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Modelling Timeouts without Timelocks

Howard Bowman*

Computing Laboratory, University of Kent at Canterbury, Canterbury, Kent, CT2 7NF, United Kingdom. (Email: H.Bowman@ukc.ac.uk)

Abstract. We address the issue of modelling a simple timeout in timed automata. We argue that expression of the timeout in the UPPAAL timed automata model is unsatisfactory. Specifically, the solutions we explore either allow timelocks or are prohibitively complex. In response we consider timed automata with deadlines which have the property that timelocks cannot be created when composing automata in parallel. We explore a number of different options for reformulating the timeout in this framework and then we relate them.

1 Introduction

A timeout is perhaps the most basic and widely arising specification structure in real-time systems. For example, they arise frequently when modelling communication protocols and work on enhancing "first generation" specification techniques with real-time has frequently been directly motivated by the desire to model timeouts in communication protocols [9].

From within the canon of timed specification notations, timed automata [1] are certainly one of the most important. One reason for this is that powerful real-time model checking techniques have been developed for timed automata, as exemplified by the tools, UPPAAL [2], Kronos [7] and HyTech [8].

However satisfactorily modelling timeout structures proves surprisingly difficult in timed automata. Broadly, problems arise because it is difficult to define timeout behaviour in a manner that avoids the possibility of *timelocks*. By way of clarification:

we say that a system is timelocked if it has reached a state from which no path can be found to a time passing transition.

Timelocks are highly degenerate situations because they yield a *global* blockage of the systems evolution. For example, if a completely independent component is composed in parallel with a system that is timelocked, then the entire composition will inherit the timelock. This is quite different from a classic (local) deadlock, which cannot affect the evolution of an independent process. These characteristics of timelocks will be illustrated in section 2.

^{*} Howard Bowman is currently on leave at VERIMAG, Centre Equation, 2 rue Vignate, 38610 GIERES, France and CNR-Istituto CNUCE, Via S. Maria 36, 56126 - Pisa - Italy with the support of the European Commission's TMR programme.

This paper addresses the issue of how to model timeouts without generating timelocks. We illustrate how the difficulty arises in current timed automata models and then we consider a new timed automata model - Timed Automata with Deadlines (TADs) [3] - which guarantee timelock free parallel composition of automata components.

We begin (in section 2) by presenting background material - we introduce timed automata, discuss the nature of timelocks and outline the timeout behaviour that we require. These requirements have been identified during practical study of the specification and verification of a lip-synchronisation algorithm [6]. Then (in section 3) we discuss possible ways to model the timeout in timed automata. As a typical timed automata model we choose the UPPAAL [2] notation. This is one of the most important timed automata approaches. We argue that none of the legal UPPAAL approaches are completely satisfactory. In particular, avoiding the possibility of timelocks is difficult and leads to prohibitively complex solutions.

In response, (in section 4) we consider how the same timeout behaviour can be modelled in Timed Automata with Deadlines [3]. However, it turns out that the standard TADs approach, as presented in [3], resolves the timelock problem, but introduces a new difficulty which is related to the generation of escape transitions. Consequently, we consider a number of different TAD formulations in section 5 which resolve these difficulties in contrasting ways. Finally, in section 6 we relate these solutions and present a concluding discussion.

2 Background

2.1 Timed Automata

We briefly review some basic timed automata notation.

- A is the set of *completed* (or *basic*) actions.
- $-\overline{A} = \{a?, a! \mid a \in A\}$ is the set of *uncompleted* actions. These give a simple CCS style [10] point-to-point communication which has also been adopted in UPPAAL.
- $-A^{+} = \overline{A} \cup A$ is the set of all actions.
- We use a complementation notation over elements of A^+ ,

$$\overline{a} = a \quad \text{if } a \in A \tag{1}$$

$$\overline{b?} = b! \tag{2}$$

$$\overline{b!} = b? \tag{3}$$

In addition, we let v, v' etc, range over vectors of processes, which are written, $\langle l_1,...,l_n\rangle, |v|$ denotes the length of the vector, we use a substitution notation as follows: $\langle l_1,...,l_j,...,l_n\rangle [l/l_j] = \langle l_1,...,l_{j-1},l,l_{j+1},...,l_n\rangle$ and we write $v[l'_1/l_1][l'_2/l_2]...[l'_m/l_m]$ as $v[l'_1/l_1,l'_2/l_2,...,l'_m/l_m]$. We assume the a finite set: $\mathcal C$

of clocks which range over \mathbb{R}^+ and \mathcal{CC} is a set of clock constraints¹. An arbitrary element of \mathcal{A} , the set of all timed automata, has the form:

$$(L, l_0, T, P)$$

where,

- -L is a finite set of locations (these appear as small circles in our timed automata diagrams, e.g. see figure 1);
- $-l_0$ is a designated start location;
- $-T \subseteq L \times CC \times A^+ \times \mathbb{P}(\mathcal{C}) \times L$ is a transition relation (where $\mathbb{P}(S)$ denotes the powerset of S). A typical element of T would be, $(l_1, \mathsf{g}, \mathsf{a}, \mathsf{r}, l_2)$, where $l_1, l_2 \in L$ are automata locations; $\mathsf{g} \in \mathcal{CC}$ is a guard; $\mathsf{a} \in A^+$ labels the transition; and $\mathsf{r} \in \mathbb{P}(\mathcal{C})$ is a reset set. $(l_1, \mathsf{g}, \mathsf{a}, \mathsf{r}, l_2) \in T$ is typically written, $l_1 \xrightarrow{\mathsf{g}, \mathsf{a}, \mathsf{r}} l_2$, stating that the automata can evolve from location l_1 to l_2 if the (clock) guard g holds and in the process action a will be performed and all the clocks in r will be set to zero. When we depict timed automata, we write the action label first, then the guard and then the reset set, see e.g. figure 4. Guards that are true or resets that are empty are often left blank.
- $-P:L\to CC$ is a function which associates a progress condition (often called an invariant) with every location. Intuitively, an automata can only stay in a state while its progress condition is satisfied. Progress conditions are shown adjacent to states in our depictions, see e.g. figure 2.

Timed automata are interpreted over time/action transition systems which are triples, (S, s_0, \rightarrow) , where,

- -S is set of states;
- $-s_0$ is a start state;
- $\rightarrow \subseteq S \times Lab \times S$ is a transition relation, where $Lab = A^+ \cup \mathbb{R}^+$. Thus, transitions can be of one of two types: *action transitions*, e.g. (s_1, \mathtt{a}, s_2) , where $\mathtt{a} \in A^+$ and *time passing transitions*, e.g. (s_1, \mathtt{x}, s_2) , where $\mathtt{x} \in \mathbb{R}^+$ and denotes the passage of \mathtt{x} time units. Transitions are written:

$$s_1 \xrightarrow{\mathbf{a}} s_2$$
 respectively $s_1 \xrightarrow{\mathbf{x}} s_2$

A clock valuation is a mapping from clock variables \mathcal{C} to \mathbb{R}^+ . For a clock valuation u and a delay d, $u \oplus d$ is the clock valuation such that $(u \oplus d)(x) = u(x) + d$ for all $x \in \mathcal{C}$. For a reset set r, we use r(u) to denote the clock valuation u' such that u'(x) = 0 whenever $x \in r$ and u'(x) = u(x) otherwise. u_0 is the clock valuation that assigns all clocks to the value zero.

The semantics of a timed automaton $A = (L, l_0, T, P)$ is a time/action transition system, (S, s_0, \rightarrow) , where S is the set of all pairs $\langle l, u \rangle$ such that $l \in L$

¹ The form that such constraints can take is typically limited, however since we are not considering verification this is not an issue for us.

and u is a clock valuation, $s_0 = \langle l_0, u_0 \rangle$ and \to is given by the following inference rules:-

$$\frac{l \xrightarrow{g,a,r} l' \ g(u)}{\langle l, u \rangle \xrightarrow{a} \langle l', r(u) \rangle} \qquad \frac{\forall d' \leq d \cdot P(l)(u \oplus d')}{\langle l, u \rangle \xrightarrow{d} \langle l', u \oplus d \rangle}$$

We assume our system is described as a network of timed automata. These are modelled by a process vector² denoted, $|| < A_1, ..., A_n >$. If $\forall i (1 \le i \le n)$. $A_i = (L_i, l_{i,0}, T_i, P_i)$ then the product automaton, which characterises the behaviour of $|| < A_1, ..., A_n >$ is given by,

$$(L^p, l_0^p, T^p, P^p)$$

where $L^p = \{ ||v| | v \in L_1 \times ... \times L_n \}, l_0^p = || < l_{1,0},...,l_{n,0} >, T^p \text{ is as defined by the following two inference rules and } P^p(|| < l_1,...,l_n >) = P_1(l_1) \wedge ... \wedge P_n(l_n).$

$$\frac{l_i \xrightarrow{g_i, a?, r_i} l_i' \ l_j \xrightarrow{g_j, a!, r_j} l_j'}{||v \xrightarrow{g_i \wedge g_j, a, r_i \cup r_j}||v[l_i'/l_i, l_i'/l_j|} \qquad \frac{l_i \xrightarrow{g, a, r} l_i' \ a \in A}{||v \xrightarrow{g, a, r}||v[l_i'/l_i|}$$

where $1 \leq i, j \leq |v|, i \neq j$.

2.2 Timelocks

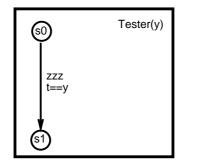
We can formulate the notion of a timelock in terms of a testing process. Consider, if we take our system which we denote System and compose it completely independently in parallel with the timed automaton, Tester, shown in figure 1, where the zzz action is independent of all actions in the system. Then for any $x \in \mathbb{R}^+$ if the composition $|\cdot| < \text{Tester}(x)$, System> cannot perform zzz then the system contains a timelock at time x.

This last illustration indicates why timelocks represent such degenerate situations - even though the Tester is in all respects independent of the system, e.g. it could be that Tester is executed on the Moon and System is executed on Earth without any co-operation, the fact that the system cannot pass time prevents the tester from passing time as well. Thus, time really does stop and it stops everywhere because of a degenerate piece of local behaviour.

This is a much more serious fault than a classical (local) deadlock. For example, the automaton Stop, also shown in figure 1, generates a local deadlock, however, it cannot prevent an independent process from evolving. In the sequel we will use the term *local deadlock* to denote such a non-timeblocking deadlock.

We consider two varieties of timelock which we illustrate by example, see figure 2,

Although our notation is slightly different, our networks are a straightforward simplification of those used in UPPAAL. The simplifications arise because we do not consider the full functionality of UPPAAL. For example, we do not consider committed locations or data variables.



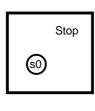


Fig. 1. A tester and a (locally) deadlocked timed automata

- 1. The first is System1; this is a zeno process which performs an infinite number of aaa actions at time zero. This system is timelocked at time zero and if we compose it independently in parallel with any other system, the composite system will not be able to pass time. We call such timelocks zeno timelocks.
- 2. The second is the network | | <System2, System3>; this composition contains a timelock at time 2, which arises because System2 must have performed (and thus, synchronised on) action aaa by the time t reaches 2 while System3 does not start offering aaa until t has past 2. Technically the timelock is due to the fact that at time 2 System2 only offers the action transition aaa and importantly, it does not offer a time passing transition. Since the synchronisation cannot be fulfilled the system cannot evolve to a point at which it can pass time. We call such timelocks composition timelocks.

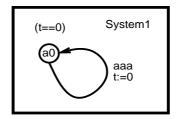
The interesting difference between these two varieties of timelock is that the first one locks time, but in the classical sense of untimed systems, is not deadlocked, since actions can always be performed. However, the second reaches a state in which neither time passing or action transitions are possible. Such composition timelocks are the variety we will address in this paper.

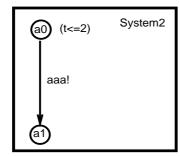
2.3 A Bounded Timeout

We describe a rather standard timeout behaviour, which we call a Bounded Timeout. The general scenario is that a Timeout process is monitoring a Component and the timeout should expire and enter an error state if the Component does not offer a particular action, which we call good, within a certain period of time. The precise functionality that we want the timeout to exhibit is³:

1. Basic behaviour. Assuming Timeout is started at time t, it should generate a timeout action at a time t+D if and only if the action good has not already occured. Thus, if action timeout occurs, it must occur exactly at time t+D

³ Our presentation here is similar to that in [6]





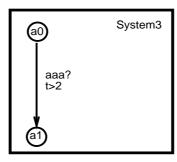


Fig. 2. Timelock Illustrations

and if action good occurs, then it must occur at some time from t up to, but not including, t + D. Using the terminology of [11] this yields a *strong* timeout. A *weak* timeout would, in contrast, allow a non-deterministic choice between the good action and the timeout at time t + D.

- 2. Urgency of good action. We also require that if the good action is enabled before time t + D then it is taken urgently, i.e. as soon as good is enabled it happens. This urgency requirement is akin to the "as soon as possible" principle which has been applied in timed process algebra [12].
- 3. Timelock Free. Finally we want our composed system to be free of timelocks, for obvious reasons.
- 4. Simple. We also require that the solution is not "prohibitively" complex.

Notice that in the first two of these requirements, urgency arises in two ways. Firstly, we require that timeout is urgent at time t+D and secondly, we require that good is urgent as soon as it is enabled. Without the former requirement the timeout might fail to fire even though it has expired and without the latter, even though the good action might be able to happen it might nonetheless not occur and thus, for example, the timeout may expire even though good was possible.

We also emphasize that although our work here was inspired by that in [6], it is somewhat different. In particular, [6] presents a bounded timeout in a discrete time setting, thus, the final time at which the good action can be performed and the time of expiry of the Timeout are at different discrete time points.

3 Modelling the Bounded Timeout in UPPAAL

In this section we describe the bounded timeout in UPPAAL. However, our discussion is not solely relevant to this notation, and could be extrapolated to timed automata notations in general.

Basic Formulation. We begin by considering the Timeout shown in figure 3. This process realises the first requirement that we identified for modelling the bounded timeout - good is offered at all times in which t<D. Then timeout is performed when t==D, in which case the system passes into state a2 which plays the role of an error state. Importantly, the guard (t<=D) forces the required urgency on the timeout action. Thus, if good has not happened earlier, timeout must happen when t==D. Furthermore, it is easy to see that this is indeed a strong timeout - its behaviour is deterministic when t==D.

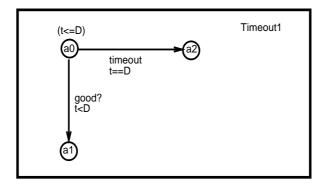


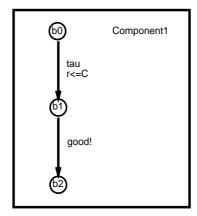
Fig. 3. An UPPAAL Automaton for Timeout1

However on its own, this automaton is not sufficient since nothing forces the good action to be taken if it can be. This was our second requirement. For example, consider Component1 shown in figure 4 which will perform an internal action tau⁴ at some time r<=C and then offer the good action. The internal action can be viewed as modelling some internal computation by Component1. The completion of which is signalled by offering good! Now if we put Timeout1 and Component1 in parallel then even if good could occur while t<D, it might not be taken. Thus, a possible trace of the system:

| | < Timeout1, Component1>

is, (tau, x_1) (timeout, x_2) where, $x_1 < C$, $x_1 < D$ and $x_2 = D$.

⁴ In fact, internal transitions are left unlabelled in UPPAAL, however, we abuse notation in order that we can refer to the transition.



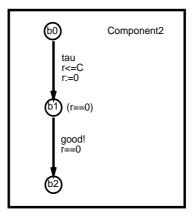


Fig. 4. UPPAAL Automata for Component1 and Component2

Thus, we need some way to make good urgent. The standard approach is to enforce urgency in the component. For example, we could use Component2 shown in figure 4. This automaton will perform the internal action as before and then it *must* immediately perform the good action.

Now the problem with the composition:

| | < Timeout1, Component2>

is the relative values of D and C. In particular, if C is larger than D then this system can time-block in the following way:-

- 1. the timeout could fire when t==D;
- 2. then if tau happens when r==C say, good! will become urgent, however it cannot be performed since Timeout1 is no longer offering it, causing a timelock. Component2 will not let time pass until good is performed, but good cannot be performed because of a mis-matched synchronisation.

We would argue that this is a big problem. In particular, it is not generally possible to ensure that C is less than D since our component behaviour would typically be embedded in the complex functioning of a complete system. In fact, writing C as we have done, abstracts from a likely multitude of complexity and deriving such a value from a system would typically require analysis of many components of the complete system, some of which might be time non-deterministic at the level of abstraction being considered.

Furthermore, in some situations we might actually be interested in analysing what happens if the good action arrives after the timeout has fired. Consider, for example, that our timeout behaviour is being used to wait for an acknowledgement in a sender process. The component performing good after timeout has fired corresponds to the acknowledgement arriving after the timeout has

expired, which is of course a possible scenario in practical analysis of communication protocols.

The problem with our | | <Timeout1, Component2> solution is that it does not enable us to analysis this situation, rather the system timelocks when Component2 forces the good action to happen. Unfortunately, as mere mortals, we are unable to analyse systems after the end of time!

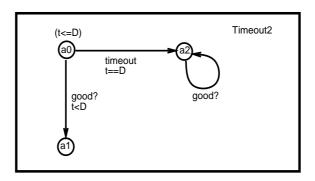


Fig. 5. An UPPAAL Automaton for Timeout2

One way to avoid this timelock is to add "escape" transitions in the timeout. For example, consider the timeout behaviour encapsulated by Timeout2. Now the composition,

| | < Timeout 2, Component 2>

cannot block time. However, this is not a satisfactory solution since rather than Timeout2 just evolving to a single deadlock state, a2, after performing timeout, it could evolve to a complex behaviour; of course in practice it is almost certain to do this. However then, escape transitions would have to be scattered throughout the complex behaviour. This would generate significant specification clutter, which would be compounded if the system contained more than one timeout.

The consequences become particularly severe if the timeout is enclosed in some repetitive behaviour, e.g. see figure 6. This is because, since no assumptions can be made about the time at which the component will want to perform the good action, escape transitions on good will have to be added at a0, a2, b0, b1 (and actually a1 as well). Thus, firstly, the behaviour prior to reaching the timeout has been altered, i.e. escape transitions must be added at b0 and secondly, it is unclear how many escape transitions need to be added to each node in the loop, since state a2 may be reached many times before the first good escape transition is performed.

Urgent Channels. UPPAAL also contains the concept of an urgent channel. The specifier is allowed to denote a particular channel as urgent, which means

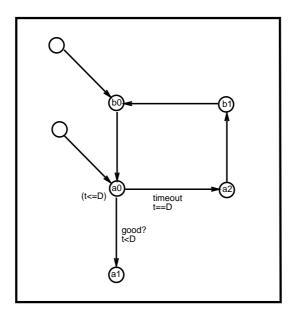


Fig. 6. Timeout2 in a repetitive context

that as soon as synchronisation on that channel can take place, it does. However, UPPAAL restricts the use of such urgent channels. In particular, an urgent transition can only have the guard true.

Intuitively, urgent channels seem to be what we require in order to avoid enforcing urgency in the component process. In particular, they enforce urgency in a "global" manner, rather than requiring it to be enforced in the component process. However, it turns out that the restriction on guarding of urgent channels that UPPAAL imposes prevents derivation of a suitable solution, see [5] which investigates possible solutions with urgent channels which were inspired by the solutions presented in [6].

In summary then, although we do not have a formal proof that a completely satisfactory UPPAAL description of the timeout cannot be found, we postulate that if it is possible, the complexity inherent in the solution would be prohibitive.

4 Timed Automata with Deadlines

A more radical approach to realising a satisfactory bounded timeout is to consider the Timed Automata with Deadlines (TAD) framework developed by Bornot et al [3,4]. The reason for selecting this model is that it is argued that it has very nice properties with regard to time progress and timelocks. In particular, the following property holds,

a state cannot be reached in which neither action or time passing transitions can be performed.

This property is referred to as *time reactivity* and since such situations (as opposed to zeno timelocks) arise through mismatched parallel compositions, it ensures freedom from composition timelocks.

Basic Framework. For a full introduction to TADs, we refer the interested reader to [3, 4]; here we highlight the main principles:

- Deadlines on Transitions. Rather than placing invariants on states, deadlines are associated with transitions. Transitions are annotated with 4-tuples:

where a is the transition label, e.g. good; g is the guard, e.g. $t \le D$; d is the deadline, e.g. t = D; and r is the reset set, e.g. t : = 0. a, g and r are familiar from standard timed automata and the deadline is new. Conceptually, the guard states when a transition is enabled, i.e. may be taken; while the deadline states when it must be taken and taken immediately. It is also assumed that the constraint,

$$d \Longrightarrow g$$

holds, which ensures that if a transition is forced to happen it is also able to. Clearly, if this constraint did not hold then we could obtain timelocks because a transition is forced to happen, but it is not enabled.

Since we have deadlines on transitions there is no need for invariants on states. Thus, they are not included in the framework.

- (Timewise) Priorities. By restricting guards and deadlines in choice contexts, prioritised choice can be expressed. For example, if we have two transitions:

$$b1 = (a1, g1, d1, r1)$$
 and $b2 = (a2, g2, d2, r2)$

then when placing them in a choice context we can give b2 priority over

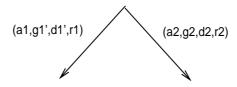


Fig. 7. A Prioritised Choice

b1 by restricting the guards and deadlines of b1, see figure 7. [3] considers a

variety of priority operators, which ensure that if the higher priority action will eventually be enabled within a particular period of time then it takes precedence over competing actions. These different priority mechanisms are obtained by including timed temporal operators in the restricted guards and deadlines. The extreme example of which is to enforce the following restricted guard and deadline:

$$g1' = g1 \land \Box \neg g2 \text{ and } d1' = d1 \land g1'$$

which ensures that b1 is only enabled if g1 holds and there is no point in the future at which g2 will hold.

- Parallel Composition with Escape Transitions. The TADs framework employs a different parallel composition operator to that arising in standard timed automata. The key idea is that of an escape transition. These are the local transitions of automata components that are combined when generating a synchronisation transition. Thus, not only are synchronisations included, but component transitions of the synchronisation are as well. The timewise priority mechanism is then used to give the synchronisation transition highest priority. Intuitively, the escape transitions can only happen if the synchronisation transition will never be enabled. We will illustrate this aspect of TADs shortly.
- Synchronisation Strategies. [3] also consider a number of different synchronisation strategies, but these are not relevant to our discussion. In terms of [3] we only consider AND synchronisation.

In fact, in addition to ensuring time reactivity, the TADs framework limits the occurrence of local deadlocks. Specifically, the escape transitions allow the components of a parallel composition to escape a potential local deadlock by evolving locally. Associated with such avoidance of local deadlocks is the enforcement of maximal progress⁵, which exactly requires that if a synchronisation is possible, it is always taken in preference to a corresponding escape transition.

Basic Definitions. We now briefly review the definition of timed automata with deadlines. Also, in order to preserve some continuity through the paper we continue to use the UPPAAL synchronisation notation even though it is different to that used in [3].

An arbitrary element of A, the set of TADs, has the form:

$$(L, l_0, T)$$

where, L is a finite set of locations; l_0 is the start location; and

 $-T\subseteq L\times CC\times CC\times A^+\times \mathbb{P}(\mathcal{C})\times L$ is a transition relation. A typical element of which is, $(l_1,\mathsf{g},\mathsf{d},\mathsf{a},\mathsf{r},l_2)$, where $l_1,l_2\in L$ are automata locations; $\mathsf{g}\in\mathcal{CC}$

⁵ Note, the term is used in a related but somewhat different way in the timed process algebra setting [12].

is a guard; $d \in \mathcal{CC}$ is a deadline; $a \in A^+$ labels the transition; and $r \in \mathbb{P}(\mathcal{C})$ is a reset set. $(l_1, g, d, a, r, l_2) \in T$ is typically written,

$$l_1 \xrightarrow{\mathsf{g},\mathsf{d},\mathsf{a},\mathsf{r}} l_2$$

In addition, we will use the function:

$$\theta_B(l) = \{ (b,g) \mid \exists l' \cdot l \xrightarrow{g,d,b,r} l' \land b \in B \}$$

Standard TADs. We will introduce a number of different TADs approaches in this paper. These are distinguished by their rules of parallel composition. Here we consider the basic approach, as introduced in [3, 4], which we call *standard TADs*. A TADs expansion theorem for deriving the product behaviour from a parallel composition is given in [3]. Here we give an equivalent inference rule definition for our state vector notation:-

$$(R1) \begin{array}{c} \frac{l_{i} - g_{i}, d_{i}, a?, r_{i}}{||v - g', d', a, r_{i} \cup r_{j}} + ||v ||_{i} - g_{j}, d_{j}, a!, r_{j}}{||v - g', d', a, r_{i} \cup r_{j}} + ||v ||_{i} / l_{i}, l'_{j} / l_{j}]} \\ ||v - g'_{i}, d'_{i}, a?, r_{i} + ||v ||_{i} / l_{i}] \\ ||v - g'_{j}, d'_{j}, a!, r_{j} + ||v ||_{i} / l_{j}] \end{array}$$

where $1 \le i, j \le |v| \land i \ne j$ and,

$$g' = g_i \wedge g_j$$

$$d' = g' \wedge (d_i \vee d_j)$$

$$g'_i = g_i \wedge \Box \neg (g_i \wedge g_j)$$

$$d'_i = g'_i \wedge d_i$$

$$g'_j = g_j \wedge \Box \neg (g_i \wedge g_j)$$

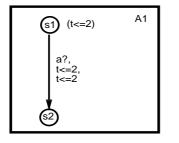
$$d'_j = g'_j \wedge d_j$$

$$(R2) \quad \frac{l_i \xrightarrow{g,d,a,r} l'_i \quad a \in \overline{A} \Rightarrow \bigcup_{k \in (\{1..|v|\} - \{i\})} \theta_{\{\overline{a}\}}(l_k) = \emptyset}{||v \xrightarrow{g,d,a,r} ||v[l'_i/l_i]}$$

where $1 \leq i \leq |v|$. (R1) generates synchronisation and escape transitions with the constrained guards and deadlines ensuring that synchronisation has priority in the required manner. (R2) is the interleaving rule, which is straightforward apart from the second condition which ensures that transitions on incomplete actions are only generated by this rule if synchronisation, and hence rule (R1), is not possible.

As an illustration of these inference rules consider $|\cdot| < A1$, A2> where A1 and A2 are shown in figure 8. The unreduced composition arising from directly applying the inference rules is shown in figure 9(a) (\square is denoted [] and \neg is denoted \sim) and figure 9(b) depicts the resulting composed TAD when guards and deadlines have been reduced by expanding out temporal operators and applying propositional logic. In addition, transitions with unfulfillable guards, e.g. false, have been removed.

We can observe the following:-



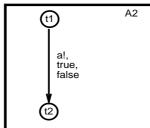


Fig. 8. TADs ${\tt A1}$ and ${\tt A2}$

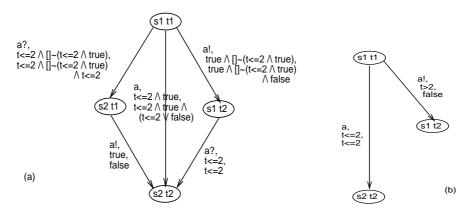
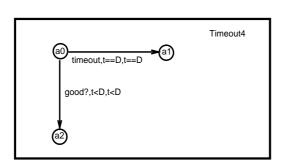


Fig. 9. Unreduced and reduced composition of A1 and A2

- 1. In figure 9(a) the transition coming from s1t1 labelled a is the synchronisation transition.
- 2. In figure 9(a) the two transitions coming from s1t1 labelled a? and a! respectively, are the escape transitions. The first arises from automaton A1 and the second from automaton A2. The guards of these escape transitions ensure that they can only fire if the synchronisation will never in the future be possible. Thus, synchronisation transitions have priority over escape transitions.
- 3. Figure 9(b) shows that since the synchronisation transition inherits the guards of a? from A1, no escape transition on a? is possible. If s1t1 is entered with t>2 then the escape transition on a! can be taken, enabling A2 to escape its local deadlock.

Bounded Timeout in Standard TADs. Now we reformulate our bounded timeout in standard TADs. The component that we consider is Component3 and the timeout is Timeout4 both shown in figure 10.



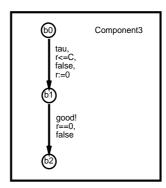


Fig. 10. A TAD for Timeout4 and Component3

So, Component3 behaves similarly to Component2 except the good! transition is not urgent, i.e. the good transition is never forced to happen⁶. In the terminology of [3], such transitions are called lazy. In contrast, all the transitions in Timeout4 are eager [3], since their guard and deadline are the same. This implies that as soon as the transition can happen it will happen.

Now by applying the above inference rules and removing impossible transitions, the composite automaton shown in figure 11 results. The full version of this paper [5] presents the intermediate steps required to derive this composition.

If we first focus on state a0 b1 then we can see that this composite behaviour gives priority to the synchronisation between good? and good! which is indicated by the transition labelled good. Thus, while t<D this is the only transition that can fire (notice r==0 automatically when entering state a0 b1) and furthermore it is eager.

Also, if state a0b1 is entered with t==Dthen timeout is urgent. Furthermore, from this state the action good! can happen (but lazily) either at time D or later. This is the escape transition, which allows Component3 to move out of state b1. Remember the timelock that we obtained previously arose because the component could not exit the state where it wished to perform good! 7.

This solution seems to fulfil our requirements - it is a strong timeout, urgency is enforced as required on both timeout and good and the solution is timelock free. However, there are some peculiarities with the resulting composite behaviour. Consider for example, the transition from a0 b0 labelled good?. This represents the timeout performing its good escape transition. However, con-

⁶ We prefer to enforce the urgency of good in the timeout because in some of our case studies, e.g. [6], there are situations in which enforcing the urgency of good on the system side can cause problems, since nothing ensures that the timeout is ready to synchronise on the good exactly when it is offered. In order to avoid this possibility we require the system to passively offer its action and thus, wait until the timeout is ready to receive it.

⁷ Actually, the situation is not as severe here since good! is lazy.

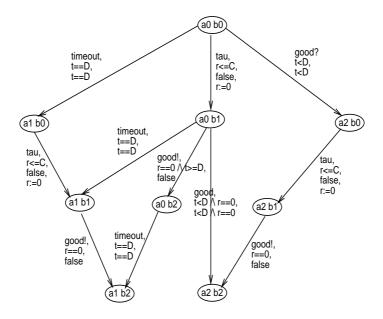


Fig. 11. | | < Timeout4, Component3 > in standard TADs

ceptually it is being performed too early - before the synchronisation on <code>good</code> is even offered. In fact, if <code>a0b0</code> is entered with <code>t==0</code>, which will almost certainly be the case, then <code>good?</code> will almost always be selected since it is an eager transition. In response to this observation we consider alternative TADs formulations in the next section.

5 Alternative TAD Formulations

We consider two alternative TAD formulations⁸. [5] actually considers a third formulation, but this turns out to be unsatisfactory. Both satisfy the requirements that we identified in the introduction for our bounded timeout. Thus, in particular, they are both time reactive. However, the solutions vary in the extent to which they limit local deadlocks.

5.1 Sparse Timed Automata with Deadlines

This is a minimal TADs approach, in which we do not generate *any* escape transitions. Furthermore, since escape transitions are not generated, we do not have to enforce any priority between the synchronisation and escape transitions.

⁸ We still call these timed automata with deadlines, because the basic principles, as concieved by Bornot et al [3, 4], still apply, i.e. placing deadlines on transitions and using prioritised choice.

With sparse TADs the following parallel composition rules are used:

$$\frac{l_i \xrightarrow{a?,g_i,d_i,r_i} l'_i \quad l_j \xrightarrow{a!,g_j,d_j,r_j} l'_j}{||v \xrightarrow{a,g',d',r_i \cup r_j}||v[l'_i/l_i,l'_j/l_j|} \qquad \frac{l_i \xrightarrow{a,g,d,r} l'_i \quad a \in A}{||v \xrightarrow{a,g,d,r}||v[l'_i/l_i]}$$

where
$$1 \le i, j \le |v|, i \ne j, g' = g_i \land g_j$$
 and $d' = g' \land (d_i \lor d_j)$.

These rules prevent uncompleted actions from arising in the composite behaviour; they only arise in the generation of completed actions, while completed actions offered by components of the parallel composition can be performed independently. This definition has the same spirit as the normal UPPAAL rules of parallel composition. The difference being that here we have deadlines which we constrain during composition to preserve the property $d \Rightarrow g$. It is straightforward to see that as long as this property holds, we will have time-reactivity.

Let us consider once again the behaviour,

| | <Timeout4, Component3>

which is the network we were focusing on in the previous section. Now with our new parallel composition rules, we obtain the composite behaviour shown in figure 12. This is an interesting and very reasonable solution. Firstly, it meets all

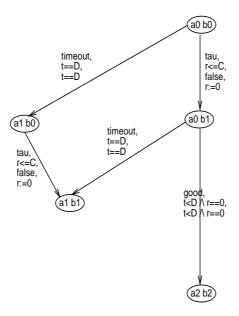


Fig. 12. | | < Timeout 4, Component 3> in Sparse TADs

the requirements identified at the start of this paper for our bounded timeout. Thus, in particular, it is time-reactive. However, it makes no effort to limit local deadlocks, so communication mis-matches yield local deadlocks rather than timelocks.

5.2 TADs with Minimal Priority Escape Transitions

The idea here is to ensure maximal progress as standard TADs do, but rather than just giving escape transitions lower priority than their corresponding synchronisation, we also give them lower priority than other completed transitions. Thus, a component can only perform an escape transition if the component will never be able to perform a completed transition.

The parallel composition rules are:

$$(R1) \quad \frac{l_i \xrightarrow{a?, g_i, d_i, r_i} l'_i \quad l_j \xrightarrow{a!, g_j, d_j, r_j} l'_j}{||v \xrightarrow{a, g', d', r_i \cup r_j}||v[l'_i/l_i, l'_j/l_j]}$$

where, $1 \le i, j \le |v|$, $i \ne j$, $g' = g_i \land g_j$, $d' = g' \land (d_i \lor d_j)$. and,

$$(R2) \quad \frac{l_i \xrightarrow{a,g,d,r} l'_i \ a \in A}{||v \xrightarrow{a,g,d,r}||v||_i'/l_i|} \qquad (R3) \quad \frac{l_i \xrightarrow{a,g,d,r} l'_i \ a \in \overline{A}}{||v \xrightarrow{a,g'',d'',r}||v||_i'/l_i|}$$

where, $1 \le i \le |v|$ and,

$$g'' = g \wedge \bigwedge_{\substack{(b, g') \in \theta_A(l_i) \\ (b, g_1) \in \theta_{\overline{A}}(l_i) \ j \in (\{1..|v|\} - \{i\})}} \Box \neg g' \wedge$$

$$\bigwedge_{\substack{(b, g_1) \in \theta_{\overline{A}}(l_i) \ j \in (\{1..|v|\} - \{i\}) \ (\overline{b}, g_2) \in \theta_{\{\overline{b}\}}(l_j)}} \bigcap \neg (g_1 \wedge g_2)$$

$$d'' = d \wedge g''$$

R1 is the normal synchronisation rule; R2 defines interleaving of completed transitions; and R3 defines interleaving of incomplete, i.e. escape, transitions. In this final rule, g'' holds when,

- 1. g holds;
- 2. it is not the case that an already completed transition from l_i could eventually become enabled; and
- 3. it is not the case that an incomplete transition (including a itself) offered at state l_i could eventually be completed.

Applying these rules to the composition:

| | < Timeout4, Component3>

and removing impossible transitions, see [5] for a full presentation, yields the composition shown in figure 13. This solution removes the excessively early escape transition from a0 b0, but preserves all other transitions.

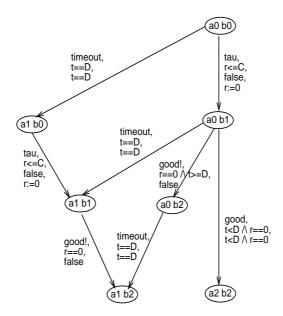


Fig. 13. | | < Timeout4, Component3 > in TADs with minimum priority escape transitions

6 Discussion and Conclusions

We failed to find a fully satisfactory UPPAAL specification of a bounded timeout. In response, we presented three different TADs solutions - standard TADs, sparse TADs, and TADs with minimal priority escape transitions. The latter two of which are new to this paper⁹. All three meet all the requirements we identified at the start of the paper for our timeout. However, our preference is for the 2nd and 3rd solutions. The 2nd is interesting because it gives a timelock free solution but does not seek to minimise local deadlocks, while the 3rd adds escape transitions to limit such local deadlocks.

It is interesting to consider a specific timeout example. In the same way as earlier in the paper, we consider the implications if we view the good action as the passing of an acknowledgment from the medium to a waiting sender process. The situation that the component wishes to perform good after the timeout has fired corresponds to the medium delivering the acknowledgment too late. The two solutions handle this situation differently.

With the sparse TADs solution, a local deadlock is generated. Conceptually, this indicates that the medium is prevented from delivering the acknowledgement. This is in fact the normal manner in which mis-matched communications are handled in untimed systems - local deadlocks result. In contrast, with TADs

⁹ In particular, the *stiff* parallel composition of [13] which seem related to our sparse TADS are in fact rather different since they do not ensure that deadlines imply guards when generating the product. Thus, they do not ensure time reactivity.

with minimal priority escape transitions the late delivery of the acknowledgement yields a local transition in the medium, which could be viewed as the acknowledgement packet being consumed/dropped. This avoids the local deadlock and allows the system to proceed. Choosing between these two should be made according to the application domain under consideration.

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