sensor on the measurement results

The installation distance from the sensor to the burner axis plays a significant part in the oscillation frequency measurement system. A series of experiments were thus conducted to investigate the effect of the installation distance on the measurement results, and obtain the maximum distance for valid oscillation frequency measurement at different voltage gains of the trans-resistance amplifier (Fig. 2) determined by the feedback resistor (R_f). This was achieved by gradually increasing the distance from 17 mm to 50 mm with an increment of 3 mm until the oscillation frequency became unstable or erroneous. The minimum installation distance of the sensor is 17 mm. Fig. 12 shows typical signals S_{I3} and their corresponding PSD at various distances with $R_f = 10 \text{ M}\Omega$ and $R_f = 1 \text{ G}\Omega$, respectively. At the higher gain, the signals at the distance smaller than 20 mm has been ignored due to signal saturation. As can be seen in Fig. 12(a), (c) that the greater the distance from the electrode and the burner axis, the weaker the output signal as less charges are transferred to the electrode surface. Observations of the power spectra of the signals at various distances have shown that the maximum distance from the sensor to the burner axis for valid oscillation frequency measurement is 35 mm and 55 mm, respectively, for $R_f = 10 \text{ M}\Omega$ and $R_f = 1 \text{ G}\Omega$. A point to stress is that the maximum distance may be increased further if the voltage gain of the trans-resistance amplifier in the signal

344 conditioning module (Fig. 2) is set higher. Fig. 12(b) shows that the dominant frequency at the
345 distance of 17 mm is smaller than under other conditions due to the fact that the closer spacing
346 from the sensor to the flame increases the possibility of physical contact between them.

347 The root mean square (RMS) value of the sensor signal is employed to indicate its
348 fluctuations, as shown in Fig. 13(a). As expected, the signal magnitude decreases with the
349 installation distance. The measured oscillation frequencies for different distances are indicated
350 in Fig. 13(b). It can be seen that the relative deviation of the measured frequency from the
351 reference value increases with the distance when it is larger than 20 mm. It is because that a
352 larger distance leads to a lower signal to noise ratio. Therefore, in consideration of the signal to
353 noise ratio and the possibility of physical contact between the flame and the electrode, the
354 installation distance from the sensor to the burner axis is set to 25 mm in this study. The
355 precision of the available resistor of 1 G Ω can only reach 5% due to the limitation of the
356 manufacturing process. In order to ensure the consistency of multiple signal conditioning
357 channels, a feedback resistor R_f of 10 M Ω with a precision of 0.1% is used in this study.



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(a)

(b)

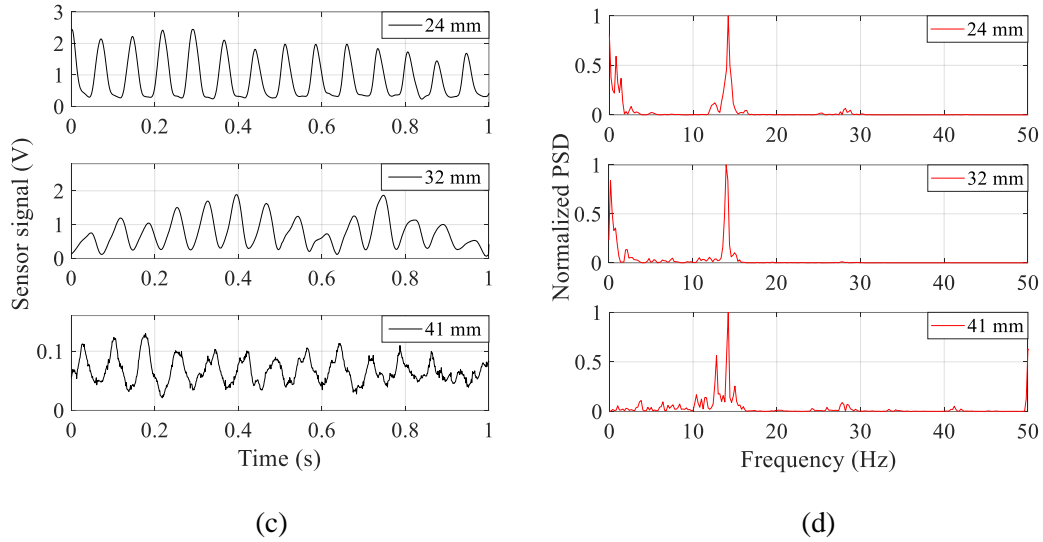


Fig. 12. Sensor signals and the corresponding PSD for different installation distances. (a) Sensor signals when $R_f = 10 \text{ M}\Omega$. (b) Power spectra of signals in Fig. 12(a). (c) Sensor signals when $R_f = 1 \text{ G}\Omega$. (d) Power spectra of signals in Fig. 12(c).

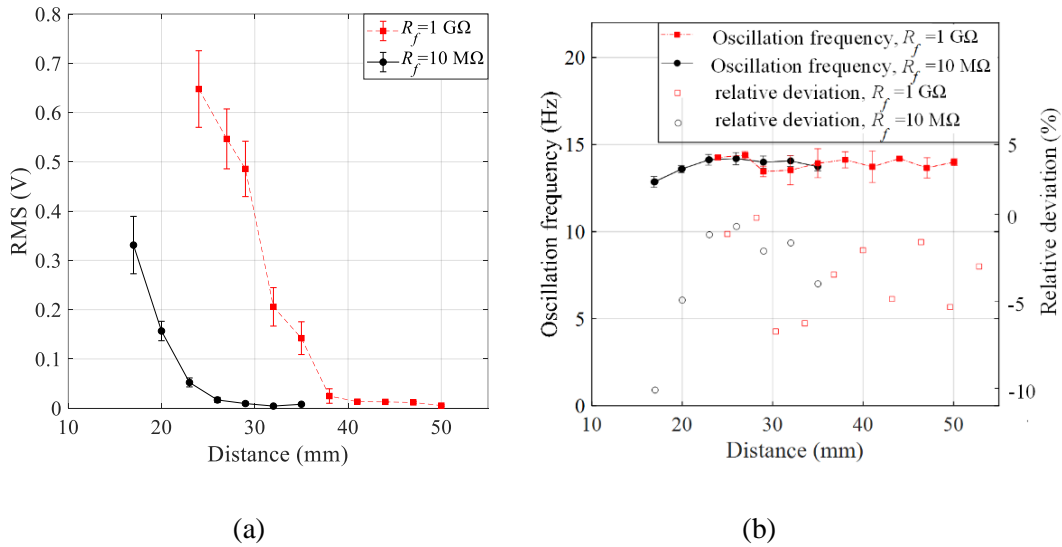


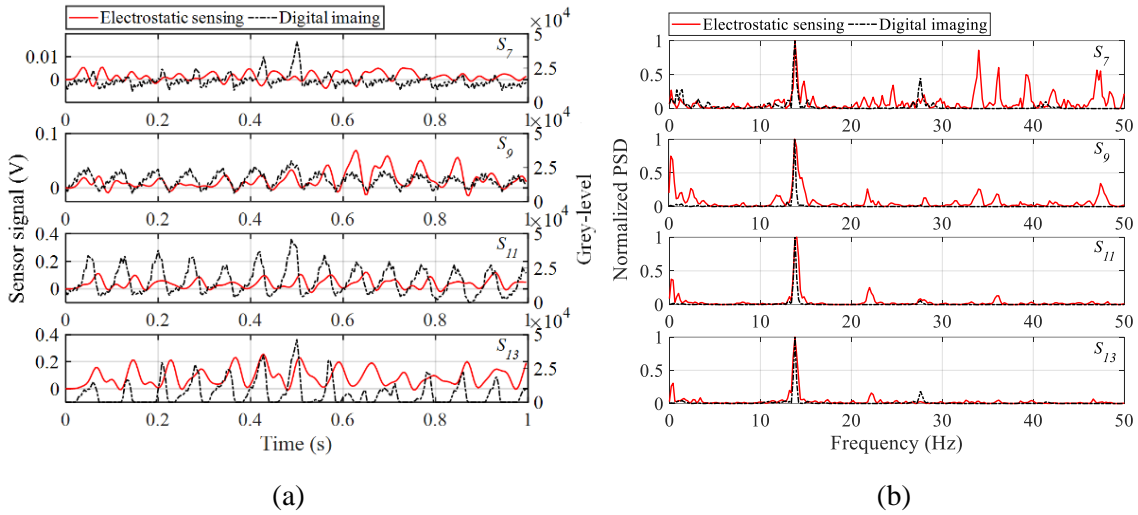
Fig. 13. Signal magnitude and oscillation frequency at various installation distances. (a) Signal magnitude. (b) Oscillation frequency and its relative deviation.

3.2.4. Sensor signals

For laminar diffusion flames, experimental tests were conducted under five conditions.

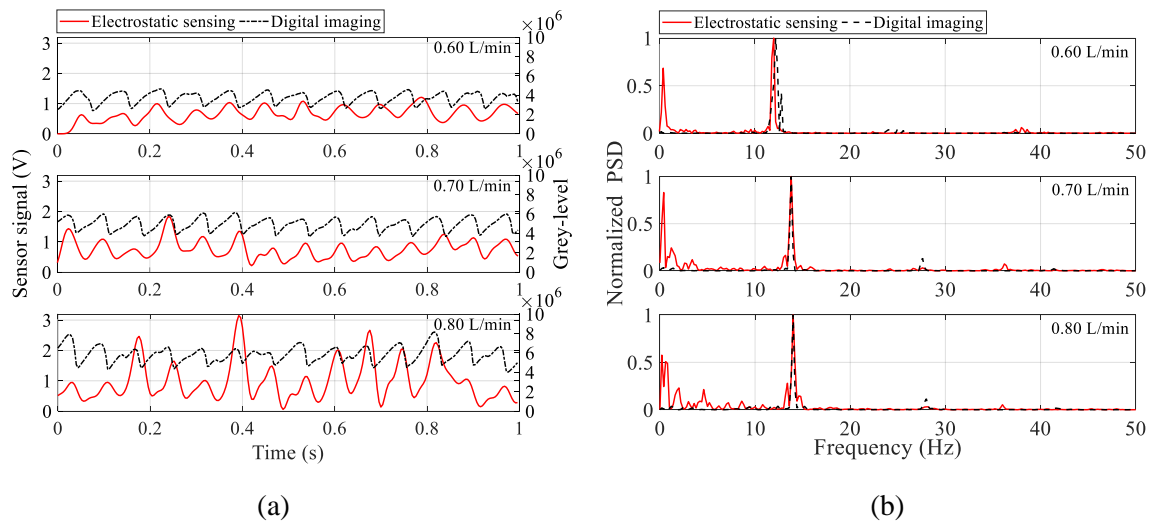
The fuel flow rate was varied from 0.60 L/min to 0.80 L/min (Reynolds number equals to 170-240) with an interval of 0.05 L/min. Fig. 14(a) illustrates typical signals S_7, S_9, S_{11}, S_{13} and grey level signals when the fuel flow rate is 0.70 L/min. As can be seen from Fig. 5(c), sensor 1

374 corresponds to the flame root and sensor 20 the flame tip. At the fuel flow rate of 0.7 L/min,
375 sensors 1 to 7 correspond to the region of the flame root. The signals S_1 , S_2 , ..., and S_6 are
376 similar to the signal S_7 , but with a smaller amplitude, and hence not plotted. Sensors 8 to 12,
377 situated at the middle region of the flame, and the signal waveforms exhibit similar
378 characteristics. Sensors 13 to 17 are located in the flame tip. A point to note is that the flame
379 height varies with time under fixed test conditions. When the fuel flow rate is 0.70 L/min, the
380 tip of the shortest flame can reach up to sensor 13 and hence signal S_{13} is plotted. A smaller
381 fluctuation of the amplitude was observed in both the signal S_7 and the corresponding grey level
382 of flame images. It results from the increasing distance from the flame to the electrode and
383 slighter fluctuation of the flame in its root region. It can be seen that signals S_9 and S_{11} and the
384 corresponding grey level exhibit a larger amplitude because of the closer distance in the middle
385 region. Sensor 13, situated at the flame tip, generates a signal of a much larger amplitude owing
386 to the closer distance and significant fluctuation at the flame tip. Smaller amplitude is observed
387 in the corresponding grey level, which is consistent with the observations in flame images. Both
388 signals from the electrostatic sensors and the digital imaging system exhibit a clear periodicity.
389 The corresponding normalized PSD of the signals (Fig. 14(a)) are plotted in Fig. 14(b). The
390 flame has a main component at a comparatively lower frequency, indicating a good agreement
391 with the flame imaging studies conducted by Huang *et. al.* [15]. A distinct peak can be seen at
392 13.8 Hz in the spectra of the two types of signals, demonstrating that the oscillation frequencies
393 of the flame are similar along the burner axis. Fig. 14(b) indicates that there are more spurious
394 peaks in the 30-40 Hz region in the signal S_7 . This is because the root region where sensor 7 is
395 located exhibits more rigorous kinetic variations in the rate of energy emission of reacting
396 species, resulting in the existence of higher frequency components in the PSD, though this
397 region is relatively more stable geometrically than other parts of the flame.



398
399
400 **Fig. 14.** Typical signals from sensors 7, 9, 11, 13 and grey levels from the digital camera and the
401 corresponding power spectra. (a) Typical signals. (b) Power spectra.

402 Fig. 15(a) shows the sum of signals obtained from the sensor array and grey levels at the
403 fuel flow rate of 0.60, 0.70 and 0.80 L/min, respectively. It is clear from Fig. 15(a) that the
404 sensor signal and the grey level of the flame images depend on the fuel flow rate. Unsurprisingly,
405 the signal amplitude increases with the fuel flow rate, because of the increasing chemical
406 reactions at a higher fuel flow rate and hence the resulting generation of more free electrons,
407 ions and soot. Fig. 15(b) illustrated the corresponding power spectra of the signals and grey
408 levels. The magnitudes of the peaks in both power spectra are almost the same.

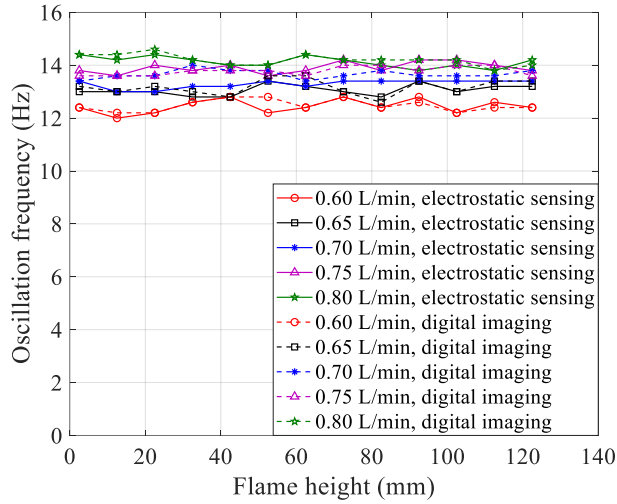


409
410
411 **Fig. 15.** Typical signals from the sensor array and grey levels from the digital camera for different fuel
412 flow rates. (a) Typical signal waveforms. (b) Power spectra of the signals.

414 3.3 Measurement Results

415 Fig. 16 shows the measurement results of oscillation frequencies in different flame regions.
416 The measured and reference oscillation frequencies in different flame regions for various fuel
417 flow rates are depicted in Fig. 16(a). The height of the measured flame increase with the fuel
418 flow rate, but within a narrow range. For a diffusion flame, the flame tip can reach up to the
419 13th electrode (fuel flow rate = 0.65 L/min). In order to compare the variation of the oscillation
420 frequency with the flame height for different fuel flow rates, the signals from 13 sensors, i.e.
421 sensors 1 to 13, for each fuel flow rate are used to obtain the measurement results. As shown in
422 Fig. 16(a), the measured and reference oscillation frequencies yield a similar trend. It can be
423 observed that the oscillation frequencies in different regions of the diffusion flame vary within
424 a small margin for each fuel flow rate, indicating that the oscillation of the flame shape along
425 the longitudinal direction is consistent. For the larger fuel flow rate, the oscillation frequency
426 is mostly larger than that for the smaller one at the same flame height.

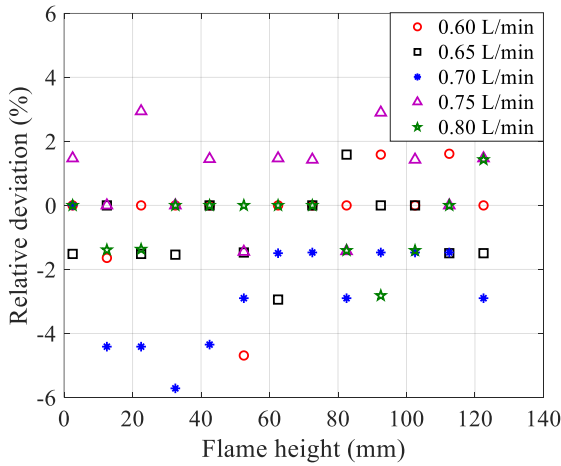
427 For all measured flames in this study, the flame height lower than 102.5 mm corresponds
428 to the root and middle regions of the flame whilst that higher than 102.5 mm corresponds to the
429 flame tip. As shown in Fig. 16(b), the relative deviation of the measured oscillation frequency
430 from the reference value is mostly within $\pm 5\%$. Normalized standard deviation of the measured
431 oscillation frequency in different regions of the diffusion flame, as shown in Fig. 16(c), is not
432 greater than 10% for the root and middle regions and less than 5% for the flame tip. In other
433 words, the standard deviation of the measured oscillation frequency for the flame tip is smaller
434 than that for the root and middle regions. This is because that the flame tip fluctuates more
435 strongly due to aerodynamic or convective effect and then more charges are transferred on the
436 electrode at the corresponding location owing to the closer distance and hence better signal
437 quality. The system performs better in terms of repeatability at the flame tip because of the
438 increased charge on the electrode.



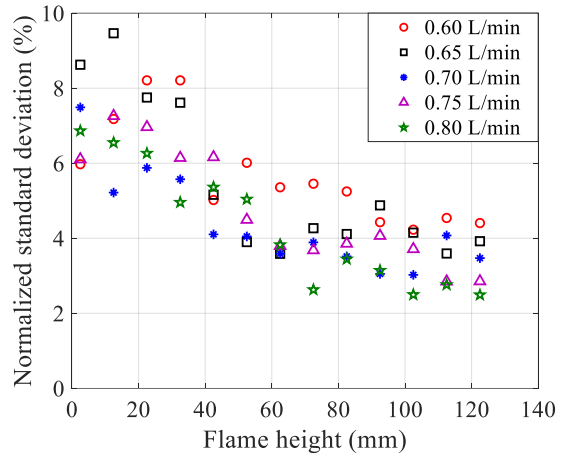
439

440

(a)



441



442

443

Fig. 16. Measured oscillation frequencies and their deviations in different regions of the diffusion

444 flame. (a) Comparison between the measured and reference frequencies. (b) Relative deviation of the

445 measured oscillation frequency. (c) Normalized standard deviation of the measured oscillation

446 frequency.

447 Fig. 17 shows the measured oscillation frequencies of the whole flame for different fuel

448 flow rates. A comparison between the oscillation frequencies of the diffusion flame from the

449 sensors and the imaging system for different fuel flow rates are depicted in Fig. 17(a). All data

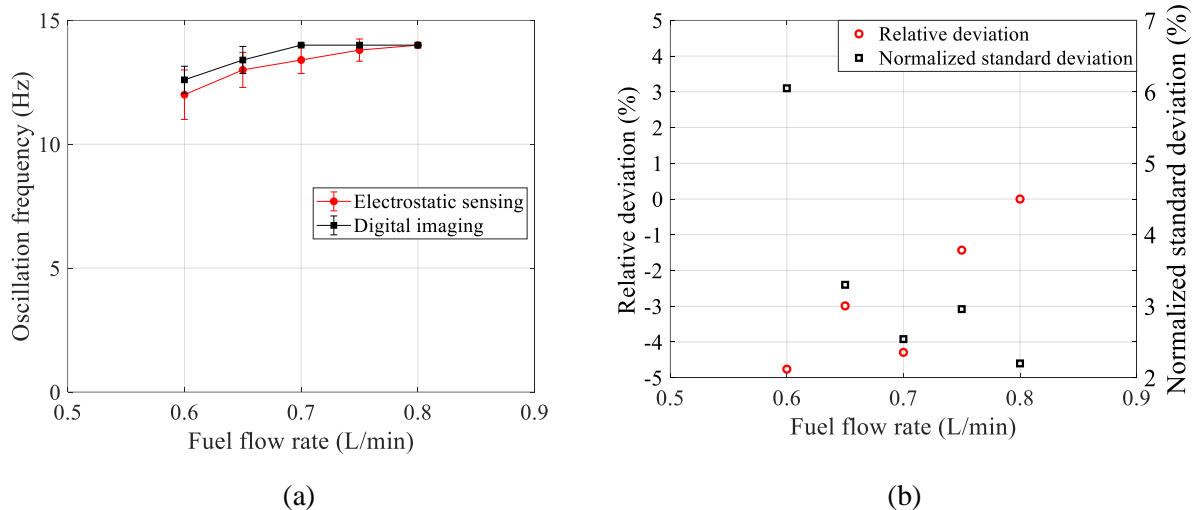
450 points in Fig. 17(a) are average values with standard deviations showed as error bars. It is

451 obvious that both the measured and reference oscillation frequencies have an increasing trend.

452 Fig. 17(a) indicates that the measured oscillation frequency of the whole flame is slightly

453 smaller than the reference due to two different sensing mechanisms, and the standard deviation
 454 of the measured oscillation frequency is greater than that of the reference value. The reason for
 455 the larger standard deviation of the measured value is that the electrostatic sensing technique is
 456 slightly more sensitive to electrical interference in the environment despite the sensor is earthed
 457 properly.

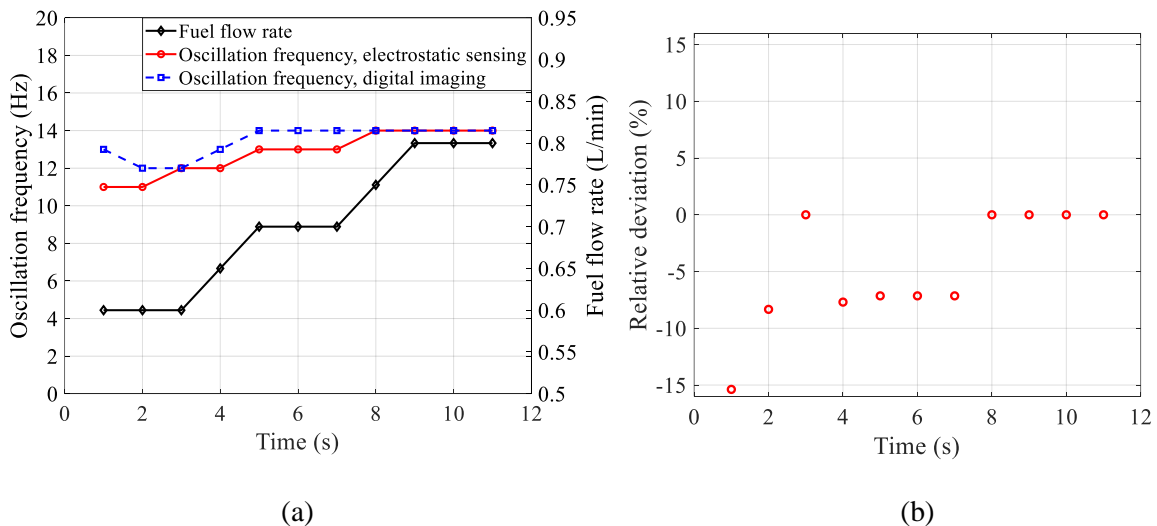
458 Fig. 17(b) shows that the relative deviation and normalized standard deviation of the
 459 measured oscillation frequency for different fuel flow rates. The relative deviation is within -
 460 5% for the lower fuel flow rate but less than -2% for the higher fuel flow rate. The normalized
 461 standard deviation is not greater than 6% for the lower fuel flow rate, but less than 3% for the
 462 higher fuel flow rate. As the fuel flow rate increases, more charged species are generated
 463 through chemical reactions, hence the increased transferred charge on the electrode and higher
 464 signal to noise ratio, leading to smaller standard deviation of the measured value and hence
 465 better repeatability in the oscillation frequency measurement.



466
 467 **Fig. 17.** Measured oscillation frequencies and their deviations for different fuel flow rates. (a)
 468 Comparison between the measured and reference frequencies. (b) Relative deviation and normalized
 469 standard deviation of the measured oscillation frequency.
 470

471 The performance of the developed system for the on-line continuous measurement of
 472 instantaneous oscillation frequency of a diffusion flame is verified in comparison to the

473 reference value from the imaging system. Experimental tests were carried out by gradually
 474 increasing the fuel flow rate from 0.60 to 0.80 L/min over a period of 11 s. As can be seen in
 475 Fig. 18(a), the instantaneous oscillation frequency measured using the electrostatic sensing
 476 technique follows an increasing trend with the fuel flow rate, so does the reference from the
 477 digital imaging approach. The measured value is slightly smaller than the reference. Such
 478 results are consistent with the earlier observations (Fig. 17(a)). As can be seen in Fig. 18(b), the
 479 relative deviation is mostly between -10% and 0%. The results demonstrate that the developed
 480 electrostatic sensing system can measure the instantaneous oscillation frequency of a diffusion
 481 flame under dynamic conditions.



482
 483 (a) (b)
 484 **Fig. 18.** Results for step changes in fuel flow rates. (a) Measured and reference frequencies. (b)
 485 Relative deviation of the measured instantaneous oscillation frequency.

486 3.4 Discussion

487 Measured oscillation frequencies of different regions and the whole flame are similar for
 488 each fuel flow rate, indicating the overall and local fluctuations of the flame are consistent. The
 489 outcomes of the whole flame are more repeatable and slightly closer to the reference values in
 490 comparison with those of different regions of the diffusion flame. The measurement system
 491 performs better in terms of repeatability at the flame tip than root and middle regions.

492 In practical applications, either a single electrostatic sensor or an array of sensors can be
493 used to monitor the flame and this will depend on the requirement of flame monitoring. The
494 aforementioned results indicate that a single sensor installed at the flame tip is sufficient for the
495 oscillation frequency measurement of a diffusion flame. An array of sensors can be used to
496 monitor the whole flame with higher accuracy and better repeatability. However, it is essential
497 to take the flame size into consideration to determine the number and installation location of
498 the sensors. For example, electrostatic sensors need to be installed at the regions of interest for
499 a large furnace flame as it is impractical to deploy the sensors that cover the whole flame.

500 A flame signal from an industrial furnace often has a wide frequency spectrum and the
501 energy of the flame signal mainly distributes between 0-200 Hz [30]. In this study, the dynamic
502 range of the oscillation frequency obtained using the electrostatic sensor array depends on the
503 cut-off frequency of the low-pass filter. In practical applications, the cut-off frequency of the
504 low-pass filter can be set according to the oscillation frequency of the flame. In the
505 measurement of the flame oscillation frequency using the electrostatic sensing technique, the
506 minimum current detectable by the electrostatic sensor can be sub-nA or even in the order of
507 pA. In practice, the minimum concentration of charged species detectable by the electrostatic
508 sensor depends on the size of the electrode as well as the sensitivity and performance of the
509 signal conditioning module.

510 It should be pointed out that, in the case of a turbulent flame, the electrostatic sensor may
511 not be able to detect and identify all the possible turbulences in the flame because of the finite
512 physical dimensions of the electrode and its fundamental characteristics in electrostatic
513 induction and charge transfer. However, the signal from the electrostatic sensor contains useful
514 information about the fundamental oscillatory characteristics of the turbulent flame and can
515 therefore be used for the measurement of its effective oscillation frequency.

516

517 **4. Conclusions**

518 In this paper a measurement method of the oscillation frequency of a laminar diffusion
519 flame using electrostatic sensing and spectral analysis techniques has been presented. In order
520 to evaluate the efficacy of the developed system, experimental tests were carried out on a
521 combustion rig. Observations of the PSD of sensor signals have shown that the diffusion flame
522 has a dominant frequency within a comparatively lower range, which is in agreement with the
523 results obtained using digital imaging techniques. It has been found that the installation of
524 electrostatic sensors around the flame has no effect on the behaviour of the flame. The system
525 is capable of producing a valid oscillation frequency measurement as long as the installation
526 distance of the sensor is within an effective range.

527 The results obtained have shown that the system performs well with a maximum relative
528 deviation from the reference value not greater than $\pm 6\%$ for a fuel flow rate from 0.60 L/min
529 to 0.80 L/min. The results have suggested that the oscillation frequency of the diffusion flame
530 increases with the fuel flow rate. The oscillation frequencies in different regions of the diffusion
531 flame are similar for each fuel flow rate, indicating that the oscillation of the flame shape along
532 the longitudinal direction is consistent. The measurement system has produced more repeatable
533 results under higher fuel flow rate conditions and at the flame tip due to increased charge on
534 the electrode surface. Under dynamic conditions the system can measure the instantaneous
535 oscillation frequency with a relative deviation from the reference value mostly between -10%
536 and 0%.

537 Future research will be conducted to evaluate the efficacy of the developed technique for
538 the measurement of oscillation frequencies of complex flames under a wide range of conditions.

539

540

Acknowledgments

541 This work was supported by the National Natural Science Foundation of China under Grant
542 61673170 and Grant 51827808. The IEEE Instrumentation and Measurement Society is also
543 acknowledged for the 2018 Graduate Fellowship Award for Jiali Wu.

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