

# Measurement of Velocity and Concentration Profiles of Pneumatically Conveyed Particles in a Square-Shaped Pipe Using Electrostatic Sensor Arrays

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## Abstract

Cross-sectional measurement of particle velocity and concentration in a pneumatic conveying pipe is desirable for the characterisation of particle flow dynamics and determination of particle mass flow rate. In this study, an inner-inserted electrostatic sensor array consisting of nine pairs of electrodes is implemented to measure the cross-sectional velocity and concentration profiling of particles over the whole cross section in a square-shaped pipe. Experimental tests were conducted on both vertical and horizontal pipe sections on a test rig under dilute conditions with different air velocities and particle mass flow rates. Test results show that the slope-shaped particle concentration profile changes to an arch-shaped one when the particles flow from a horizontal pipe to a vertical one. The particle velocity profile is arch-shaped in both vertical and horizontal pipes. A comparative study of cross-sectional mean particle velocity and concentration measured by the developed electrostatic sensor arrays is conducted.

**Keyword:** *Flow profile; dilute gas–solid two-phase flow; electrostatic sensor array; square-shaped pipe; pneumatic conveying; flow measurement*

## 1. Introduction

On-line flow measurement of pneumatically conveyed particles in a square-shaped pipe is indispensable for the optimal control of industrial processes, enhancing productivity and reducing energy consumption [1]. The flow profile of solid particles in a dilute gas–solid transport pipe can be highly inhomogeneous depending upon the pipe orientation, measurement position, phase loading ratio, conveying air velocity and properties of the particles. In consequence, incorrect quantification of the volumetric concentration, velocity and mass flow rate of conveyed particles may be obtained using most of the available measurement and numerical methods [1]. Therefore, measurement of the cross-sectional distribution of particle concentration and velocity is desirable for the characterisation of the dynamics of pneumatically conveyed particles.

40 Due to the advantages of simple manufacturing and easy installation, square-shaped pipes are commonly  
41 used for conveying particles in industrial processes, such as circulating fluidised beds [2], and thermal power  
42 plants in Germany, China and some eastern European countries [3], flue gas transportation systems and for  
43 ventilation in buildings. However, research on the modelling and measurement of dilute phase particle flow  
44 profile within square-shaped pneumatic pipes is rarely conducted in the past [4–7]. Most of the modelling  
45 research [4] was performed under various flow conditions on key flow phenomena. Some factors were not  
46 considered during modelling due to the limited understanding of mutual couplings between the gas and solid  
47 phases, such as carrier fluid turbulence modulation, gas–particle interactions, the relationship between the  
48 electrostatic force of particles and the air drag force etc. [8, 9]. Experimental research is not only able to  
49 obtain key parameters of particle flow under a variety of controllable flow conditions, but also provides  
50 actual boundary conditions for simulation study and useful information for validation of established models.  
51 However, most of the experimental research focused on the particles in circular-shaped pipes instead of the  
52 square-shaped ones. Besides, particle image velocimetry (PIV), phase-Doppler anemometry (PDA), fibre  
53 optic probe techniques, ray computed tomography, electrical capacitance tomography (ECT), microwave,  
54 acoustic and radioactive attenuation techniques have their limitations in the measurement of particle flow  
55 profile [1, 10–15].

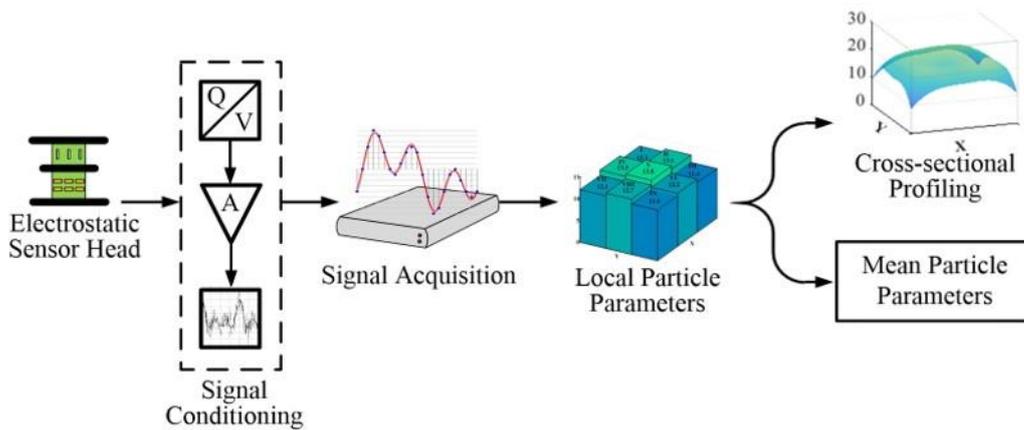
56 In recent years, substantial efforts have been made to develop electrostatic techniques for the characterisation  
57 of particles in pneumatic pipes due to its advantages over other methods, including structural simplicity,  
58 robustness, low cost, etc. [6, 13, 16–19]. Whereas, little research has been conducted on the flow profiling of  
59 particles in square-shaped pipes [5]. Particle flow regimes [20] and electric field distribution of charged  
60 particles [7] in a square-shape pipe are more complex than those in a circular-shaped pipe. As the cross  
61 section of a square-shaped pipe is not centrosymmetric and has four right angles, small flow turbulence  
62 exists in the corner areas and particle distribution in the pipe cross section is very different from that of a  
63 ring-shaped pipe (especially the area near the pipe walls). A mathematical model of a square-shaped  
64 electrode was developed and its characteristics, including sensitivity distribution and frequency response,  
65 were theoretically analysed and experimentally verified by Murnane et al. [21] and Peng et al. [7]. The  
66 physical models of an intrusive rod electrode and distributed rod electrode for a large diameter rectangular  
67 pipe at the outlet of a coal mill were proposed by Jurjevčič et al. [3]. Mathematical modelling and  
68 experimental tests of non-intrusive strip-shaped electrostatic sensor arrays, which are uniformly embedded in  
69 the four pipe walls, for the measurement of pulverised fuel flow in a square-shaped pipe were conducted by  
70 Zhang et al. [6]. The experimental results have shown that the velocity profiles of air and particles over the  
71 whole cross-section of the pipe are similar and relatively non-uniform. However, parameters of particles in  
72 the centre of the pipe are deduced from those near the pipe walls. A large eddy simulation in a large range of  
73 high Reynolds numbers was conducted by Adams et al. [20] and its result demonstrates that the dynamic  
74 characteristics of particles close to the four sharp corners of the pipe are more complex than those in circular  
75 pipes. Therefore, an electrostatic sensing system that is capable of measuring the particle velocity and  
76 volumetric concentration profiles over the whole pipe cross section is desirable for the quantitative  
77 characterisation of pneumatically conveyed particles.

78 In this study, a sensor array composed of nine pairs of electrostatic electrodes is designed and implemented  
 79 for measuring the volumetric concentration and velocity profiles of pneumatically conveyed particles in a  
 80 square-shaped pipe. Experimental tests using plain flour as conveying material were conducted under various  
 81 dilute phase flow conditions with combinations of different air velocities and mass flow rates. Concentration  
 82 and velocity profiles of particles over a pipe cross section are obtained using localised particle flow  
 83 parameters measured from the developed sensor array and a non-intrusive sensor array proposed by Zhang et  
 84 al. [6]. A study on the mean volumetric concentration and velocity of particles over the whole cross section  
 85 measured by these two different sensor arrays is also conducted.

## 86 2. Measurement principle and system design

### 87 2.1. Overall measurement strategy

88 The schematic block diagram of the measurement principles of the proposed electrostatic system is shown in  
 89 Fig. 1. Particles are electrostatically charged when flowing through a pipe due to the collisions between  
 90 particles, impacts between particles and pipe walls, and friction between particles and air. An electrostatic  
 91 sensor head is embedded into the pipe of a gas–solid two-phase flow test rig to measure the electrostatic  
 92 signals of pneumatically conveyed particles. The electric current signals from the electrostatic sensor arrays  
 93 that embedded in the sensor head are converted into voltage signals and then amplified and filtered by a  
 94 signal conditioning circuit [6, 22]. The filtered signals are sampled by a data acquisition card (DAQ) for the  
 95 calculation of localised volumetric concentration and velocity of particles near the electrode. The signal  
 96 processing algorithms and cross-correlation velocimetry are performed to obtain the local concentration and  
 97 velocity of particles, respectively. The cross-sectional profiles (section 2.3) and cross-sectional mean particle  
 98 concentration and velocity (section 2.4) are then obtained using the localised particle parameters.

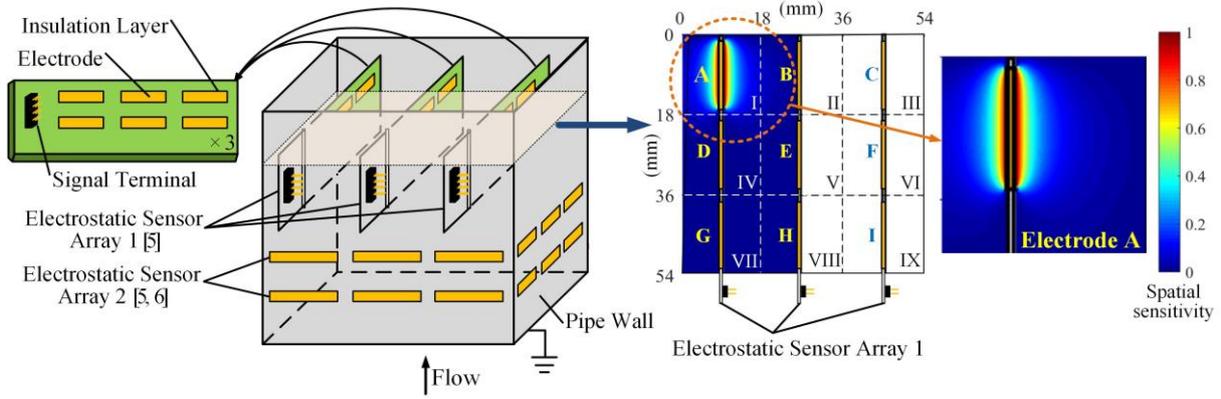


99  
100 **Fig. 1.** Block diagram of the measurement system.

### 101 2.2. Design and implementation of electrostatic sensor head

102 Fig. 2 shows the structure of the proposed electrostatic sensor array (namely electrostatic sensor array 1) and  
 103 the non-intrusive electrostatic sensor array designed by Zhang et al. [6] (namely electrostatic sensor array 2).  
 104 Electrostatic sensor array 1 consists of nine pairs of strip-shaped electrostatic electrodes, which are inserted  
 105 into the square-shaped pipe with an identical spacing in between. The surface of sensor array 1 (facing the  
 106 flow) is made in the form of a knife-edge to minimise the flow disturbance. Electrostatic sensor array 2,

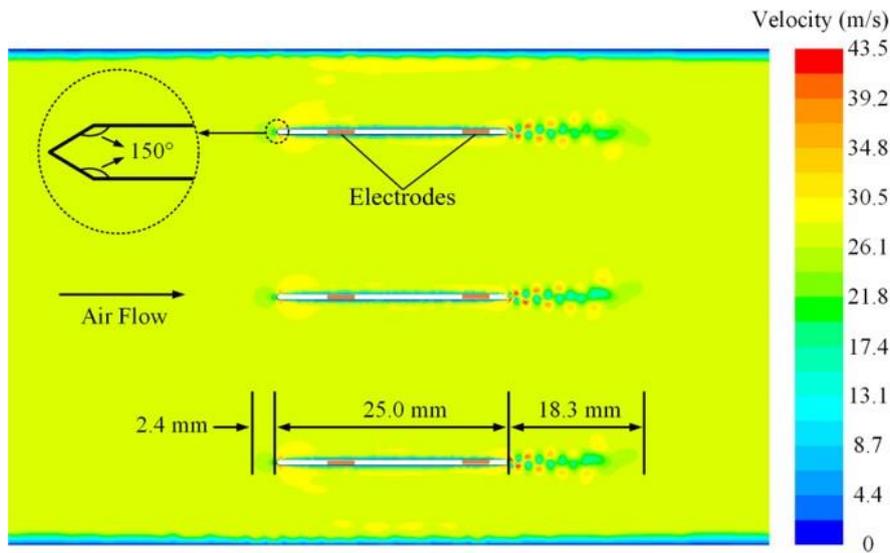
107 which consists of  $3 \times 4$  pairs of strip-shaped electrostatic electrodes that are uniformly embedded in the four  
 108 flat pipe walls, is placed upstream of sensor array 1 to avoid the fluid disturbance caused by sensor array 1.  
 109 Each electrode in the two sensor arrays has the same length and width, and the electrode spacing of each  
 110 electrode pair is identical as well.



111  
 112 **Fig. 2.** Structure of the sensor head [5] and sensitivity distribution of electrostatic sensor array 1.

113 In order to determine the sensing characteristics of the sensor arrays, the spatial sensitivity of an individual  
 114 strip-shaped electrode (marked as electrode A) within electrostatic sensor array 1 is simulated using the in-  
 115 house software based on the finite element method (FEM) under the COMSOL Multiphysics environment.  
 116 The simulation is validated using an analytical mathematical model (based on the theory of electrostatics and  
 117 the method of images) proposed by Zhang et al. [6]. According to the dimensions of the sensor head used in  
 118 the experimental work, the dimensions of the electrode (made of copper) used in the simulation has a length  
 119 of 15 mm and a width of 3 mm, and the side-length of the pipe is set as 54 mm. The boundary conditions are  
 120 set to ground for the electrode and zero charge for the outer surface of the model domain. As shown in Fig. 2,  
 121 the sensitivity distribution of all electrodes of sensor array 1 can be derived by duplicate the sensitivity area  
 122 of electrode A to other electrodes without regard to the interference between the adjacent electrodes as they  
 123 are isolated by a grounding layer. As can be seen from Fig. 2, the sensitivity of the stripe-shaped electrode is  
 124 not linear with the distance between the particles and the electrode. Electrostatic sensor array 1 is suitable for  
 125 measured localised particle parameters as the strip-shaped electrode is more sensitive to its surrounding area.  
 126 Because the strip-shaped electrode senses the particles on both of its left and right sides, it provides larger  
 127 sensing volume and more uniform sensitivity than the similar electrodes used in reference [5]. Based upon  
 128 the sensing area of each electrode, the square-shaped cross section is uniformly divided into nine  
 129 measurement zones, i.e. Zones I, II, ..., IX, as shown in Fig. 2, and one pair of electrodes are placed in the  
 130 symmetry axis of each zone. The number of electrodes is a trade-off between the intrusive effect of the  
 131 electrodes and the spatial resolution of the sensor. Because if this number is too large, a more detailed  
 132 measurement of local particle parameters can be obtained, while the movement of the particle flows in the  
 133 pipe will be hindered by the intrusive electrodes. Besides, a powerful computer with high calculation speed  
 134 is required due to heavy computation. On the contrary, if the number is too small, the profiles of particle  
 135 flow parameters cannot be obtained with sufficient details and the mean particle concentration and velocity  
 136 cannot be calculated using less localised particle parameters measured over the pipe cross section.

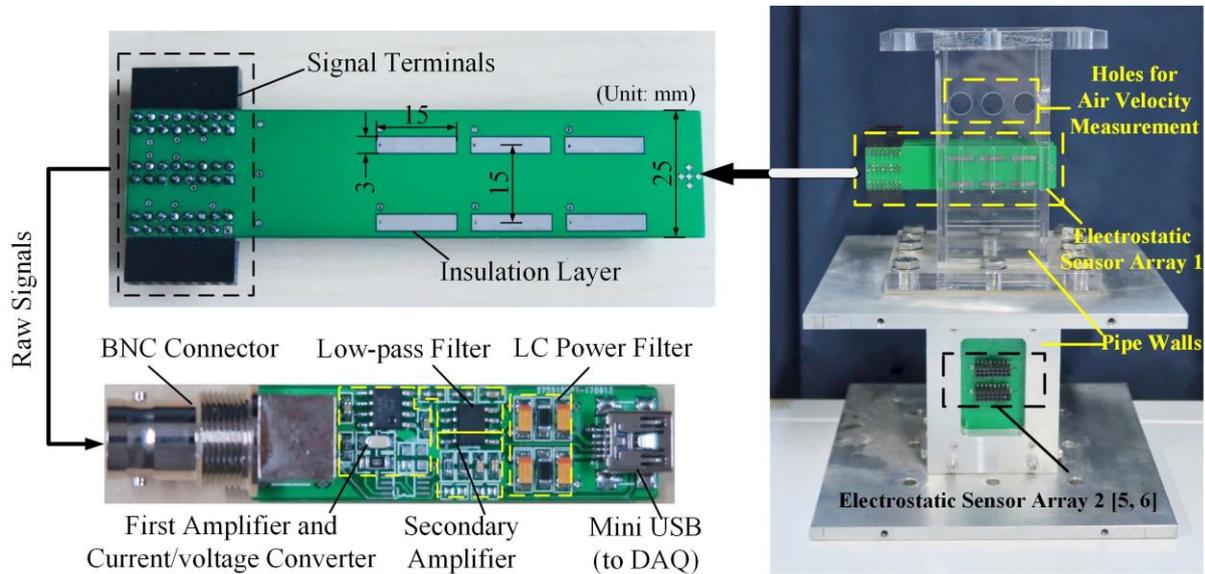
137 The degree of the intrusiveness of electrostatic sensor array 1 depends mainly on the sensor configuration,  
 138 such as the dimensions and spacing of the electrodes. To mitigate the intrusive effect of electrostatic sensor  
 139 array 1 on pneumatically conveyed particles, the thickness of the sensor array is made to be 0.6 mm in the  
 140 experiment so that only 3.3% of the pipe cross section is occupied by the sensor array. Furthermore, the  
 141 wind-facing side of the sensor array is made as a sharp corner of  $60^\circ$  to weaken the flow turbulence and  
 142 vortex caused by the blockage and to minimise the chance of collision with particles. As the volumetric  
 143 concentration of particles is normally as low as 0.1% in fully suspension conditions, only a tiny proportion of  
 144 particles will collide with the electrodes. Therefore, minimum effect on the movement behaviours of  
 145 particles can be achieved by the sensor design and the moving trajectory of most particles still follows the  
 146 conveying air. As can be seen from Fig. 3, the insertion of sensor array 1 has limited effect on the air flow  
 147 field in the sensing area of the electrodes. As the air velocity in wind-facing area (green and yellow coloured  
 148 area) of the sensor array is a bit lower than the preset air velocity (27 m/s), the upstream electrode is located  
 149 about 6 mm from the sensor edge to avoid the flow turbulence. A few small eddy currents only appear in the  
 150 downstream area of the sensor array, therefore, have very limited effects on the air velocity near the  
 151 downstream electrode.



152  
 153 **Fig. 3.** Velocity distribution of air flow with the presence of electrostatic sensor array 1.

154 Fig. 4 shows the implemented electrostatic sensor head consisting of the electrostatic sensor arrays 1 and 2  
 155 according to the design presented in section 2. Sensor array 1 is located about 10 cm downstream to sensor  
 156 array 2 and inserted into the square-shaped pipe through three rectangular grooves on one side of the pipe  
 157 wall to obtain local particle flow information directly. Polymethyl methacrylate is utilised as the main body  
 158 of sensor array 1 due to the advantage of easy machining. The whole sensor head is covered by a grounded  
 159 shielding case to isolate both sensor arrays from external electromagnetic interference. As can be seen from  
 160 Fig. 4, three holes on the upper side of the grooves are used for inserting a hot-wire anemometer (Model  
 161 MP210, KIMO, France) to measure air velocity prior to each particle flow test. The pure air velocities in the  
 162 nine zones of the pipe cross section are measured for the purpose of comparison with those in the presence of  
 163 particles. The twelve pairs of strip-shaped electrostatic electrodes within sensor array 2 are uniformly

164 embedded in the four flat pipe walls to obtain local particle flow information using the weighting method  
 165 presented by Zhang et al. [6]. As shown in Fig. 4, nine pairs of strip-shaped electrodes embedded in three  
 166 identical printed circuit boards (PCBs) are inserted to the square-shaped pipe. Each electrode (silver coloured)  
 167 has a length of 15 mm and a width of 3 mm, and the spacings between two lateral electrodes are 18 mm and  
 168 15 mm, respectively. All the electrodes are physically separated from each other using a very thin insulation  
 169 layer and electrically isolated by a grounded metal layer (green area). The signal from an electrostatic  
 170 electrode is amplified and filtered before being sampled for flow parameter calculation since the raw signal  
 171 is very weak and can be easily distorted by environmental interferes. Fig. 4 also shows the signal  
 172 conditioning circuit board consisting of three modules, i.e. power supply voltage regulation, signal  
 173 amplification, and signal filtering modules. The cut-off frequency of the low-pass filter circuit is set to about  
 174 16 kHz to retain the useful signal. A grounding shield is utilised to prevent the measured signal from external  
 175 environmental interference by covering the electronic components on the signal conditioning circuit board.  
 176 The Bayonet Nut Connector (BNC) and mini USB connectors are used for the connection to an electrode and  
 177 the conditioned signal transmission to the signal acquisition unit, respectively.



178  
 179

**Fig. 4.** Implementation of the sensor head and signal conditioning circuit board.

### 180 2.3. Cross-sectional profiling of particles

181 The signals from the electrodes mounted inside the pipe contain dynamic information of local particles.  
 182 Sensing Zones I, II, ..., IX in Fig. 2 are represented by  $i = 1, 2, \dots, 9$ , respectively. The relative volumetric  
 183 concentration of local particles ( $\beta_i$ , hereafter referred to as particle concentration) in one zone is represented  
 184 by the root-mean-square (RMS) value of measured electrostatic signals ( $A_{RMS}$ ) [3, 6, 13, 18, 20–24] and  
 185 local particle velocity ( $v_i$ ) is calculated through cross-correlation velocimetry [6, 7, 13, 17, 18, 19, 22, 25].  
 186 According to the spatial sensitivity distributions of both electrostatic sensor arrays 1 and 2, the electrostatic  
 187 signals from sensor array 1 contain information about the particles over the whole pipe cross section, while  
 188 those from sensor array 2 contain information about the particle flow near the pipe walls [6]. In order to  
 189 obtain an in-depth understanding of the particle flow dynamics over the pipe cross section, the relative

190 concentration and velocity profiles of particle flow are obtained using the biharmonic spline interpolation  
 191 method [26, 27] other than a simple combination of the particle parameters measured in each of the nine  
 192 zones [5]. Biharmonic spline interpolation, also known as biharmonic spline filtering, is a solution to the  
 193 biharmonic equation based on the Green's function [26–28], which is initially developed to solve elasticity  
 194 problems, such as calculate the elastic force distribution of a curved stretchable surface based on the mean  
 195 elastic forces of several discrete small areas. Obtained data points are smoothly connected in this way, which  
 196 illustrated that this method is superior to other interpolation methods, such as linear method, cubic method,  
 197 nearest neighbour method etc. In this study, the pipe cross section is divided into a number of small areas and  
 198 the volumetric concentration and velocity of particles in several specific areas can be measured with both  
 199 sensor arrays. All the particles are subjected to the resultant force due to air drag, gravity, etc. Therefore, the  
 200 concentration and velocity distribution of particles in the pipe cross section can be obtained using biharmonic  
 201 spline interpolation method. The values of measured parameters of local particles (located at  $x_1, x_2, \dots, x_N$ )  
 202 using all the electrostatic sensors over the cross section (with the number of  $N$ ) are  $\alpha(x_1), \alpha(x_2), \dots, \alpha(x_N)$ ,  
 203 respectively. The position of one small area ( $x$ ) and the displacement of the interpolation surface at  $x$  ( $\alpha(x)$ )  
 204 satisfy biharmonic equation [26]:

$$205 \quad \nabla^4 \alpha(x) = \sum_{j=1}^N \omega_j \delta(x - x_j) \quad (1)$$

206 where  $\nabla^4$  is the Biharmonic operator,  $\delta(x)$  is Delta Function,  $j$  is the serial numbers of the measuring points  
 207 ( $j=1, 2, \dots, N$ ) and  $\omega_j$  is a weighting coefficient to represent the magnitude of the resultant force. The  
 208 particular solution to Eq. (1) can be expressed as the following linear combination of 2-dimensional Green's  
 209 functions ( $g_2(x-x_j)$ ):

$$210 \quad \alpha(x) = \sum_{j=1}^N \omega_j g_2(x - x_j) \quad (2)$$

211 where the weight coefficient ( $\omega_j$ ) can be obtained by solving the following linear equation since  $x_i$  and  $\alpha(x_i)$   
 212 are known ( $i=1, 2, \dots, N$ ):

$$213 \quad \alpha(x_i) = \sum_{j=1}^N \omega_j g_2(x_i - x_j) \quad (3)$$

214 Consequently, the displacement of the interpolation surface ( $\alpha(x)$ ) at each area position ( $x$ ) can be calculated  
 215 using Eq. (2) and the interpolation surface can be plotted.

#### 216 2.4. Cross-sectional mean parameters of particles

217 The mean volumetric concentration ( $\bar{\beta}$ ) and velocity ( $\bar{v}$ ) of particles over the whole pipe cross section are  
 218 also concerned in the characterisation of particle flow. The mean particle parameters and their evaluation  
 219 parameters, i.e. the maximum difference of particle concentrations and velocities and their normalised values,  
 220 are calculated through this approach (using the particle flow parameters from both sensor arrays) to analyse  
 221 the characteristics of particle flows over the whole pipe cross section quantitatively. The mean particle  
 222 concentration can be obtained as follows:

223

$$\bar{\beta} = \frac{S_p}{S} = \frac{\sum_{i=1}^9 \beta_i S_i}{\sum_{i=1}^9 S_i} = \frac{\sum_{i=1}^9 \beta_i}{9} \quad (4)$$

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where  $S_p$  is the total cross-sectional area occupied by the particles,  $S$  is the pipe cross-sectional area and  $S_i$  is the area of one zone over the pipe cross section. Since the particle distribution over the pipe cross section is non-uniform, local particle concentration is employed as a weighting factor in mean particle velocity calculation [25].

228

$$\bar{v} = \frac{q_v}{S_p} = \frac{\sum_{i=1}^9 v_i \beta_i S_i}{\sum_{i=1}^9 \beta_i S_i} = \frac{\sum_{i=1}^9 v_i \beta_i}{\sum_{i=1}^9 \beta_i} \quad (5)$$

229

where  $q_v$  is the volumetric flow rate of particles.

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To characterise the variation range of the particle concentration and velocity profiles, the maximum difference of particle concentrations ( $d_\beta$ ) and velocities ( $d_v$ ) over the whole pipe cross section are calculated through the following equations:

233

$$d_\beta = \max\left(\sum_{i=1}^9 \beta_i\right) - \min\left(\sum_{i=1}^9 \beta_i\right) \quad (6)$$

234

$$d_v = \max\left(\sum_{i=1}^9 v_i\right) - \min\left(\sum_{i=1}^9 v_i\right) \quad (7)$$

235

236

Since  $d_\beta$  and  $d_v$  are concerned with  $\bar{\beta}$  and  $\bar{v}$ , respectively, the normalised maximum difference of particle concentrations ( $D_\beta$ ) and velocities ( $D_v$ ) can be obtained as follows:

237

$$D_\beta = \frac{d_\beta}{\bar{\beta}} \times 100\% \quad (8)$$

238

$$D_v = \frac{d_v}{\bar{v}} \times 100\% \quad (9)$$

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### 3. Experimental results and discussion

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#### 3.1. Test rig and experimental conditions

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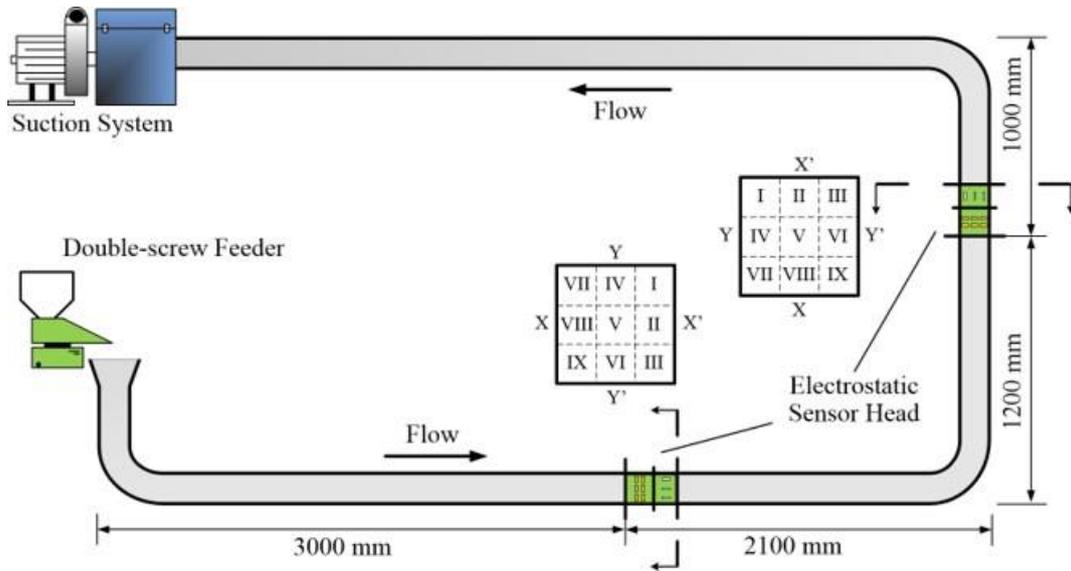
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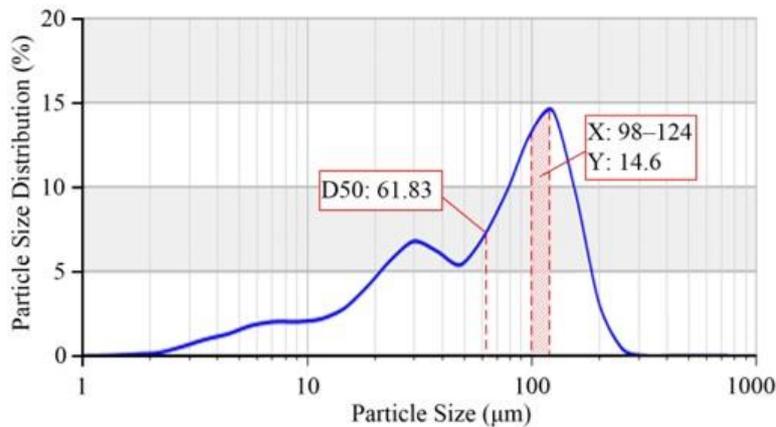
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A laboratory scale carbon steel test rig with a square-shaped pneumatic conveying pipe, as shown in Fig. 5, was used in the experimental tests. The dimension of the inner pipe wall is 54 mm×54 mm. A negative pressure generating device with a receiving hopper for particle recycling is used to create different air velocities for the pneumatic conveying of particles. A double-screw feeder with a programmable controller is employed to provide a stable particle flow rate during each test. The pipe walls close to and far from the readers are marked as sides X and X', respectively. While the pipe walls close to the medial and lateral walls of the right lower bend of the rig are marked as sides Y and Y', respectively. Experimental tests were conducted on vertical and horizontal pipe sections using plain flour as conveying material under the laboratory environment. Plain flour is used as conveying material in the tests because it is a representative of fine particles that widely exist in many industries.



251  
252 **Fig. 5.** Layout of particle flow test rig with a square-shaped pipe.

253 The particle size distribution of plain flour, as shown in Fig. 6, was measured using a laser particle size  
 254 analyser (Model LOP9, OMEC, China). As can be seen from Fig. 6, the median diameter (D50) of plain  
 255 flour used in the tests is 61.83  $\mu\text{m}$  and the most populated particles (14.6 percent, vertical axis Y)  
 256 are within the range from 98 to 124  $\mu\text{m}$  (horizontal axis X). Such parameters are similar to pulverised coal used in coal-  
 257 fired power plants, medicinal powder in the pharmaceutical industry and various chemical compound  
 258 particles in the chemical industry.



259  
260 **Fig. 6.** Particle size distribution of plain flour particles.

261 All the tests were conducted under an air conditioning environment with an ambient temperature of 26.1  $^{\circ}\text{C}$ ,  
 262 the relative humidity of 69% and the ambient PM<sub>2.5</sub> (particulate matter that has a diameter of less than 2.5  
 263  $\mu\text{m}$ ) density of 62  $\mu\text{g}/\text{m}^3$ . As shown in Table 1, experimental tests were conducted under sixteen test  
 264 conditions, i.e. combinations of four air velocities (measured in Zone V) and four mass flow rates. The  
 265 equivalent particle volumetric concentrations under different test conditions were within the range from  
 266 about 0.0012% to 0.0077%. In order to avoid the air velocity drop caused by the negative pressure  
 267 generating device during long operation period, the air velocity in the central zone of the pipe was calibrated  
 268 using the hot-wire anemometer before each test. During each test, the electrostatic signals from both  
 269 electrostatic sensor arrays 1 and 2 were conditioned by the same signal conditioning circuit board

270 aforementioned, sampled synchronously by a data acquisition card (Model USB-6363, National Instruments)  
 271 and then processed by a host computer when the particle flow has reached a relatively stable state.

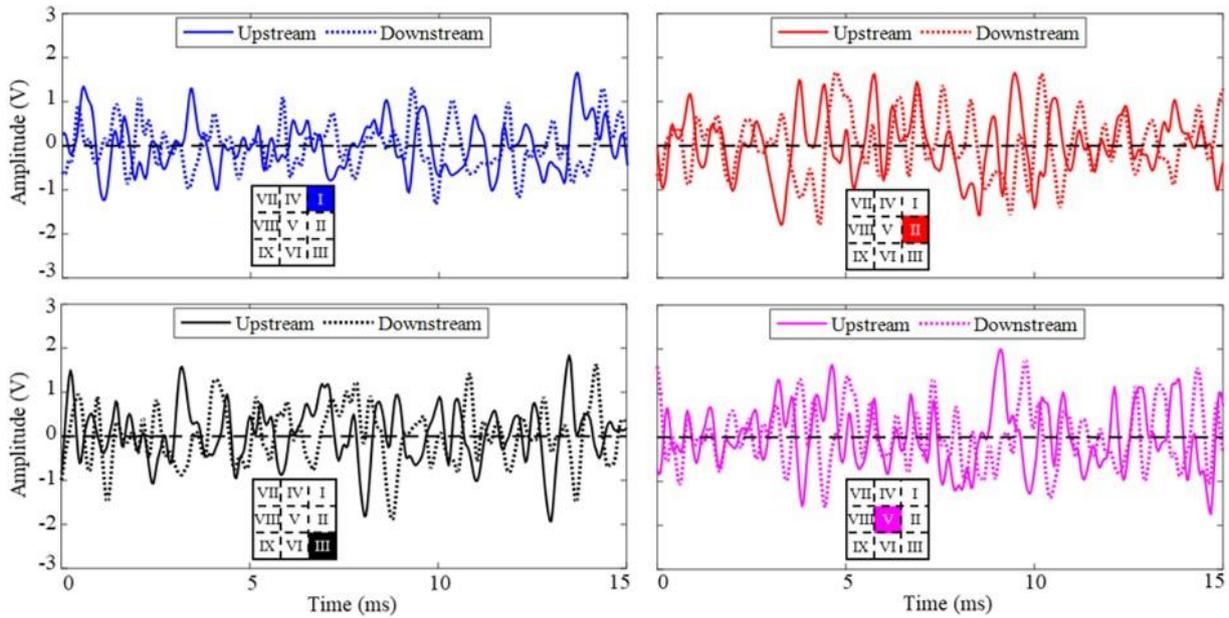
272 **Table 1** Test matrix of plain flour

Mass flow rate (kg/h)	Air velocity (m/s)			
	V1=19	V2=23	V3=27	V4=31
M1=2	V1M1	V2M1	V3M1	V4M1
M2=4	V1M2	V2M2	V3M2	V4M2
M3=6	V1M3	V2M3	V3M3	V4M3
M4=8	V1M4	V2M4	V3M4	V4M4

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 274 The particle flow is regarded as stable when all the pipes are filled with particles, the test rig is running  
 275 normally and the RMS value of measured signal fluctuates in a small range. The signal sampling frequency  
 276 is set at 25 kHz and 2048 data points are used to calculate particle concentration and velocity in each  
 277 measurement cycle. A total of 240 concentration and velocity readings were obtained, at least, from each pair  
 278 of electrodes under each test condition to derive particle flow parameter in each zone.

279 *3.2. Features of electrostatic signals*

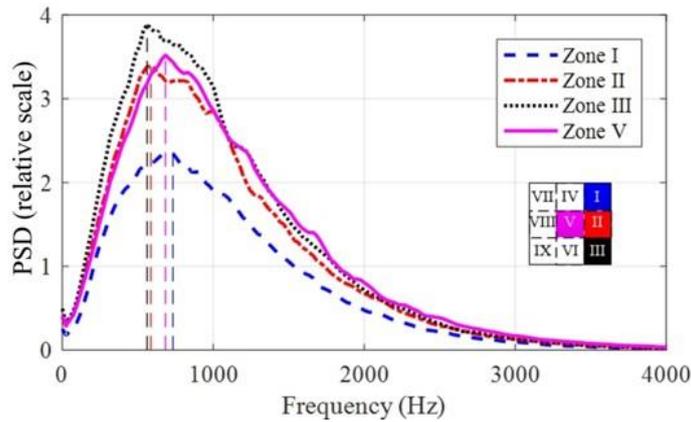
280 The features of the electrostatic signals measured by different electrode pairs reflect the dynamic behaviours  
 281 of particles in the corresponding measurement zones across the whole pipe cross section. The simultaneously  
 282 sampled raw electrostatic signals of particles from the upstream and downstream electrodes in Zones I, II III  
 283 and V of the horizontal pipe under V3=27 m/s, M2=4 kg/h condition are shown in Fig. 7. The mean absolute  
 284 value of the signals measured in the upper corner zone (Zone I) is 0.43, which is the smallest. The mean  
 285 absolute value of the signals in the zone (Zone II) is lower than that in the lowest corner zone (Zone III). In  
 286 addition, the mean absolute value of the signals in the central zone (Zone V) is higher than that in the zone  
 287 with one side pipe wall adjacent at the same height (Zone II). To analyse the raw signals shown in Fig. 7  
 288 further, the corresponding power spectral densities (PSDs) are plotted in Fig. 8 to illustrate the frequency-  
 289 domain features of the signals. As can be seen from Fig. 8, it is evident that the main peak frequencies of the  
 290 electrostatic signals in the four zones vary from 561.5 Hz to 732.4 Hz (illustrated by the vertical dash lines).  
 291 The area surrounded by the PSD curve represents the magnitude of the signal energy, which reflects particle  
 292 concentration, velocity etc. It is noticeable that the signal energy of moving particles in the bottom zone  
 293 (Zone III) is the highest as more particles are transported on the bottom of the pipe due to the gravitational  
 294 effect. On the contrary, the signal energy of particles in the upper corner zone (Zone I) is the lowest, which  
 295 agrees well with the trend in the amplitude of raw electrostatic signals shown in Fig. 7. The signal energy of  
 296 particles in the central zone (Zone V) is slightly higher than that in the adjacent zone because fewer particles  
 297 travel slower in Zone II due to the impact between particles and pipe wall.



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299

**Fig. 7.** Raw electrostatic signals of particles in Zones I, II, III and V of the horizontal pipe.



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**Fig. 8.** PSDs of electrostatic signals of particles in Zones I, II, III and V of the horizontal pipe.

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### 3.3. Cross-sectional profiling of particle concentration and velocity

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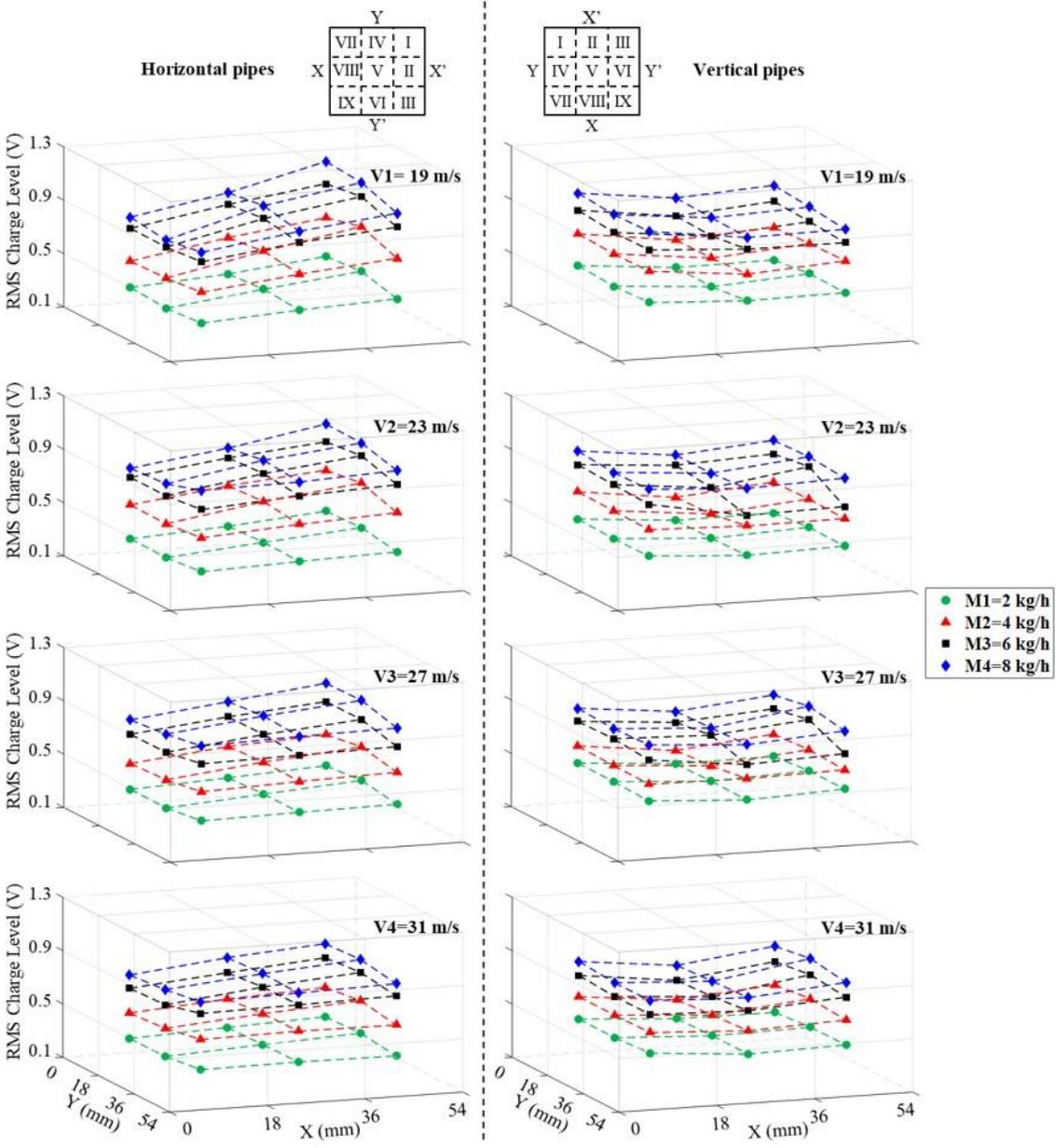
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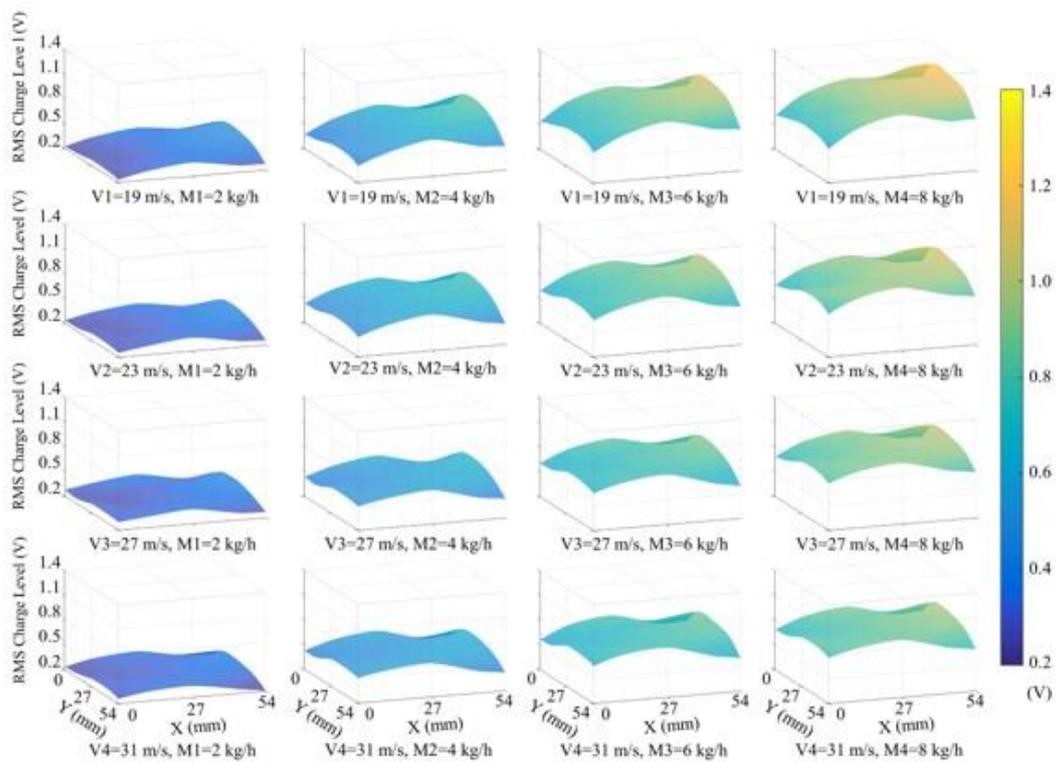
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Fig. 9 shows the RMS charge levels of the electrostatic signals (as an evaluation of particle relative concentration) measured in the cross sections of both horizontal and vertical pipes under all test conditions measured by electrostatic sensor array 1. The cross-sectional concentration profiles of particle flow are obtained using the biharmonic spline interpolation method based on the measurement results from both electrostatic sensor arrays 1 and 2, as shown in Fig. 10. It is clear that the profiles are able to provide qualitative images of the particle concentration in the pipe cross section. As can be seen from Figs. 9 and 10, the RMS charge level of the signal increases with the mass flow rate since more particles are fed into the pipe while the air velocity is unchanged. The RMS charge level decreases slightly with the increasing air velocity when the mass flow rate keeps constant because the particle concentration slightly decreases at a higher air velocity. This result demonstrates that the RMS charge level of the signal is basically unsusceptible to the air velocity, which indicates that the RMS charge level of the signal can be regarded as relative particle concentration in the same flow condition. The concentrations of particles in different zones are non-uniform over the whole pipe cross section. In horizontal pipe sections, more particles are transported at the

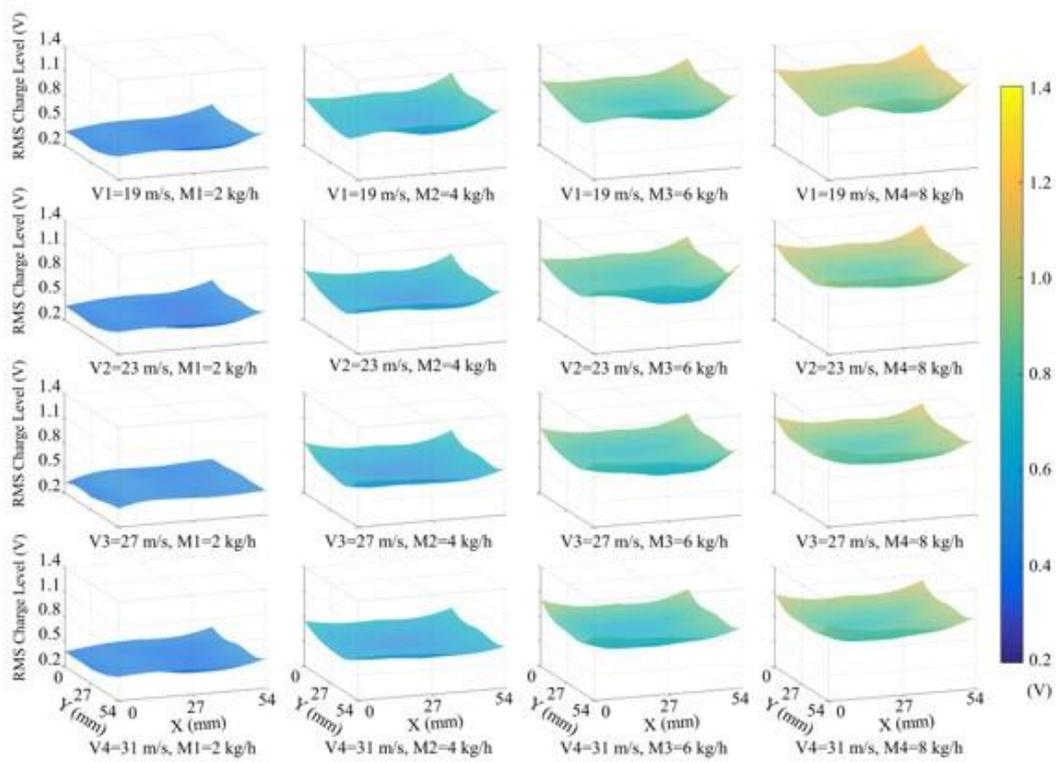
316 bottom of the pipe (Zone III, VI and IX) than those at the top of the pipe (Zones I, IV and VII) mainly due to  
 317 the gravitational effect. Besides, the particle concentration in the central zone (Zone V) is slightly higher  
 318 than the zones of the same height with one side pipe wall adjacent to it (Zones II and VIII), which agrees  
 319 with the trend in Fig. 7 and 8. As shown in Fig. 9, the slopes of three lines that through the points of Zones I,  
 320 II, III, Zones IV, V, VI and Zones VII, VIII, IX decrease as the particle velocity increases. In other words,  
 321 particles concentrations in zones with the same horizontal position and different heights are getting closer at  
 322 a higher particle velocity, which means a more even particle concentration distribution. In vertical pipe  
 323 sections, the particle concentrations in four zones (Zones II, IV, VI, and VIII) adjacent to the central zone are  
 324 lower compared with those in four corner zones (Zones I, III, VII and IX) and the lowest particle  
 325 concentration is measured in the central zone (Zone V). When the particles flow from the horizontal pipe  
 326 section to the vertical pipe section through a bend, the slope-shaped particle concentration profile changes to  
 327 an arch-shaped one.



328  
 329 **Fig. 9.** Particle concentration distribution under different particle mass flow rate and air velocity conditions.



(a)



(b)

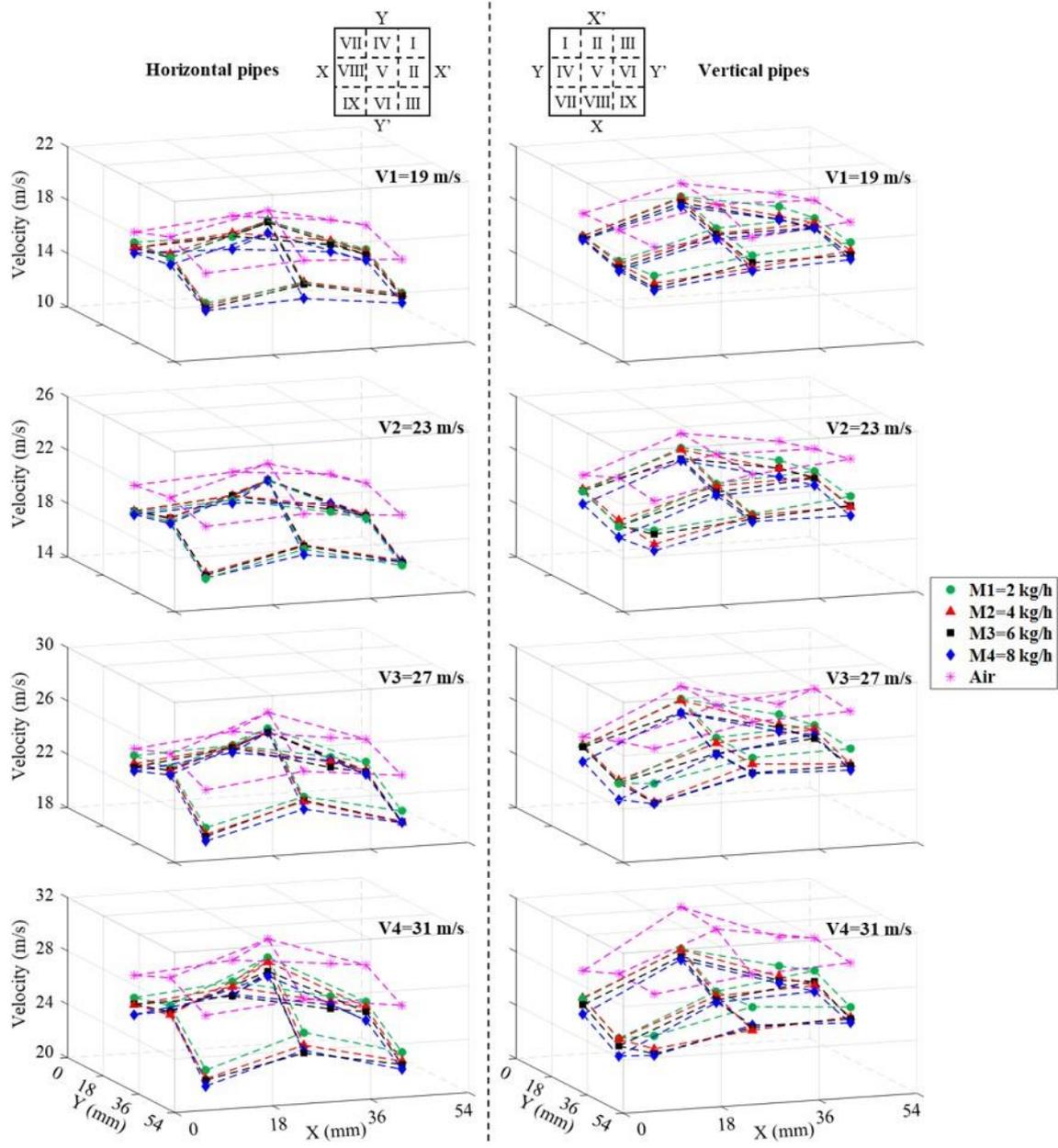
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334 **Fig. 10.** Particle concentration profiles under different particle mass flow rate and air velocity conditions: (a)  
335 horizontal pipe; (b) vertical pipe.

336 The velocity distributions of pure air flow and particles under different test conditions are shown in Fig. 11.  
337 As can be seen from Fig. 11, the velocity distributions of both pure air and particles are not uniform in the  
338 cross sections of horizontal and vertical pipes but have very similar variation trends under different flow

339 conditions. The velocity of the air in the central zone (Zone V) is the highest. The air velocities in the four  
340 zones (Zones II, IV, VI, and VIII) adjacent to the central zone are higher than those in four corner zones  
341 (Zones I, III, VII, and IX). In the horizontal pipe, it is noticeable that the air velocities in the top zones  
342 (Zones I, IV and VII) are similar to those in the bottom zones (Zones III, VI and IX). In the vertical pipe, the  
343 air in three zones close to the pipe wall Y (Zones I, IV, and VII) travel slower than those in three zones close  
344 to the pipe wall Y' (Zones III, VI, and IX). This tendency demonstrates that the velocity distribution of air is  
345 still asymmetric in the measurement pipe section, although the sensor head is placed 20 times of the pipe  
346 inner dimension away from the upstream bend to avoid the effect of the centrifugal force. In general, the  
347 particle velocity distributions under the four different air velocities agree with the trend in air velocity  
348 profiles, but with different distribution compare to the particle concentration distribution. The particle  
349 velocity profiles based on the measurement results from electrostatic sensor arrays 1 and 2 are shown in Fig.  
350 12. As can be seen from Figs. 11 and 12, the particle velocities in all zones increase with the conveying air  
351 velocities correspondingly due to the larger air drag force. When the air velocity remains unchanged, the  
352 velocity difference between the particles and the conveying air (slip velocity) increases with the mass flow  
353 rate because the presence of particles has an obstructive effect on the air flow (Fig. 11). Besides, the slip  
354 velocity in the vertical pipe is higher than that in the horizontal pipe under the same test condition due to  
355 gravity. However, in horizontal pipe sections, the velocities of the particles in the top zones (Zones I, IV and  
356 VII) are higher than those in the bottom zones (Zones III, VI and IX), which is inconsistent with the air  
357 velocity distribution (Fig. 11). Due to more particles need to be conveyed in the bottom zones because of  
358 gravity, the viscous force applied to the air flows is stronger, and hence, particle velocities in the bottom  
359 zones is lower.

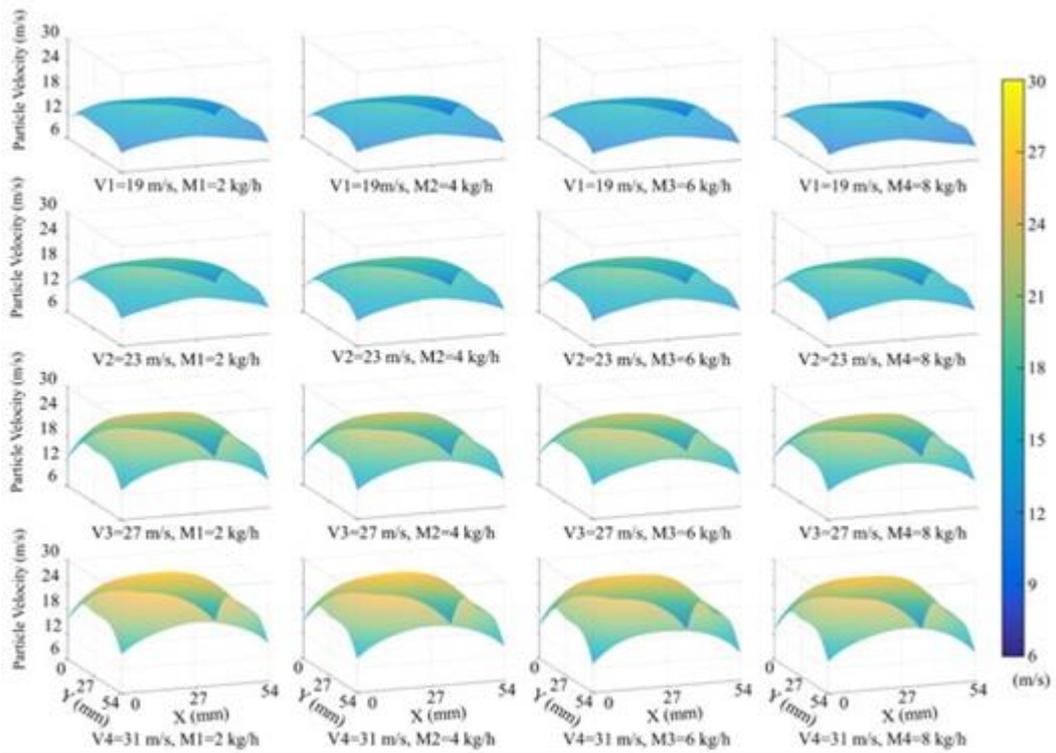


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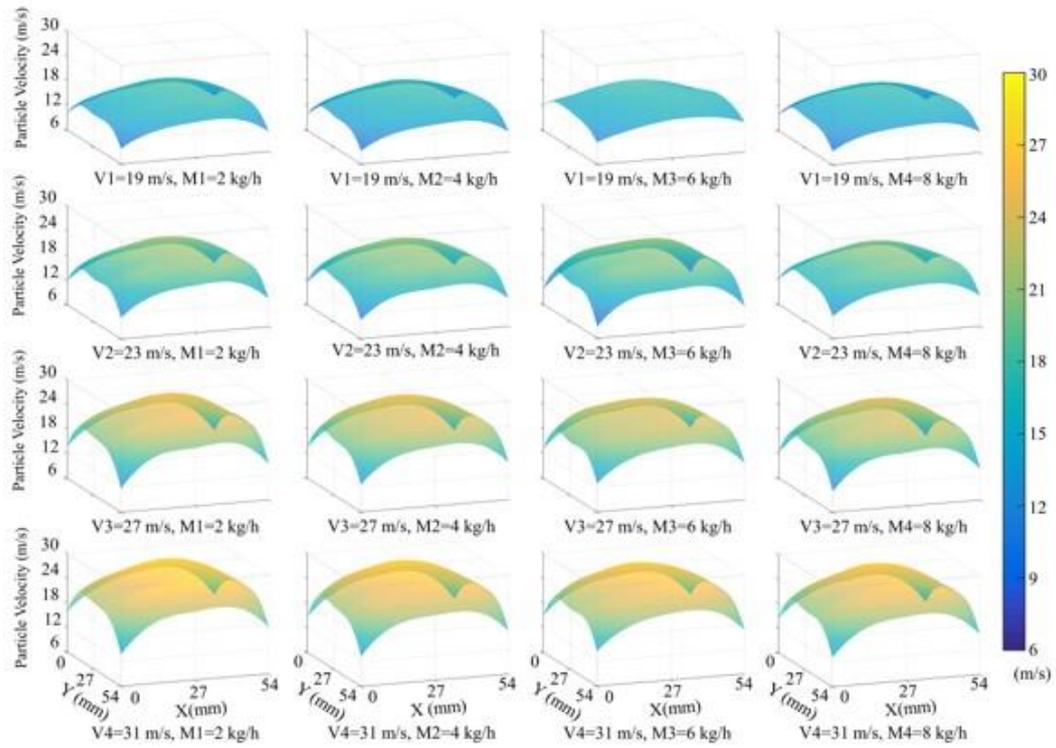
361

**Fig. 11.** Particle velocity distribution under different particle mass flow rate and air velocity conditions.

362  
363



(a)



(b)

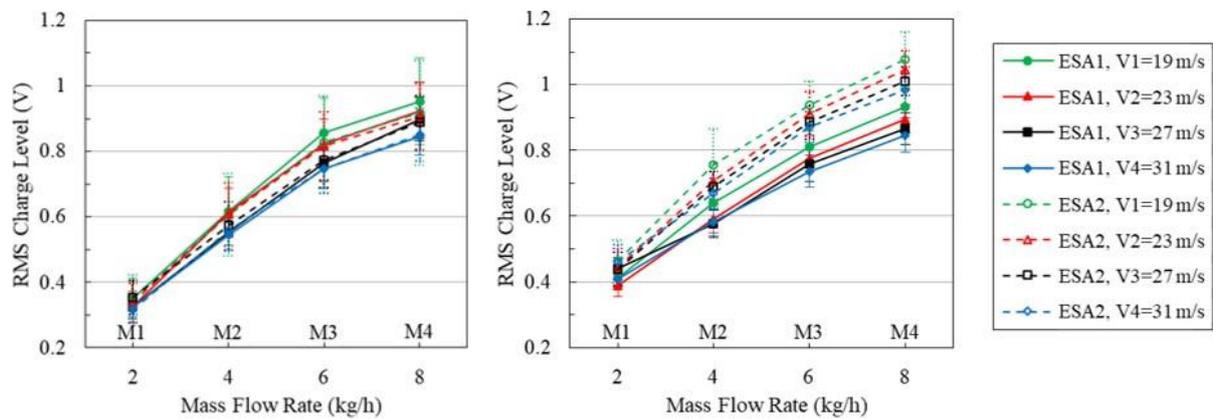
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**Fig. 12.** Particle velocity profiles under different particle mass flow rate and air velocity conditions: (a) horizontal pipe; (b) vertical pipe.

368 *3.4. Cross-sectional mean particle velocities and concentrations*

369 The cross-sectional mean volumetric concentration and velocity of particles are common characteristics for  
370 industry processes monitoring. Therefore, a study on the mean particle cross-sectional parameters (Eq. (4)

371 and (5)) over the pipe measured by electrostatic sensor arrays 1 and 2, respectively, were conducted. Mean  
 372 particle concentrations measured by these two sensor arrays under sixteen test conditions (as shown in Table  
 373 1) are shown in Fig. 13. As can be seen from Fig. 13, the variation trends of the mean particle concentrations  
 374 measured by both of the sensor arrays are similar. The mean RMS charge level of the signals increases about  
 375 0.18 V on average for every 2.0 kg/h increase in particle mass flow rate when the air velocity remains  
 376 unchanged. The mean RMS charge level of the signals decreases by 0.02 V with every 4 m/s increase of air  
 377 velocity. In addition, the standard deviation of RMS charge level increases by 0.01 V on average for every 2  
 378 kg/h increase in particle mass flow rate and decreases by 0.01 V for every 4 m/s increase in air velocity,  
 379 which is consistent with the RMS charge level. The mean RMS charge levels of the signals measured by the  
 380 two sensor arrays have obvious gaps but with similar trends when plain flour particles flow from the  
 381 horizontal pipe section to the vertical pipe section. The mean RMS charge level of the signals measured by  
 382 sensor array 1 increases 0.01 V, while that measured by sensor array 2 increases 0.12 V, which is much  
 383 higher than that derived from sensor array 1. Because there are fewer particles in the pipe centre than those  
 384 near the pipe walls (Fig. 11) in the vertical pipe.



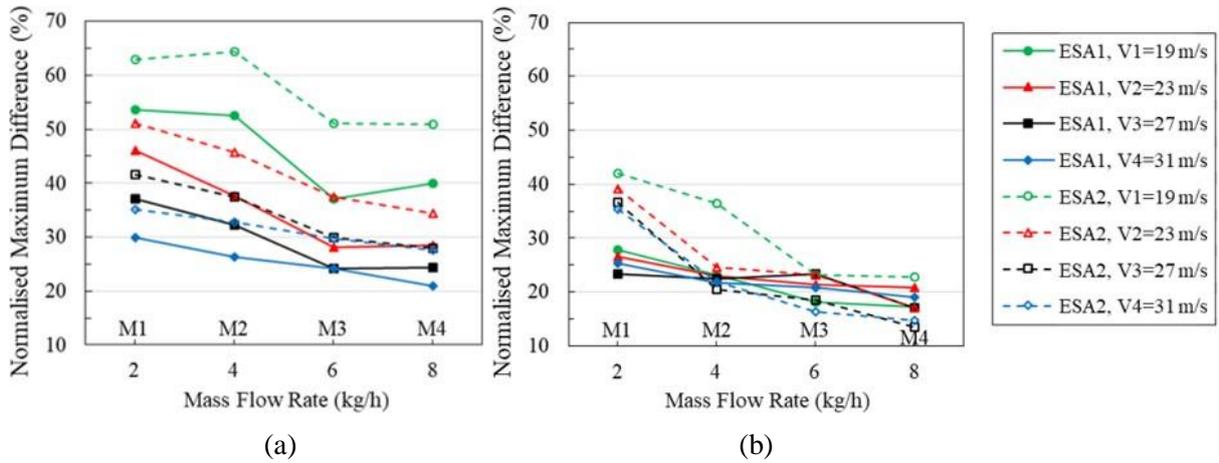
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387 **Fig. 13.** Mean RMS charge levels measured by electrostatic sensor array 1 (ESA1) and electrostatic sensor  
 388 array 2 (ESA2) under different test conditions: (a) horizontal pipe; (b) vertical pipe.

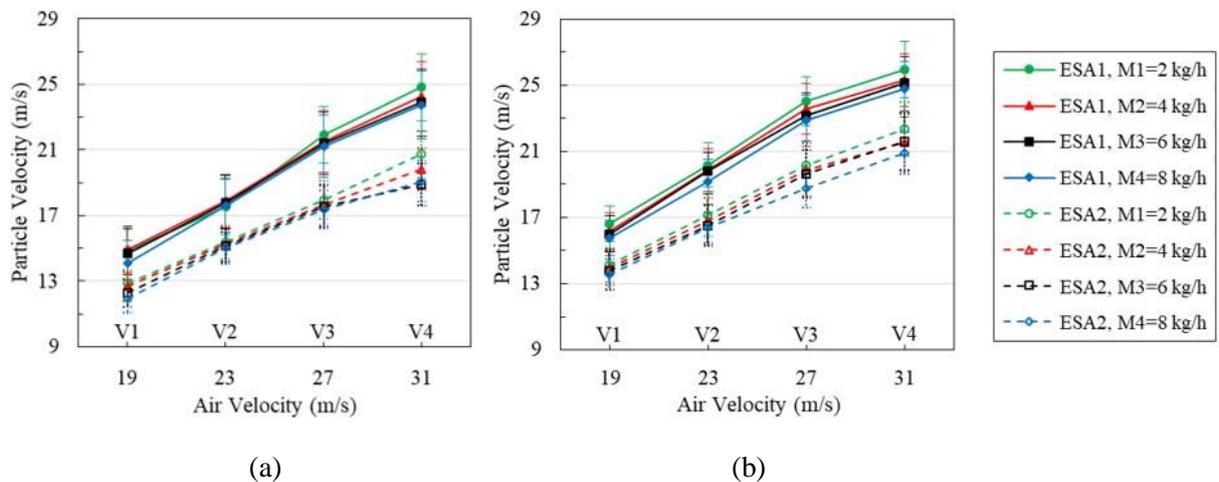
389 The normalised maximum differences of RMS charge levels of the signals measured by electrostatic sensor  
 390 arrays 1 and 2 are plotted in Fig. 14. A greater normalised maximum difference of RMS charge levels of the  
 391 signals means a larger slope of particle concentration profile in a horizontal pipe considering the variation of  
 392 the mean particle velocities. While a greater normalised maximum difference means a higher height of the  
 393 arch of the normalised particle concentration profile in a vertical pipe. As can be seen from Fig. 14, the  
 394 normalised maximum differences measured by sensor array 1 are 5.4% smaller than those by sensor array 2  
 395 on average under the same test conditions on average. The normalised maximum differences measured in the  
 396 vertical pipe are 14.0% less than those measured in the horizontal pipe in the same test conditions on average  
 397 due to the gravitational effect. In addition, the normalised maximum difference reduces by 4.5% for every 2  
 398 kg/h increase in particle mass flow rate and reduces by 4.6% for every 4 m/s increase in air velocity. Such a  
 399 phenomenon is probably due to the larger viscous force applied to the air flows and the higher collision

400 probability between particles and, consequently, the normalised curvatures of the concentration profiles tend  
 401 to be smaller.



402  
 403  
 404 **Fig. 14.** Normalised maximum differences of RMS charge levels of the signals measured by electrostatic  
 405 sensor array 1 and electrostatic sensor array 2 under different test conditions: (a) horizontal pipe; (b)  
 406 vertical pipe.

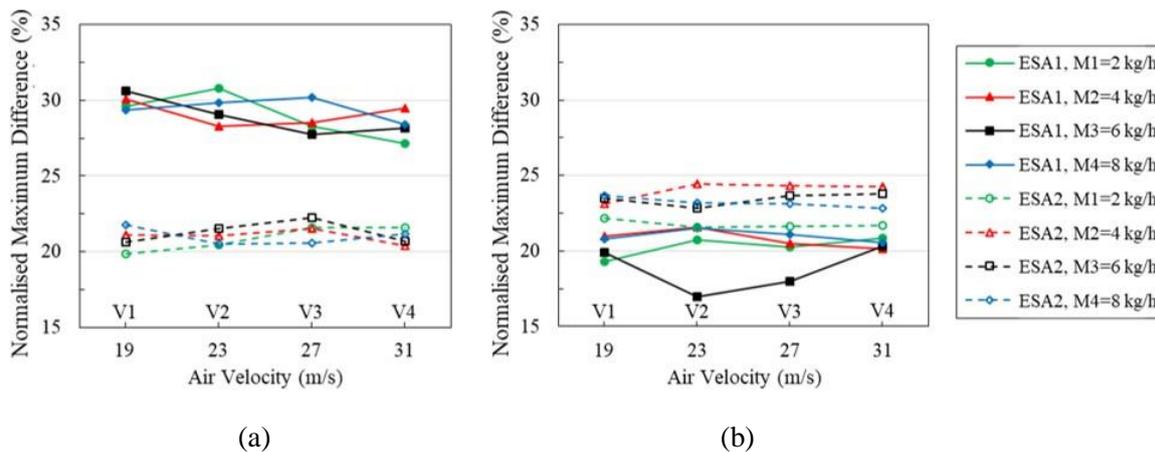
407 The cross-sectional mean particle velocities under sixteen test conditions are shown in Fig. 15. As can be  
 408 seen from Fig. 15, the mean particle velocity increases 2.8 m/s on average for every 4 m/s increase in the air  
 409 velocity when the particle mass flow rate is fixed. The mean particle velocity decreases by 0.3 m/s with  
 410 every 2.0 kg/h increment of particle mass flow rate because of the limitation of the drag force of conveying  
 411 air. Besides, the standard deviation of it increases by 0.19 m/s on average for every 4 m/s increase in air  
 412 velocity and keeps unchanged with the increasing particle mass flow rate. Under the same test condition, the  
 413 mean particle velocities measured by electrostatic sensor array 1 are 3.2 m/s higher on average than those  
 414 measured by electrostatic sensor array 2, and their difference increases 0.6 m/s for every 4 m/s increase in air  
 415 velocity. Because the velocity of the particles in the central area of pipe cross section is higher than that near  
 416 the pipe walls (Fig. 12) and sensor array 1 is more sensitive to the particles in the whole pipe cross section  
 417 compared to sensor array 2. The mean particle velocities in the vertical pipe section are 1.7 m/s higher on  
 418 average than those in the horizontal pipe section since the vertical pipe section is closer to the suction system.



419  
 420

421 **Fig. 15.** Mean particle velocities measured by electrostatic sensor array 1 and electrostatic sensor array 2  
 422 under different test conditions: (a) horizontal pipe; (b) vertical pipe.

423 The normalised maximum differences of velocities measured by electrostatic sensor arrays 1 and 2 are  
 424 plotted in Fig. 16 to illustrate the overall velocity profiles across the pipe. A greater normalised maximum  
 425 difference of velocities means a higher arch of the normalised particle velocity profile. As can be seen from  
 426 Fig. 16, the normalised maximum differences remain constant with the increasing conveying air velocity or  
 427 particle mass flow rate, which is inconsistent with the trend of the normalised maximum differences of RMS  
 428 charge levels of the signals (Fig. 14). In the horizontal pipe, the normalised maximum differences measured  
 429 by sensor array 1 are 8.1% higher than those by sensor array 2 on average under the same test conditions due  
 430 to the difference of sensing areas of the two sensor arrays. Additionally, the normalised maximum  
 431 differences measured by sensor array 1 in the vertical pipe are 8.9% less than those measured in the  
 432 horizontal pipe in the same test conditions on average due to the gravitational effect. However, the  
 433 normalised maximum differences measured by sensor array 2 in horizontal and vertical pipes are similar.  
 434 Because the particle velocity in the central zone is obtained from the weighting method and the same weight  
 435 coefficient is used for both horizontal and vertical pipe tests. As illustrated in Fig. 12, the maximum particle  
 436 velocities are measured in the pipe centre and the minimum velocities are measured near the pipe walls.  
 437 Consequently, the normalised maximum differences measured by sensor array 2 change very little. This  
 438 result demonstrates that the measurement accuracy of the sensor array 2 is essentially affected by the choice  
 439 of weighting coefficient, indicating that sensor array 1 is more reliable than sensor array 2 when measuring  
 440 the local parameters inside the pipe. Therefore, the developed electrostatic sensor array can be used to  
 441 calibrate other types of non-intrusive ones for flow parameter measurement in a square-shaped pipe.



442  
 443 (a) (b)  
 444 **Fig. 16.** Normalised maximum differences of velocities measured by electrostatic sensor array 1 and  
 445 electrostatic sensor array 2 under different test conditions: (a) horizontal pipe; (b) vertical pipe.

#### 446 4. Conclusions

447 Intrusive and non-intrusive electrostatic sensor arrays in combination with the biharmonic spline  
 448 interpolation method have been used to measure the cross-sectional velocity and concentration profiles of  
 449 pneumatically conveyed particles in a square-shaped pipe under various dilute flow conditions. Experimental

450 results have demonstrated that in a horizontal pipe more particles are transported in the central area at the  
451 bottom of the pipe with lower velocity than those in the two corners. While more particles are conveyed near  
452 the pipe walls than those in the centre of the pipe in a vertical pipe. Particles in the centre of both horizontal  
453 and vertical pipe cross sections travel faster compared with those close to the pipe walls. In a vertical pipe,  
454 the velocities of the particles close to the medial wall of the bend are higher than those close to the lateral  
455 wall of the bend. The mean cross-sectional particle parameters measured by the proposed electrostatic sensor  
456 array and the non-intrusive electrostatic sensor array are slightly different due to their different localised  
457 particle parameter calculation methods and the spatial sensitivity distribution. The normalised maximum  
458 difference of the RMS charge levels reduces by 4.5% for every 2 kg/h increase in particle mass flow rate and  
459 reduces by 4.6% for every 4 m/s increase in air velocity. This outcome can be extended such that the particle  
460 concentration distribution is more uniform across the pipe under higher particle mass flow rate or conveying  
461 air velocity conditions. However, the particle velocity distribution remains unchanged with particle mass  
462 flow rate or conveying air velocity. The measured particle velocity profiles show that the proposed intrusive  
463 sensor array is advantageous to the non-intrusive sensor array when measuring the local parameters of  
464 particles. Therefore, the intrusive sensor array can be used for the calibration of other electrostatic sensing  
465 systems used for flow parameter measurement in a square-shaped pipe.

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