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Influence of the Cubic Sublattice on Magnetic Coupling Between the Tetrahedral Sites of Garnet

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Abstract

We present a study on the nuclear and magnetic structures of two iron-based garnets with magnetic cations isolated on the tetrahedral sites. $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ offer an interesting comparison for examining the effect of increasing cation size within the diamagnetic backbone of the garnet crystal structure, and how such changes affect the magnetic order. Despite both systems exhibiting well-pronounced magnetic transitions at low temperatures, we also find evidence for diffuse magnetic scattering due to a competition between the nearest-neighbor, next nearest-neighbor, and so on, within the tetrahedral sites. This competition results in a complex non-collinear magnetic structure on the tetrahedral sublattice creating a mixture of ferro- and antiferromagnetic interactions above the long-range ordering temperature near 20 K and suggests that the cubic site of the garnet plays a significant role in mediating the superexchange interactions between tetrahedral cations.

Introduction

$\text{Y}_3\text{Fe}_5\text{O}_{12}$ garnet (YIG) has been extensively studied due to its widespread use as a magnetic material in many commercial applications.^{1–8} Yet, many questions remain about the fundamental magnetic interactions in garnets, which is due, in large part, to the multiple sublattices and vast compositional diversity available. Garnets adopt the general formula $R_3B_2A_3O_{12}$ with three uniquely coordinated environments that can

accommodate a wide swath of the periodic table, making them an ideal test system for exploring structure-property relationships [see Figure 1].

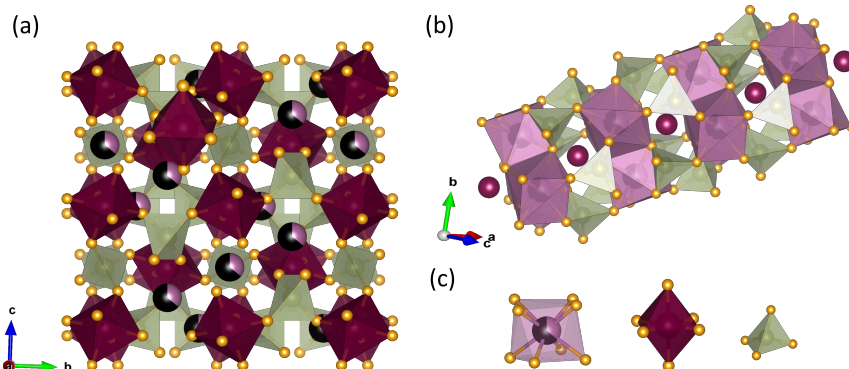


Figure 1: (a) An ideal cubic garnet unit cell along one equivalent axis. (b) Looking at a single rod with the octahedral center surrounded by alternating cubic and tetrahedral sites. (c) From left to right, the cubic site is depicted in black and pink indicating a mixed cation occupation (R , 8-coordinated), the octahedral site as maroon (B , 6-coordinated), and the tetrahedral site as light green (A , 4-coordinated).

To better understand the magnetic coupling within each sublattice, the individual sites must be isolated from one another by forcing magnetic cations to occupy a single site through judicious selection of the diamagnetic components in the material.⁹ A great deal of work has been done in this regard to study the magnetism of the octahedral and cubic sites in materials like $\text{Gd}_3\text{Ga}_5\text{O}_{12}$,⁶⁻⁸ $\text{Mn}_3\text{Al}_2\text{Ge}_3\text{O}_{12}$,^{10,11} $\text{Mn}_3\text{Al}_2\text{Si}_3\text{O}_{12}$,^{11,12} $\text{CaY}_2\text{Co}_2\text{Ge}_3\text{O}_{12}$,¹³ and $\text{Ca}_3\text{Cr}_2\text{Ge}_3\text{O}_{12}$.¹⁴ Yet, keeping cations with open valence shells on the tetrahedral site is far more challenging due to the lack of magnetic cations with a strong preference for a tetrahedral coordination environment. Instead, the simplest way to study the tetrahedral sublattice is to select cations that localize strongly to the cubic and octahedral sites, which then indirectly force more site-promiscuous cations to stay in place. To-date, only a few studies have examined the magnetism of the tetrahedral sublattice in materials like $\text{Na}_3\text{Te}_2\text{Fe}_3\text{O}_{12}$, $\text{Ca}_3\text{SnSbFe}_3\text{O}_{12}$, $\text{NaCa}_2\text{Sb}_2\text{Fe}_3\text{O}_{12}$, and $\text{Ca}_3\text{ZrSbFe}_3\text{O}_{12}$.¹⁵

As early as 1964 Geller *et al.*¹⁶ had begun to explore the magnetism of the tetrahedral sublattice and, while they were unable to prepare phase-pure samples, they hypothesized that compositions like $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ should be fully ordered with Zr on the octahedral site and Fe in the tetrahedra, but would only exhibit short-range antiferromagnetic order.¹⁶ Dodokin *et al.*¹⁵ later used Mössbauer spectroscopy to study the orientation of the moments on the tetrahedra and found that the spins no longer ordered along the $[111]$ when iron is removed from the octahedral sites. At the time, this was attributed to the extremely weak coupling seen between the tetrahedra, which is roughly an order of magnitude less than that of the octahedra.

In this report, we sought to more carefully examine the ground state magnetic order of the tetrahedral

sublattice in $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$, which only differ through a minor change in the size of the diamagnetic ions on the cubic site. Interestingly, we find that both materials exhibit clear signatures of long-range magnetic order, but also show more subtle evidence at higher temperatures for short-range correlations between the spins that manifest as a result of through-cubic polyhedra super exchange pathways. In order to better understand this short-range magnetic order, we employ Reverse Monte-Carlo (RMC) methods to model the contribution of the magnetism to the magnetic diffuse scattering data, which supports a non-collinear antiferromagnetic arrangement of the moments in the ordered structure arising from magnetic frustration, thus highlighting the importance of the cubic sublattice.

Experimental

Synthesis Polycrystalline samples were synthesized by grinding stoichiometric ratios of CaCO_3 , Y_2O_3 , La_2O_3 , ZrO_2 , and Fe_2O_3 and pressing into pellets before sintering in air in multiple heating treatments. All pellets were heated on a layer of sacrificial powder to isolate them from the zirconia crucible. Samples were first heated to 900°C for 6 hours in air to decompose the carbon containing starting materials. Samples were subsequently heated at 1250°C for 24 hours in air until phase pure.

Structure Determination Sample purity and potential site-mixing were evaluated using both X-ray and neutron diffraction. Powder XRD was performed at room temperature using 11-BM at Argonne National Laboratory at $\lambda = 0.457861 \text{ \AA}$ and $\lambda = 0.412797 \text{ \AA}$ for $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ respectively, while neutron diffraction data was collected at the HB-2A high resolution neutron powder diffractometer at High Flux Isotope Reactor at Oak Ridge National Laboratory.

Physical Property Measurements Temperature- and field-dependent DC magnetic susceptibility, AC magnetic susceptibility, and heat capacity were measured on a Quantum Design 14T Dynacool Physical Property Measurement System. All magnetic measurements were performed on bulk powder samples held in place using eicosane wax. Heat capacity measurements were measured on powdered samples mixed with equal parts silver in order to increase the thermal coupling to the sample stage. The silver and epoxy contribution were measured separately and subtracted out.¹⁷

RMC-SPINVERT Since the diffuse magnetic neutron scattering was strongest in the 18 K data of the $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ phase this was isolated by removal of the nuclear scattering through subtraction of the 100 K data set. The data were then placed on an absolute intensity scale ($\text{barn sr}^{-1} \text{ Fe}^{-1}$) by normalisation to the calculated nuclear Bragg profile from the 100 K data set. This diffuse magnetic scattering was subsequently

fitted using the RMC program – SPINVERT,¹⁸ using a supercell of $6 \times 6 \times 6$ units of the cubic crystal structure with a total volume of $442,284 \text{ \AA}^3$. Spins in these refinements were refined as three dimensional vectors, as expected for tetrahedral $d^5 \text{ Fe}^{3+}$ magnetic cations, with magnetic moments fixed to $5.92 \mu_B$ and standard analytical magnetic form factors. The value of $5.92 \mu_B$ was chosen to reflect the expected magnetic moment that an octahedrally coordinated Fe^{3+} will experience in a high-spin coordination environment.

Results and Discussion

Both $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ exhibit signatures of antiferromagnetic order in the DC magnetic susceptibility starting near 18 and 21 K respectively but, more interestingly, these sharp peaks were followed by more broadened features starting around 10 K ($\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$) and 7 K ($\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$), as seen in the insets of Figure 2. When completely removing magnetic cations from the octahedral site, it comes as no surprise that the ordering temperature would drop from the 570 K seen in YIG to the low temperatures found for $\text{Ca}_2\text{MZr}_2\text{Fe}_3\text{O}_{12}$, but it is somewhat unexpected that the tetrahedral sublattice would order as high as 20 K given the lack of short superexchange pathways to couple the spins. Yet, extensive work on ferrimagnets like YIG have clearly shown the antiferromagnetic tetrahedra–tetrahedra ($A - A$) coupling is stronger than the antiferromagnetic octahedra–octahedra ($B - B$) interactions.¹⁶ More unexpected is the presence of two magnetic ordering transitions since this type of order is more common for materials containing multiple magnetic sublattices as in $\text{Mn}_3\text{Cr}_2\text{Ge}_3\text{O}_{12}$.¹⁹ So given that Fe^{3+} has very little preference to sit on any one of the sites within the garnet structure, care was taken to rule out any cation mixing between the sites or the presence of minute paramagnetic impurities.

As such, X-ray and neutron powder diffraction were collected at Argonne and Oak Ridge National laboratory respectively to fully characterize the nuclear and magnetic structure. Both data sets were carefully refined and showed no evidence for any site mixing of the Fe onto the octahedral or cubic site as demonstrated in Figure 3, with the relevant parameters from the refinement given in SI Table S2 and S3. This strongly suggests that both features in the magnetic susceptibility are associated solely with the tetrahedral site. Fitting the high-temperature region (150-300 K) of the susceptibility to the Curie-Weiss equation and including a temperature independent paramagnetic contribution, $\chi = C/(T - \Theta_{CW}) + \chi_0$, yields a Θ_{CW} of -85 K (-82K) and an effective paramagnetic moment of 6.1 (6.2) μ_B per Fe and $\chi_0 = 9.4 \times 10^{-4}$ (5.5×10^{-3}) $\text{emu mol}^{-1} \text{ Oe}^{-1}$ for the Y and La analogue respectively. This moment is in close agreement with the expected value for Fe^{3+} $5.92\mu_B$ in a high-spin tetrahedral coordination environment (d^5 , $S=5/2$, $L=0$).²⁰ The negative sign of Θ_{CW} indicating that antiferromagnetic exchange is dominant between the spins and that there is a modest suppression of the ordering temperature due to geometrical competition between the exchange interactions.

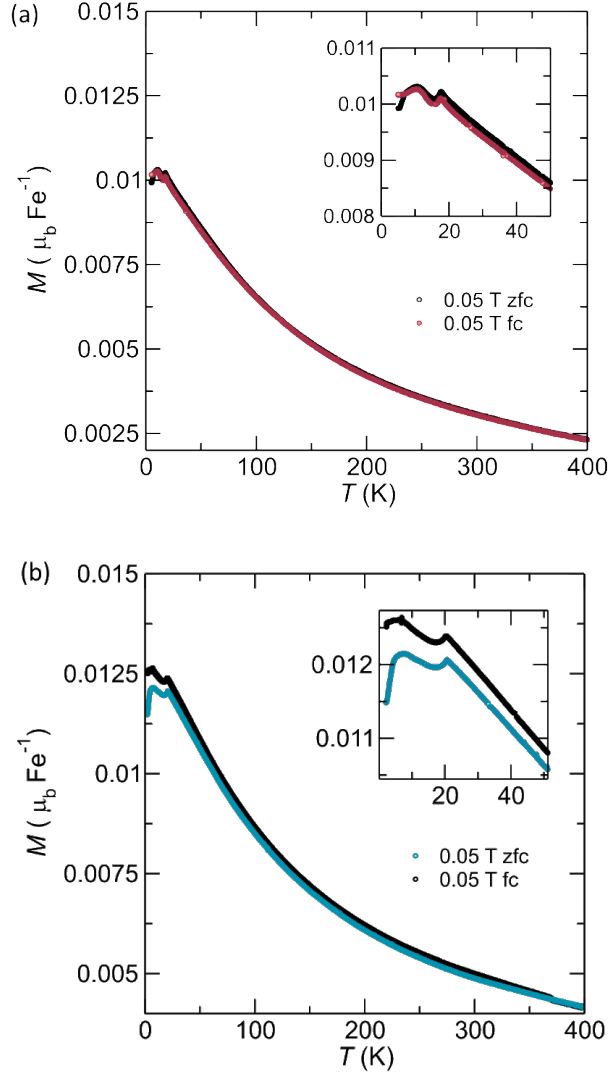


Figure 2: Temperature dependent DC magnetic susceptibility under 500 Oe from 2 to 400 K. (a) $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ orders at 18 K and (b) $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ orders at 21 K.

Neutron powder diffraction was performed at several temperatures around the magnetic transitions to monitor the onset of magnetic order. As the temperature is decreased, magnetic reflections gradually appear, as seen in Figure 4(a) and (b) for $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ respectively. The higher angle magnetic peaks appear sharply below the respective ordering temperatures as is expected when new scattering planes are created as the thermal energy is no longer sufficient to disrupt the cooperative ordering of the spins and the spins form an ordered structure over a relatively small temperature range. This contrasts with the peak at 15° , for both samples, where a diffuse peak slowly begins to evolve well above the peak in the susceptibility and gradually shifts to lower theta until the sharp appearance of the magnetically ordered Bragg peak. This diffuse peak continues to grow with decreasing temperature as well as shifting to slightly

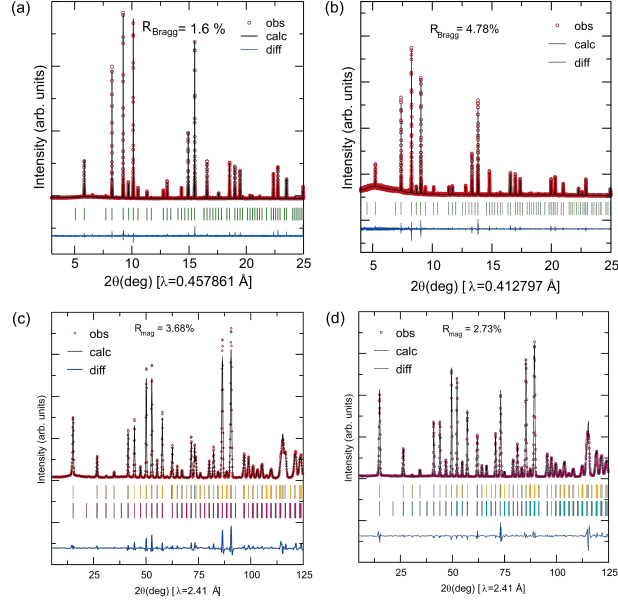


Figure 3: Results of structural refinement against X-ray and neutron data of $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ in the left and right column respectively. (a) and (b) are Rietveld fits of X-ray powder diffraction powders from 11-BM at 295 K. The red circles, black line, and blue line represent the the observed pattern, fitting line, and difference line respectively. (c) and (d) are refined fits from the corresponding neutron powder diffraction data at 1.5 K with the vanadium sample can (dark green) used in the experiment. Nuclear reflections are highlighted in yellow on the first row while the magnetic reflections are the second row.

lower theta as illustrated in Figure 4 and SI Figure S5.

At room temperature, or any temperature within the paramagnetic state, the Bragg reflections in the neutron data are fit well using solely the cubic $\text{Ia}\bar{3}\text{d}$ nuclear structure of the garnet. Below the ordering temperature, additional peaks appear at 15° , 47° , 67° , and 84° with magnetic contribution to several of the nuclear peaks at 26° , 35° , and 41° . Representational analysis was used to fit the neutron data at 1.5 K with the following associated magnetic reflections at: 15° , 26° , 35° , 41° , 47° , 67° , and 84° . All the observed magnetic reflections were indexed using the propagation vector $\mathbf{k} = 0$, but within the space group $\text{R}\bar{3}\text{c}$ (# 167), which corresponds to a $\sqrt{2} \times \sqrt{2} \times 2$ supercell of the cubic structure.²¹ The space group symmetry was lowered based on literature and historical precedence where iron garnets have been more accurately modeled using trigonal space groups.^{9,22,23} For example, it has been observed that the magnetic structure of YIG cannot be accurately described using the cubic symmetry, so instead $\text{R}\bar{3}$ for better agreement with bulk magnetometry. $\text{R}\bar{3}\text{c}$ was chosen while exploring the possible subgroups and subgroup pathways to $\text{R}\bar{3}$ using Bilbao Crystallographic Server.^{24,25}

Symmetry analysis of the magnetic structure was performed using SARAh,²⁶ which returned five one-dimensional and one two-dimensional representations within the Little Group G_k . Both compositions were

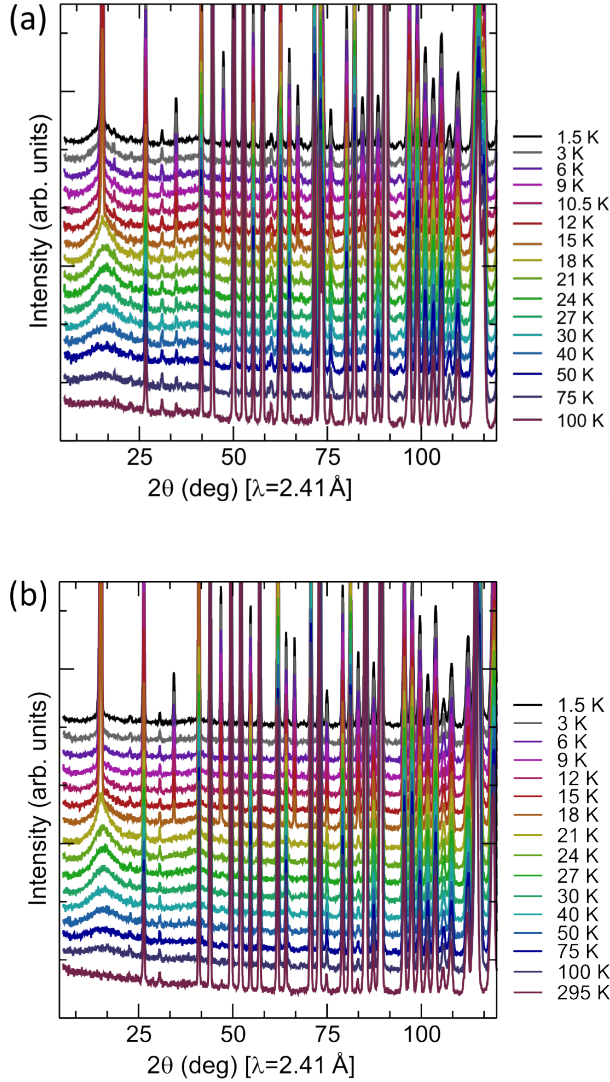


Figure 4: The temperature dependent neutron data for each composition where symmetry-allowed magnetic peaks appear at (a) 18 K for $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and (b) 21 K for $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$. Both compositions have a dynamic diffuse scattering peak at the (101) reflection (15°) before the systems order.

fit using the fourth representation, Γ_4 , as seen fit in Figure 3 and illustrated in Figures 5 and 6. This representation consists of the basis vectors listed in SI Table S1 and produce a non-collinear arrangement of the spins that wraps around the rods as seen in Figure 5. Within $R\bar{3}c$, the rods are oriented along the c -axis with the majority of the magnetic moment laying within the ab -plane rather than simply aligning along a common easy axis. The magnetic moment at 1.5 K refined to a value of 3.28 and $3.97 \mu_B$ for $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ respectively and is in agreement with the isothermal M-H measurements, which exhibit a linear response (SI Figure S3) and fail to saturate by 14 T at 2 K and only reach a maximum value of 2.59 and $2.79 \mu_B$ for $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ respectively.

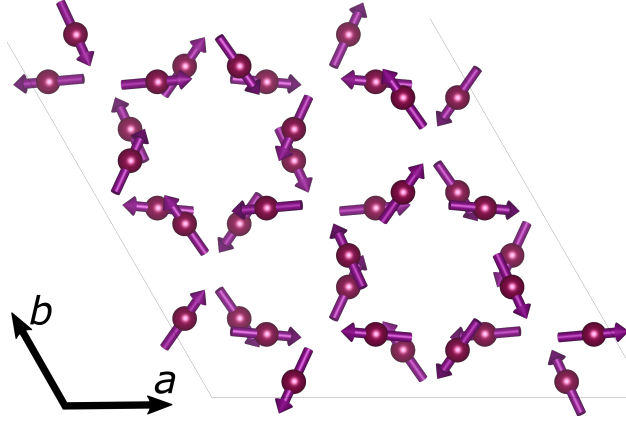


Figure 5: The resulting magnetic structure of $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ at 1.5 K. While both compositions are refined using the same representation $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ is presented in SI Figure S6.

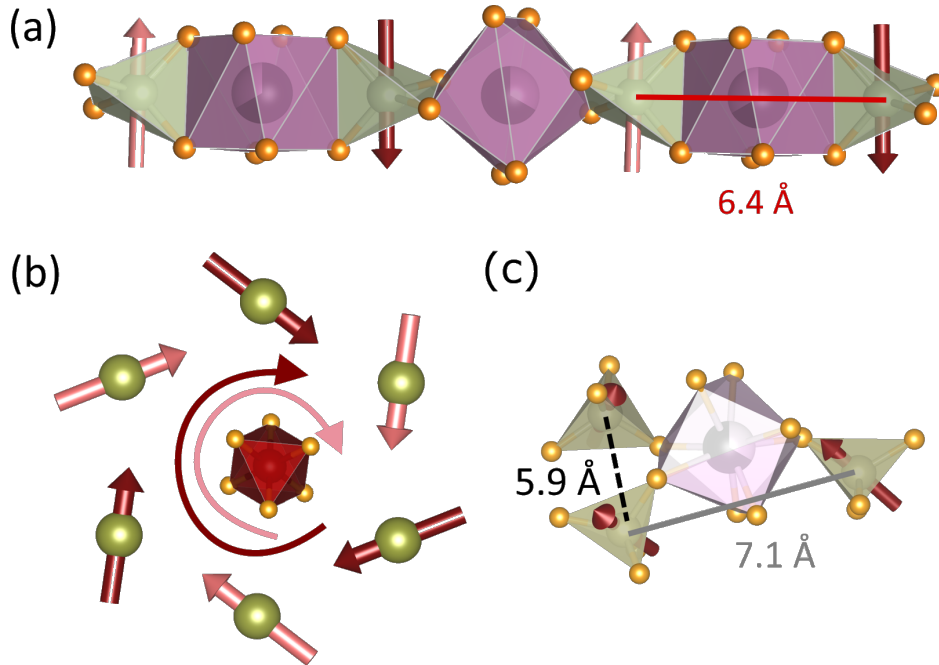


Figure 6: To understand the source of the competing exchange interactions, the intrarod interactions are plotted where (a) the two sets of tetrahedra from different rods are antiferromagnetic to each other. (b) Looking along the rod, the sets of tetrahedra on opposite faces of the dodecahedra are ferromagnetic to each other. (c) The tetrahedra are edge-sharing with dodecahedra between different rods and corner-sharing with dodecahedra along the same rod. Iron to iron distances are shown.

Below the ordering temperature, the moments are consistently larger in the La-based composition, which we attribute to higher covalent character of La versus that of Y. In an 8-coordinate environment, lanthanum (III) and yttrium (III) have ionic radii of 1.160 Å and 1.019 Å respectively. The smaller radius of yttrium is sufficient, even at only one third occupancy of the cubic site, to cause the unit cell to decrease from 12.81870(1) Å to 12.529387(2) Å (at 295 K from synchrotron X-ray powder diffraction) which increases

the Zr–O bond lengths in the octahedra from 2.059(1) Å to 2.068(4) Å. Similarly, the Fe–O bonds in the tetrahedra increase from 1.869(1) Å to 1.898(4) Å, yet this is offset by a contraction of the cubic metal-oxygen bond lengths from 2.455(4) Å to 2.381(1) Å. Thus, $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ contains longer tetrahedral and octahedral metal-oxygen bonds indicating higher covalency for the lanthanum cation over that of the yttrium cation.

The octahedral sites are commonly believed to have the largest influence on the magnetic coupling within the garnet structure; however, in this instance, the cubic site appears to play a more considerable role. This is best seen by examining the coupling between the tetrahedral sites as illustrated in Figure 6 (a), which shows the seemingly complex non-collinear magnetic structure can be viewed more simply as an antiferromagnetic coupling across the shared edges of the cubic and tetrahedral sites. While this is slightly surprising given that these neighboring spins correspond to the second-nearest-neighboring pairs of spin, there are many more degenerate pathways through which the moments can interact through the shared edges of the polyhedra compared to the corner-sharing nature of the nearest neighbors. Figure 6 (b) and (c) further show that two ferromagnetic sublattices of spins are present (illustrated as pink and dark red) and couple antiferromagnetically to each other to form a spiral revolving around the octahedral chains. So, while the unit cell of $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ may be larger, the shorter bond lengths in the tetrahedra produce stronger superexchange pathways, which makes the ordering temperature slightly higher than that of $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ due to the improved covalent character from the enhanced orbital overlap.

To further understand the magnetic order in these materials, specific heat measurements were performed from 2 to 200 K. As shown in SI Figure S2, both specific heat measurements exhibit a sharp asymmetric lambda-like anomaly at the respective magnetic ordering temperatures, which is a common indication of a second order phase transition and suggests a long-range collective magnetic transition. Yet, the absence of a similar feature near the temperatures corresponding to the broad feature in the magnetic susceptibility suggests a less collective short-range change in the ordering of the spins. AC magnetic susceptibility measurements were, therefore, used to explore the possibility of short-range ordering or glassy features at various AC frequencies, shown in SI Figure S4. Two maxima occur at the same temperatures as those in the DC susceptibility and show no frequency dependence, which seems to rule out the presence of glassy domains in the material. We, therefore, tentatively attribute the broad feature in the susceptibility, the diffuse scattering in the neutron powder diffraction, and the deviation between the zero-field-cooled and field cooled data to a small an uncompensated moment associated with the short-range magnetic correlations.

To better understand the nature of these short range magnetic correlations, the diffuse magnetic scattering data for $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ at 18 K, where the diffuse scattering was strongest, was fitted using SPINVERT

with consistent results obtained across a large number of refinements with a typical fit of χ^2 of 13.5 as seen in Figure 7. Stereographic projections of the refined spin orientations, both from individual refinements and averaged out over all refinements, were examined and did not show any indication of preferential alignment within the unit cell. To confirm this, refinements were carried out in which the spins were, artificially, constrained to be oriented along the [100], [110] and [111] directions. No significant deterioration in the fits was observed, which suggests that the data obtained is insensitive to absolute orientation of the spins with respect to the crystallographic axes.

If, as is typically the case in metal oxides, the separation between Fe atoms is sufficient that magnetic interactions must be facilitated by superexchange examination of the crystal structure reveals that this must occur via five atom superexchange bridges. For the nearest neighbors and closest three Fe – Fe neighbors with antiferromagnetic interactions coupling is possible through a combination of Fe – O – Zr – O – Fe and Fe – O – Ca/Y – O – Fe pathways, although the latter should presumably be more significant due to the greater radial extension of the Zr *4d* orbitals. It should also be noted at this point that the Fe cations separated by ≈ 7.4 Å lack any direct links through the zirconium octahedra, which may explain its weaker antiferromagnetic correlations. The complex nature of these superexchange pathways makes it difficult to understand why the nearest neighbors and other significant correlations have opposite signs.

Comparison of the correlations obtained from the paramagnetic phase and the ordered antiferromagnetic structure provides a likely explanation for the non-collinear spins in the order structure and the role this plays in reducing the magnetic frustration in this structure. Comparing the distances, for which there are likely superexchange pathways in terms of increasing distance, we will start with the nearest neighbors. Here examination of the Fe sites in the ordered structure shows that the spins for all sites have angles of less than 90° with at least three of the neighboring spins and the average of all of these angles with their four neighbors less than 90° . In contrast, for the spins of the Fe atoms separated by ≈ 5.9 Å from each other in the ordered structure neighboring spins all have greater than a 90° angle from each other but are typically far from the 180° expected of purely antiferromagnetic correlations. For the Fe–Fe atoms separated by ≈ 6.4 Å, where the refined antiferromagnetic correlations are the strongest, there are only very small canting angles that prevent spins from being antiferromagnetically coupled to each other. Finally, for Fe cations separated by ≈ 7.4 Å which have the weakest of the significant antiferromagnetic correlations in the paramagnetic phase, the spins on each Fe site have an angle of less than 90° with at least three of their four neighbors and the average of all of these angles with their four neighbors are less than 90° . Thus it appears that for the three Fe–Fe distances for which significant correlations are observed in the paramagnetic phase it appears that, on average, the ordered phase satisfies the sign of the correlation expected from the

paramagnetic phase. For Fe cations for which significant magnetic correlations can be identified as arising from a superexchange pathway this pattern breaks down only for Fe-Fe distances of $\approx 7.4 \text{ \AA}$ but this is consistent with their weaker antiferromagnetic correlations in the paramagnetic phase, likely a result of the lack of Fe-O-Zr-O-Fe superexchange pathways. This suggests the highly canted structure plays a key role in satisfying the magnetic correlations expected from the paramagnetic phase.

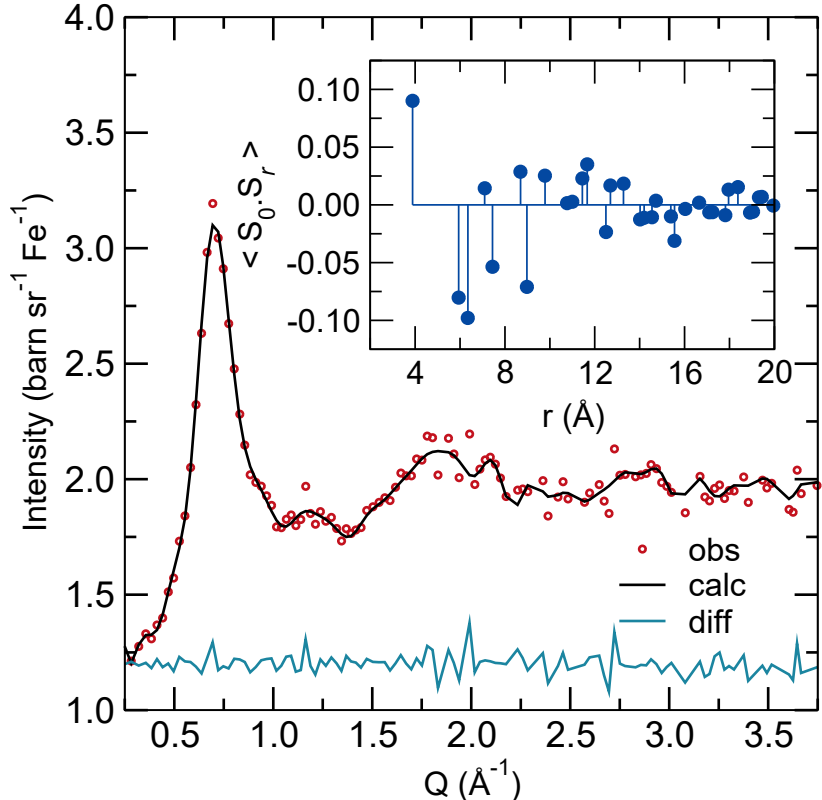


Figure 7: Results from the RMC fitting of the diffuse scattering, using Heisenberg-like spins, of $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ measured at 18 K. Data is shown in red, fit in black, and the difference in blue. (inset) Spin correlation $\langle S_0 \cdot S_r \rangle$ versus r from RMC fits to the diffuse magnetic scattering of $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$, averaged over 300 refinements. Errors in the values are smaller than the circular markers.

From these fits, the nearest-neighbor correlation is found to be ferromagnetic and all other significant magnetic correlations, that are between atoms separated by less than 10 \AA , are antiferromagnetic as seen in the inset of Figure 7. A number of weak ferromagnetic correlations between atoms separated by 5-12 \AA distances also exist, but these all appear to be associated with cations connected to each other through a sequence of nearest neighbor distances and are therefore likely a result of the ferromagnetic nearest neighbor correlations. Comparing the correlations in this paramagnetic phase with the ordered antiferromagnetic structure suggests that the nearest neighbor ferromagnetic interaction competes, and ultimately loses out, to the second nearest neighbor antiferromagnetic coupling due to the higher degeneracy of the coupling through

the cubic site.

Taken as a whole, the 120° antiferromagnetic ground state we have determined is fully consistent with prior studies on garnets with magnetism isolated to the tetrahedral sublattice.²⁷ Upon removing magnetic cations from the octahedral sublattice, the moments on the tetrahedral sites cant away from the (111) axis of the cubic structure and instead orient antiparallel across the shared edge of the cubic sites, much like what Geller and coworkers proposed¹⁶ and what Dodokin *et al.* observed using Mössbauer spectroscopy.¹⁵ Indeed, we even observe the short-range canting of the moments predicted through theoretical calculations by Rosencwaig²⁸ and Smirnov.²⁹ It is particularly interesting to recognize that our results suggest that the origin of the 120° orientation of the spins derives from antiferromagnetic coupling through the cubic site. These findings shed new light on the magnetic coupling between neighboring tetrahedra and how the cubic and octahedral sites mediate such interactions.

Summary

The magnetic structures of $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ have been determined using powder neutron diffraction and symmetry analysis, which reveals the co-existence of both long- and short-range magnetic order. Both compositions order in a non-collinear fashion at 18 K and 21 K for $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$ and $\text{Ca}_2\text{LaZr}_2\text{Fe}_3\text{O}_{12}$ respectively, with the minor change in the ordering temperatures attributed to the smaller tetrahedral sites in the Y vs. the La phase. Most importantly, this work highlights the impact of the cubic site in mediating magnetic interactions between neighboring tetrahedral sites, which is frequently overlooked.

Acknowledgments

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Supporting Information

Table S1, magnetization vector components; Tables S2 and 3, Rietveld refinement results of the powder neutron diffraction data for both materials; Figure S1, figures of Rietveld refinements; Figure S2, specific heat of each respective material; Figure S3, isothermal M-H measurements of each respective material; Figure S4, alternating current magnetic susceptibility at multiple frequencies; Figure S5, the diffuse scattering peaks in neutron powder diffraction at low two-theta; Figure S6, illustrations of the respective magnetic structures.

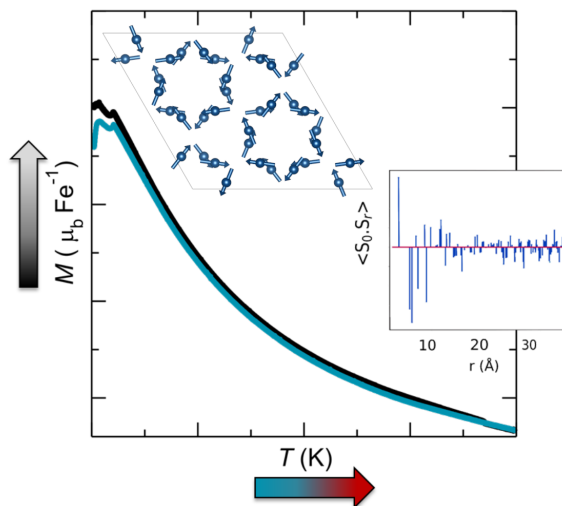
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Synopsis: We report on the temperature- and field-dependent magnetic properties of $\text{Ca}_2\text{YZr}_2\text{Fe}_3\text{O}_{12}$. By isolating the paramagnetic ions to the tetrahedral sublattice of the garnet structure, we find the material adopts a complex 120° magnetic structure that suggests a strong coupling of the moments mediated by the 8-coordinate cubic site.