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Semi-disparate impact of kinases GCN2 and PERK in modulating the dynamic control properties of eIF2 pathway

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ABSTRACT The tumor microenvironment associated with deficiencies in nutrients and oxygen is important in observing the regulation of tumor progression. The aggressiveness of the tumour cells can be stimulated by exposing it to nutrient starvation and hypoxia. During nutrient starvation, activation of integrated stress response pathway takes place, which helps tumor cells to cope with nutrient stress. In this paper, an evolutionarily conserved central translational control pathway, i.e. the integrated stress response pathway is analysed with the help of a mathematical model. The present study is of significant novelty in terms of testable predictions about specific pathway properties with the help of analysis tools from control theory. Investigation has suggested that, both kinases GCN2 and PERK has semi-disparate impact on dynamic control properties of the system. Examples include both kinases show analogous behaviour towards the robustness and stability of the system, but disparate behaviour in compensating the loss of another kinase.

INDEX TERMS Bode analysis, linear system, mathematical modelling, protein synthesis, robustness, stability, biophysics.

I. INTRODUCTION

Translational and transcriptional regulations are known to control and determine the gene expression levels [1], [2]. The translational activity is solely controlled by numerous translation factors, and broadly occurs in four different stages namely initiation, elongation, termination and recycling. One of the best studied translational control mechanisms impinges on the eukaryotic initiation factor 2 (eIF2) [3].

The eIF2 has a tendency to quantitatively block gene expression levels when phosphorylation of its α -subunit occurs during diverse array of stimuli [4]. Phosphorylation of eIF2 α converts eIF2 into competitive inhibitor of eIF2B, which as a result disturbs the guanidine exchange cycle and ceases ongoing translation activity [5]. Down-regulation of eIF2 due to excessive phosphorylation is responsible for survival of tumour cell [6], and causes numerous neurological diseases such as Alzheimer [7], Parkinson [8], Huntington [9].

There are various kinases known to phosphorylate eIF2 α

in response to a diverse array of stimuli such as GCN2, PERK, PKR and HRI [10]. Integrated stress response (ISR) pathway is one of the pathways that constitutes all four kinases and responds during extracellular stimuli [4]. Such array of stimuli trigger changes in the cells by activating kinases, which tend to phosphorylate eIF2 α .

Among these kinases, GCN2 is conserved in eukaryotes at both structural and functional levels and activates by interacting with uncharged tRNAs during amino acid deprivation, whereas PERK is activated due to accumulation of unfolded proteins in the endoplasmic reticulum (ER) [11], [12]. Also, it has been found that uncontrolled production of protein under amino-acid deficiency causes accumulation of misfolded peptides in the ER and lead to PERK activation [13]. The similarity between regulation of GCN2 and PERK is that, both kinases have tendency to connect to the output of translational activity in a form of feedback loop under amino-acid starvation. On the other hand, the remaining two

kinases which are not derived from translational activity are PKR and HRI. PKR activates to double-stranded RNA, while kinase HRI responds to heme deprivation [14]. In this paper, the former group of kinase is mathematically modelled under amino-acid deficiency, and the analysis tools from control theory are used to address the dynamic control properties of the pathway.

The active role of GCN2 and PERK on overall translation activity has been studied extensively in the literature [15]–[19]. To study the role of GCN2 and PERK on translation initiation with the help of mathematical model is possible in two different ways. The first approach is to consider the overall translation initiation pathways, while another approach is to focus on core reactions [20]–[26]. In this paper, a system of core eIF2:GDP complexes is adopted to investigate the semi-disparate role of kinases GCN2 and PERK in modulating the dynamic control properties of the eIF2 system.

The remainder of the paper is organised as follows. In Section II, a mathematical model of eIF2 dependent regulatory system is developed using mass action kinetics. The same section also demonstrate a simple yet effective optimisation algorithm for parameter estimation comprising of number of constraints to cope from limited data problem. Section III presents the detailed analyses of the dynamical behaviour of eIF2 dependent regulatory system. The analyses presented in this section is novel in terms of testable predictions about specific pathway properties. Finally the paper is concluded in Section IV.

II. MATERIALS AND METHODS

A. MATHEMATICAL MODEL

Fig. 1 illustrates the eIF2 pathway, which comprises of the core reactions required for sustaining ongoing translation activity. The initiation factor eIF2 has an ability to exchange between its GDP-bound and GTP-bound states with the help of guanine nucleotide exchange factor (GEF) termed eIF2B, before it is capable for the next round of translation initiation. The exchange process is further regulated by a guanidine dissociation inhibitor (GDI) function of eIF5 [27]. The release of eIF2:GDP in the form of eIF2:GDP:eIF5 complex indicates completion of translation initiation process [28]. To sustain the ongoing translation activity, regeneration of eIF2:GDP is required by forming eIF2B:eIF2:GDP GEF complex. The formation of eIF2B:eIF2:GDP GEF complex is possible either by release of eIF5 prior to recruitment of eIF2B (route 1) or through eIF5:eIF2B:eIF2:GDP intermediate complex (route 2) [27].

During diverse array of stimuli, phosphorylation of eIF2 converts it into a competitive inhibitor of eIF2B. Phosphorylated eIF2 (eIF2-P) binds with eIF2B to form a tight complex that disrupts nominal translation activity [29]. The proposed model includes two distinct kinases that impact the concentration level of phosphorylated eIF2. The rationale for considering two kinases is to investigate the theory proposed by Lehman *et al.* [4] after experimental analyses. That is, in the tumour cells, one kinase takes over another kinase when

it is inhibited or removed from the system. In the proposed model, active PERK and GCN2 are considered as two kinases that are responsible for phosphorylating eIF2. In the present model, both kinases combine with respective activators and form a Kinase:KinaseActivator complex for further reaction. In the mathematical model, the reaction of kinase activation is controlled by initial concentrations of reacting species.

The overall reaction system of eIF2 cycle is defined in supplementary file S1. To develop a deterministic mathematical model constituting ODEs to describe the aforementioned reaction system, the mass-action kinetic modelling approach is adopted. The overall ODEs of eIF2 mediated regulatory system is given in supplementary file S2.

Note that, the model represents kinase activation by one of the two aforementioned distinct modes which are responsible for phosphorylation of eIF2 α , that is, kinases GCN2 and PERK that are generated as part of the translation reaction. The non-linear mathematical model comprising ODEs in supplementary file S2 has been implemented in Matlab and solved using a modified rosenbrock solver (ode23s) [30].

In order to estimate rate constants of the mathematical model, the Levenberg-Marquardt (LM) algorithm [31] is used. Note that, the quantitative experimental data for the model is limited, and hence the rate constants are estimated with the help of the LM algorithm by integrating it with pathway characteristics such as robustness against parametric fluctuations. The parameter estimation process is to be thoroughly discussed in the sub-section II-C.

B. EXPERIMENTAL DATA

The mammalian molecular initial concentration used to estimate the unknown rate constants are given in supplementary file S3. The range of initial molecular concentrations of the species considered in this work lie between $10nM - 1\mu M$ [32]–[34]. The activation of kinases and phosphorylation of eIF2 are simulated by increasing the total cellular concentrations of activators of GCN2 and PERK [35]. The target of 2,000,000 proteins per micro cubic meter is set as the algorithm constraint [32] for parameterisation process, which indicate the sustainable translation activity under non-stress case (when kinase is not activated). Note that, the intracellular concentrations were calculated from molecule numbers based on a mammalian protein density or protein mass per volume ≈ 0.2 g/mL, average length in amino acids of a protein ≈ 400 aa/protein and average mass of amino acid ≈ 110 Da/aa [32]–[34].

To estimate the ratio of eIF2 α -P to eIF2 α in response to a diverse array of stimuli, the adenovirus expressing cre recombinase (Ad-cre) is injected into the right leg muscle of mice, which resulted in the formation of soft tissue sarcomas in nearly 100% of mice [4]. Further to determine if the GCN2 has been activated in the sarcomas, Lehman *et al.* [4] have homogenised tumors and normal muscle from GCN2+/+, GCN2+/-, and GCN2-/- mice and immunoblotted for total and phosphorylated GCN2. Note that, GCN2 +/+ implies an active state of both copies of GCN2, while

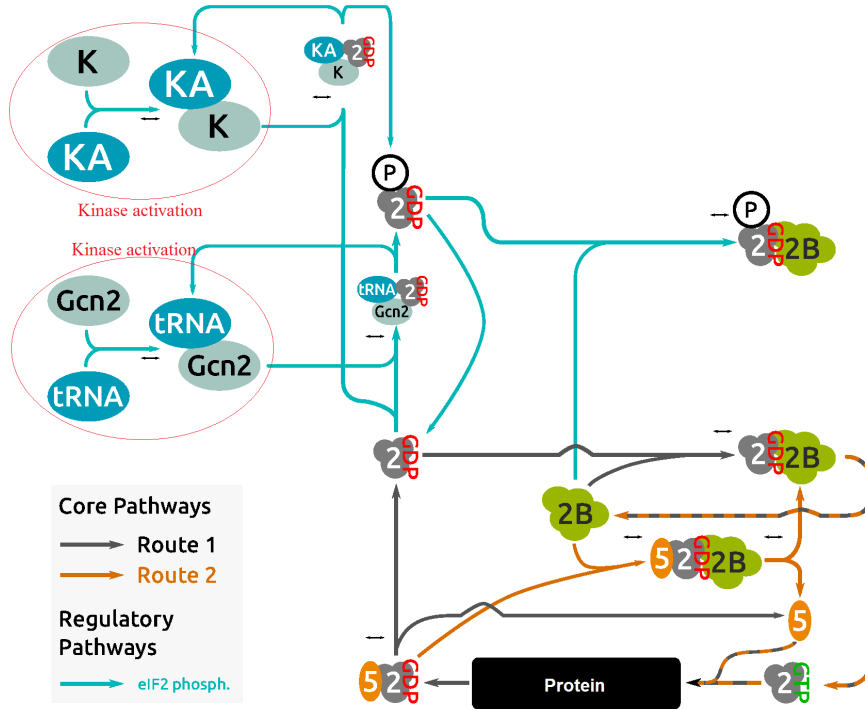


FIGURE 1. eIF2 dependent regulatory pathway representing regulation of translation via phosphorylation of eIF2. Under diverse array of stimuli, the activation of PERK and GCN2 occur, which disrupts the translation activity and sustain cell metabolism. The species indicated in the form of symbols are: 2, eIF2; 2-P, phosphorylated eIF2; 2B, eIF2B; 5, eIF5; K, PERK; KA, misfolded peptide.

GCN2 +/− means only one copy (out of two) is active, and the last one GCN2 −/− indicates both copies of GCN2 are inactive.

Observing two different western blot samples of mixed background sarcomas in [4], reveals that reducing the level of GCN2 affects the level of eIF2α-P. The quantified result shows that, for GCN2 −/− the ratio of eIF2α-P to eIF2α yields a significant reduction in the eIF2α-P level. However in C57BL6 tumors, the reduction in GCN2 concentration has no effect on the levels of eIF2α-P.

C. PARAMETER ESTIMATION

In this section, a minimisation of temporal error functions (ξ_1 and ξ_2) is adopted for estimating the unknown rate constants of the model, similar to the one reported by Khan et al. in [25]. The minimisation of error functions are briefly discussed below.

If the value of ξ_1 is close or equal to zero, then this suggests that the experimental data of protein and data value of simulated model are equal and overlapping.

$$\xi_1 = |Y_{1D} - Y_1(\mathbb{V}, \mathbb{C}, t)| \quad (1)$$

where, ξ_1 is an absolute error between experimental and simulated values, Y_{1D} is the experimental data value of translation, $Y_1(\mathbb{V}, \mathbb{C}, t)$ is *in-silico* experimental value of translation rate obtained after solving ODEs for rate constant obtained using the LM algorithm.

After obtaining a set of rate constants giving $\xi_1 \equiv 0$, the vector of rate constants i.e. \mathbb{C} is perturbed to $\pm 50\%$ from its

obtained value, and the error between $Y_1(\mathbb{V}, \mathbb{C}, t)$ and new simulated protein values is recorded. The average value of error ξ_2 can be determined by

$$\xi_2 = \frac{1}{T} \int_0^T \frac{|Y_1(\mathbb{V}, \mathbb{C}, t) - Y_1(\mathbb{V}, \Delta\mathbb{C}, t)|}{\max(Y_1(\mathbb{V}, \mathbb{C}, t), Y_1(\mathbb{V}, \Delta\mathbb{C}, t))} dt \quad (2)$$

where, T is the evaluation time and $\Delta\mathbb{C}$ is equal to $\pm 50\%$ of original \mathbb{C} value. The purpose of perturbing the rate constants is to analyse the responsiveness of translation activity. Lower value of ξ_2 defines high robustness against parametric changes [36], [37]. Therefore, the combination of \mathbb{C} giving minimum value of ξ_2 is considered. Note that, this step helps to extract the highly robust parameter sets from other comparatively less robust parameter sets.

The set of rate constants obtained from the parametrisation process is given in Supplementary file S4. Fig. 2 shows the deviation of translation activity with respect to its principal behaviour. The red bars represent error ξ_2 for non-stress case, while the blue line represents the translation activity for initial concentration values and rate constants reported in supplementary files S3 and S4 respectively. Steady state translation under non-stress conditions in our model captures the robustness of real-life translation against high parametric fluctuations upto $\pm 50\%$ [4].

III. MODEL ANALYSES AND PREDICTIONS

In this section a semi-disparate behaviour of two kinases over dynamic properties of eIF2 dependent regulatory system is analysed with the help of control theory. The initial

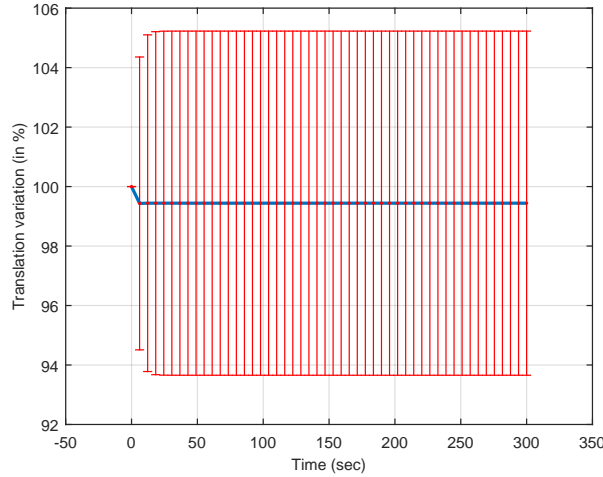


FIGURE 2. Principal behaviour and robustness of the non-stress model, when the rate constants of the model undergo fluctuations upto $\pm 50\%$ from its original value. Blue solid line represents principal behaviour and red lines represent standard deviation from principal behaviour when parameters are fluctuated.

concentrations and rate constants obtained for non-stress and stress cases are all the same except the values of Y_{13} and Y_{15} , which are zero (minimum) for non-stress case and greater than zero for stress case respectively. The activation of kinases has a reciprocal effect on changes to the translation activity which resulted into drop of translation activity from $\approx 2,000,000$ proteins/micro cubic meter (100%) to $\approx 20,000$ proteins/micro cubic meter (1%) in a span of 4 minutes.

A. LINEARISATION AND STRUCTURED SINGULAR VALUE ANALYSIS

In this sub-section a non-linear model is linearised around equilibrium point to analyse the frequency behaviour of the eIF2 cycle. Note that, the mathematical model is considered as a multi-input single-output (MISO) system, in which formation of protein is system output where the impact of two input kinases is observed. To simulate such model, the transfer functions of MISO model can be considered as two different arrays of elementary single-input single-output (SISO) transfer function: one array resembles uncharged tRNA which activates kinase GCN2 (Y_{13}) as input for one SISO model, while another array resembles active kinase PERK (Y_{15}) as input for another SISO model. Such arrays can help in investigating and comparing the impact of two different kinases individually on general translation activity. Based on ODEs given in supplementary file S2, the generalised state space representation of non-linear SISO model can be defined as follows:

$$\dot{Y}(t) = \hat{Y}_i(Y(t), C) + \hat{B}_i(Y(t))u_i \quad (3)$$

$$Z(t) = Y_1(t) \quad (4)$$

where, $i = [1, 2]$, \hat{Y}_i is a matrix with $\dot{Y}_{13} = 0$ while \hat{Y}_2 is a matrix with $\dot{Y}_{15} = 0$, vectors \hat{B}_i can be represented as:

$$\hat{B}_1(Y(t)) = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ -C_{12}Y_9 \ C_{12}Y_9 \ 0 \ 0 \ 0 \ 0 \ 0]^T$$

$$\hat{B}_2(Y(t)) = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ -C_{20}Y_7 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ C_{20}Y_7]^T,$$

$Z(t)$ is the output (or protein) and vector $C = [C_1 \ C_2 \ C_3 \ \dots \ C_{22}]^T$.

The linearised model of non-linear SISO system around equilibrium point (Y^{eq}) is described below. Note that, the non-linear model is first linearised around equilibrium point Y^{eq} and then the linearised system dynamics are equated to zero. The feasible equilibrium point for the model is given in Supplementary file S5.

The state space representation of approximate linear SISO system around the equilibrium point mentioned in Supplementary file S6 can be re-written in the form:

$$\dot{y} = A_i y + B_i u_i \quad (5)$$

$$Z = D y \quad (6)$$

where, $i = [1, 2]$, A_i is the Jacobian matrix (given in Supplementary file S7), u_i is input signal, B_i and D are constant input and output matrices respectively defined as follows.

$$B_1 = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ -4.039 \ 4.039 \ 0 \ 0 \ 0 \ 0 \ 0]^T \times 10^{-2}$$

$$B_2 = [0 \ 0 \ 0 \ 0 \ 0 \ 0 \ -3.955 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 3.955]^T \times 10^2$$

$$D = [1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0]$$

Note that, for the sake of simplicity, the linear version of non-linear system Y_i is denoted by y_i . In this case, size of the matrix A_i is 15×15 . On the other hand, finite values within matrix B_i represent the species on which input is acting and matrix D represents the location at which final impact is to be observed that is protein formation. Fig. 3 compares the frequency behaviour of two models for different inputs. Observing Bode magnitude plots of both systems, it can be stated that both active kinase inputs GCN2 and PERK are impacting the translation activity distinctly during phosphorylation process, which is evident from red and green solid lines in Fig. 3. On the other hand, the frequency analysis shows the partial tracking of red solid line and black dotted line, which indicate that elimination of active GCN2 from the model is compensated by another active kinase PERK, while vice-versa is not justified. In other words, this observation

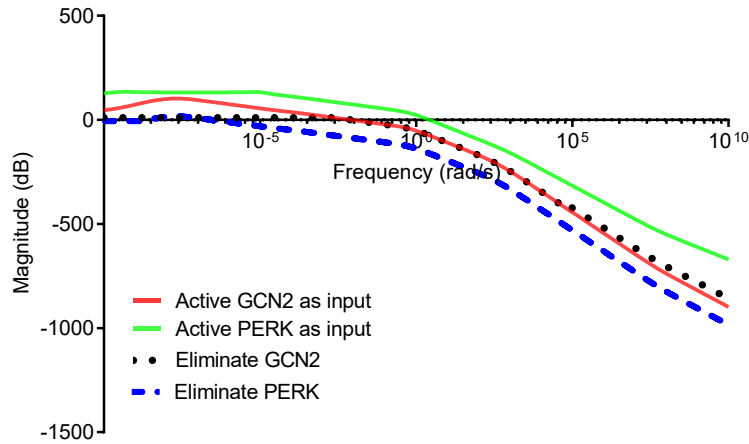


FIGURE 3. Bode magnitude plots by considering activated GCN2 (y_{13}) and PERK (y_{15}) as the inputs. Red solid line represents linear SISO model with active GCN2 as input, while green solid line represents another linear SISO model with PERK as input. The black dotted line and blue dashed line represent behaviour of model when GCN2 is removed while PERK is active input and PERK is removed when GCN2 is active input.

suggests that, the downstream of translation activity due to the activation of kinase GCN2 is different than PERK, and change in the general behaviour of the system due to the loss or removal of active kinase GCN2 is not similar to that of loss of activated PERK. Note that, the elimination process has been conducted by using matched DC gain method [25].

The above prediction clearly states the distinct role of both kinases on ceasing translation activity, it is worthy to estimate the impact of individual kinase on the robustness and stability of the system. The robustness and stability analyses will help in further investigating the distinct impact of both kinases on the system properties. The robustness of the system can be analysed using a tool from control theory known as structured singular value (μ) [38], while stability of the system can be analysed with the help of pole analysis of linearised system. The μ of the proposed linear eIF2 system is defined as:

$$\mu = \frac{1}{\min_{\Delta} \{\bar{\sigma}(\Delta) | \det(I - M(s)\Delta) = 0 \text{ for } \Delta \in B_{\Delta}\}} \quad (7)$$

where, $\bar{\sigma}$ denotes maximum singular value, $M(s)$ denotes the transfer function of the system and B_{Δ} represents a set of uncertainties Δ . From the above equation it is evident that, the principle at which μ -analysis works is to find the smallest value of $\bar{\sigma}(\Delta)$ which makes $(I - M(s)\Delta)$ singular. When there is no Δ such that $\det(I - M(s)\Delta) = 0$ then $\mu = 0$.

To analyse the robustness of the system, a parametric uncertainty matrix block Δ is introduced into the linear system. Note that, $\Delta = \text{diag}[\delta_{C_1} \ \delta_{C_2} \ \delta_{C_3} \ \dots \ \delta_{C_{22}}]$ and $M(s)$ is the transfer function defined as:

$$M(s) = D(sI - A_i)^{-1}B_i \quad (8)$$

Now, introducing Δ into the system changes the rate constant C to $C(1 + \delta_C)$. Recalling the state space representation of perturbed system:

$$\begin{aligned} \delta \dot{y} &= A_i \delta y + B_{0i} \Delta y \\ y &= D_{0i} \delta y \end{aligned} \quad (9)$$

Note that the dimensions of constant matrices B_{0i} and D_{0i} are 15×22 and 22×15 respectively. The matrices B_{0i} and D_{0i} for perturbed linear system with two different inputs are defined in Supplementary file S8.

From Figs. 4 and 5, it is evident that the upper bound of $\mu^{-1} = 1$ for both kinases, which suggest that the robustness of the system is similarly affected by both kinases illustrated in Fig. 1. Observing poles of linearised system in supplementary file S9, a similar observation is also noticed for the stability of the system, that is, the poles of the system with different kinase input are distributed in a very similar fashion, which suggest that the overall stability of the system is also arising from the properties of the common core pathway species. Hence, it can be asserted that, both kinases has analogous impact in terms of robustness and stability of the eIF2 dependent regulatory system.

B. LOSS OF GCN2 ON PHOSPHORYLATION OF EIF2 α

It is well understood that under diverse array of stimuli, the activation of kinases GCN2 and PERK take place which leads to formation of Kinase:KinaseActivator complex which phosphorylates eIF2 α and form eIF2-P. The mathematical model mimics this particular scenario in a similar way, that is, during the absence of kinase activator complex, the level of eIF2 α remains in its steady state and there is no phosphorylation or formation of eIF2-P. On the other hand, during amino acid starvation, the loss in concentration of eIF2 α and gain in the strength of eIF2-P take place. It is found that, this process is gradual in nature, that is the ratio of gain/loss in eIF2-P/eIF2 α largely depends on the strength of reciprocal effect from starvation.

The Bode plot analysis has revealed that removal of kinase GCN2 has disparate effect on compared to removal of PERK on translation activity. To investigate the effect of loss of GCN2 and tRNA signalling on eIF2-P/eIF2 α , the mathematical model performs simulation by considering the concentration of GCN2 as 100%, 50% and 0% of 3.00×10^{-8} M

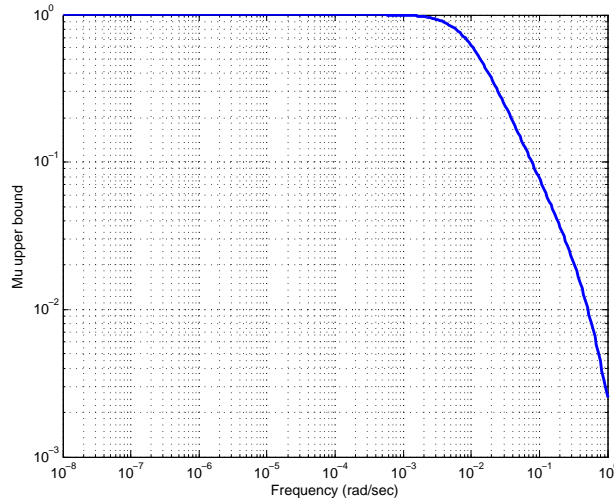


FIGURE 4. Upper bound of the structured singular value μ of linear system (supplementary file S6) with y_{13} as input

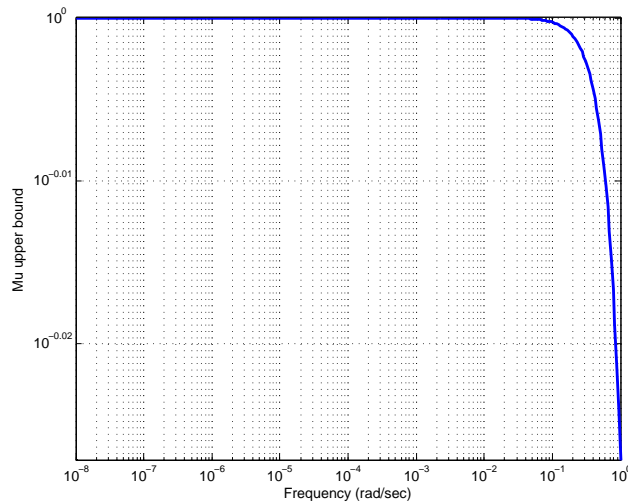


FIGURE 5. Upper bound of the structured singular value μ of linear system (supplementary file S6) with y_{15} as input

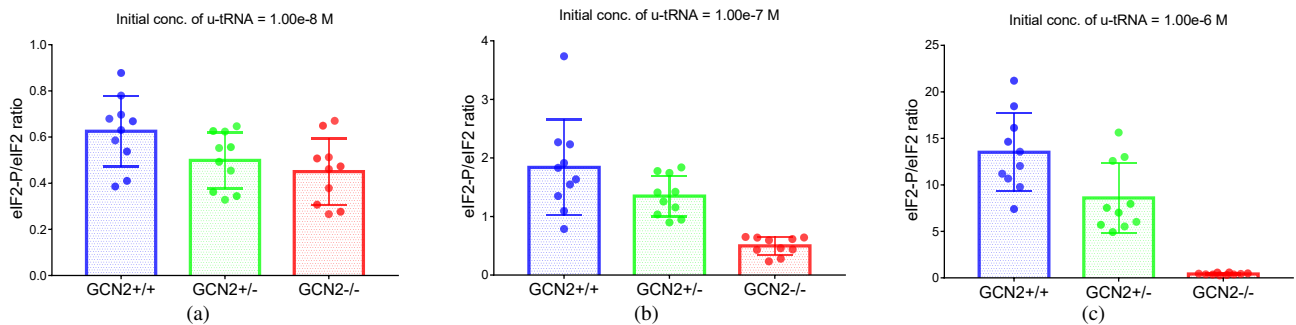


FIGURE 6. Effect of increasing concentration levels of uncharged tRNA on eIF2-P/eIF2 ratio for three different genotypes, while keeping initial concentration of active PERK constant

for GCN2 +/+, GCN2 +/- and GCN2 -/- respectively. Fig. 6 illustrates the role of strength of uncharged tRNA on eIF2-P/eIF2 ratio. Observing Fig. 6(a) it is found that, lower the pool concentration of uncharged tRNA, lesser will be the statistical significant difference among all three geno-

types. On the other hand, higher the pool concentration of uncharged tRNA (Figs. 6(b)-(c)), higher will be the statistical significant confidence limit. This observation reinforces that, variation in tRNA strength is one of the important factor which is responsible for showing statistical significant dif-

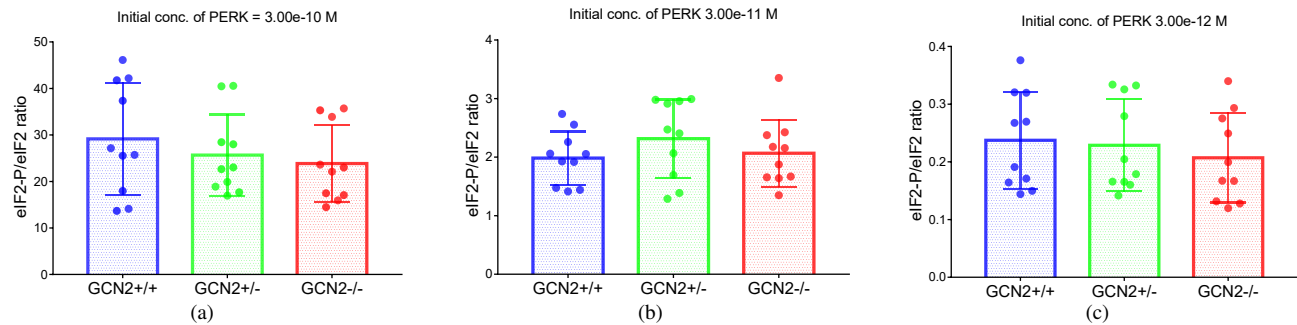


FIGURE 7. Effect of increasing concentration levels of active PERK on eIF2-P/eIF2 α ratio for three different genotypes, while keeping initial concentration of uncharged tRNA constant

ference among three genotypes.

In order to further extend this observation, the role of PERK over eIF2-P/eIF2 α ratio in Fig. 7 is also illustrated which indicates that, varying concentration of PERK has no impact on statistical significant difference among all three genotypes but drastic increase in strength of eIF2-P. These observations suggest that impact of PERK and GCN2 on the ratio of eIF2-P/eIF2 α ratio is distinct, and PERK is compensating the loss of GCN2 and maintaining levels of phosphorylated eIF2 α in tumours. Another prediction suggests that one of the reasons behind statistically significant difference between eIF2-P/eIF2 α for two different sarcomas is due to the varying strength of uncharged tRNA. This investigation suggests the scenarios in which the removal of kinase has no impact on increase in limit of eIF2 α phosphorylation and is therefore not sufficient for derepression of translation activity.

IV. CONCLUSION

In this paper, a mathematical model of eIF2 dependent regulatory model is developed and its dynamic control properties have been addressed. The proposed model consists of two different kinases, which have a tendency to phosphorylate eIF2 in diverse conditions. The mathematical model is able to reach a steady state translational activity at levels very similar to a well-studied *in vivo* system, and during activation of eIF2 kinases the translation ceases accordingly. Tools from control theory such as structured singular value and Bode plot analysis have been used to investigate the properties of the system under two kinases namely GCN2 and PERK. The investigations have revealed both kinases has semi-disparate impact on translation activity, that is, both kinases have similar or analogous impact on robustness and stability of the system, whereas disparate impact on the ceasing translation activity. On the other hand, out of the two kinases, only PERK has a tendency to compensate the loss of kinase GCN2 and is responsible for maintaining levels of phosphorylated eIF2 α in tumours.

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