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Emergence of evolutionary cycles in size-structured food webs

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1 Emergence of evolutionary cycles in size-structured food
2 webs

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8 **Abstract**

9 The interplay of population dynamics and evolution within ecological com-
10 munities has been of long-standing interest for ecologists and can give rise
11 to evolutionary cycles, e.g. taxon cycles. Evolutionary cycling was intensely
12 studied in small communities with asymmetric competition; the latter drives
13 the evolutionary processes. Here we demonstrate that evolutionary cycling
14 arises naturally in larger communities if trophic interactions are present, since
15 these are intrinsically asymmetric. To investigate the evolutionary dynam-
16 ics of a trophic community, we use an allometric food web model. We find
17 that evolutionary cycles emerge naturally for a large parameter ranges. The
18 origin of the evolutionary dynamics is an intrinsic asymmetry in the feeding
19 kernel which creates an evolutionary ratchet, driving species towards larger
20 bodysize. We reveal different kinds of cycles: single morph cycles, and coevo-
21 lutionary and mixed cycling of complete food webs. The latter refers to the
22 case where each trophic level can have different evolutionary dynamics. We
23 discuss the generality of our findings and conclude that ongoing evolution in
24 food webs may be more frequent than commonly believed.

25 *Keywords:* Community Cycling, Taxon Cycles, Coevolution, Red-Queen
26 Dynamics, Evolutionary Limit Cycles

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27 1. Introduction

28 One of the main goals of evolutionary ecology is to gain insights into the
29 interplay of population dynamics and evolution, shaping the structure and
30 dynamics of communities [13, 7]. The outcome of eco-evolutionary processes
31 is not easy to understand from first principles, but much progress has been
32 achieved by theoretical approaches. Of particular interest are the condi-
33 tions under which eco-evolutionary processes within communities give rise to
34 dynamic patterns. Early theoretical studies of evolutionary driven commu-
35 nity dynamics were restricted to simple community-modules of two or three
36 species with fixed species roles and primarily focused on temporal changes
37 in the abundance and mean trait values of different species or populations.
38 These works studied the influence of co-evolution on the stability of predator-
39 prey systems [27, 3, 2], the occurrence of character displacement in models
40 of competition mediated by a quantitative trait [38, 35, 36, 42, 41], as well as
41 the dynamics of co-evolutionary arms races [43]. Further theoretical analysis
42 showed that evolution can also induce temporal changes in the composition
43 and diversity of a community and may either increase species richness, for
44 example via speciation events [31, 11], but may also reduce species richness,
45 for example via self-extinction through evolutionary suicide [24, 15, 25].

46 One major insight of these studies was that the interplay of ecological
47 and evolutionary processes does not inevitably lead to an evolutionary equi-
48 librium, but can lead to a situation of non-equilibrium states, characterized
49 by sustained evolutionary change. One particularly intriguing case is that
50 of evolutionary cycling, which is the emergence of ongoing periodic changes
51 in species traits or community states [12, 19]. In one of the first studies
52 of evolutionary cycling, Rummel and Roughgarden [35] suggested the ap-
53 pearance of community cycles, i.e. the occurrence of evolutionary cycles in
54 the community composition going together with sustained species turnover.
55 Rummel and Roughgarden [35] simulated the buildup of island faunas based
56 on a model of competitive interactions mediated by bodysize as the dominant
57 phenotypic trait. Thereby, one key ingredient for the emergence of commu-
58 nity cycles was attributed to the asymmetry of species interactions, The
59 resulting community cycles, sometimes referred to as taxon cycles [45, 34],
60 describe a scenario where an island (or local habitat), which is initially oc-
61 cupied by a single resident, is colonised by a new invading species of larger
62 bodysize. The invading species forces the smaller resident to evolve to smaller
63 bodysize, while following this evolutionary movement. The resulting coevo-

64 lutionary arms-race towards smaller bodysizes weakens the viability of the
65 resident which is eventually driven to extinction, leading again to a single
66 species community. It was shown that this simple mechanism is able to de-
67 scribe the empirical patterns in the build-up of island faunas in the case of
68 *Anolis* lizards in the Lesser Antilles [34] and was subsequently investigated in
69 a series of further studies (e.g. [36, 42, 41, 24]). In these studies, it was found
70 that community cycles are a robust model outcome, but the details of the
71 cycles depend on the specific model assumptions. In particular, it is possible
72 that the bodysize change of the cycle operates in the reverse direction, so
73 that species are driven towards larger bodysizes.

74 Despite this progress in describing generic mechanisms of evolutionary
75 cycling, the studies mentioned above are limited in several respects. First,
76 most demonstrations of evolutionary community cycles are restricted to small
77 communities, consisting of very few species. Recently, there has been much
78 interest in the evolutionary build-up of community structure in multi-species
79 communities [17, 6, 20, 37, 32]. However, these studies typically observed
80 static community structures, whereas not much is known about the condi-
81 tions that favour the emergence of ongoing evolutionary change and commu-
82 nity cycling in multi-species assemblages [40, 39]. A second related question
83 is whether larger communities can exhibit different coevolutionary processes
84 that occur independently from each other in different community modules,
85 possibly at different frequencies. Finally, even though community cycles have
86 been studied extensively for competitive interactions, not much is known
87 about their relevance in trophically structured communities. This is quite
88 astonishing, given the striking structural similarity of allometric evolutionary
89 food web models [7] to competition models on a niche axis [35, 41].

90 One of the first allometric evolutionary food web models was introduced
91 by Loeuille and Loreau [20] and several variants were studied in great detail
92 [21, 20, 4, 8, 5]. In this model class, similar to (Rummel and Roughgarden
93 [35, 36]), each species is characterized by its bodysize as a major phenotypic
94 trait, the interactions between species are determined by their differences
95 in bodysize, and allometric relations are considered explicitly. The essential
96 new ingredient of allometric food web models is that they not only con-
97 sider competition between species of similar bodysize, but also incorporate
98 trophic interactions between species, so that a large species is able to prey
99 upon smaller species. Given the strong similarity between these two model
100 classes and the fact that predator-prey interactions are naturally asymmet-
101 ric, one would expect that evolutionary community cycles, similar to taxon

102 cycles in models of competition, are a typical outcome in evolutionary food
103 web models. However, while several other studies have reported evolution-
104 ary dynamics in such models, e.g. irregular extinction cascades [5], trophic
105 outbursts [30] and Red Queen dynamics in two species communities [46], to
106 date there has been no rigorous investigation of evolutionary cycling in this
107 framework.

108 In this study, we revisit the well-studied evolutionary allometric food web
109 model by Loeuille and Loreau [20]. We show that this model can indeed pro-
110 duce evolutionary cycles in a large parameter range and that the possibility
111 of evolutionary cycles is related to the competition between species. When
112 Loeuille and Loreau [20] introduced this model, they found food webs that
113 are relatively invariant over time. While these results proved to be robust
114 to a broad range of feeding ranges and competition strength, the rest of
115 the parameter space was relatively unexplored. In particular, the parameter
116 governing the bodysize distance over which morphs can compete, the com-
117 petition range, was limited to rather small values. While some biological
118 justification for this range was given, we argue here that this range may be
119 too small. If competition between species arises from niche overlap (sensu
120 MacArthur and Levins [22]), we should expect a competition range that is
121 significantly broader and is of the same order as the feeding range of a species.
122 This would allow inter-species competition to have a much stronger effect on
123 the evolutionary dynamics.

124 Motivated by this observation, we numerically investigate the evolution-
125 ary behaviour in the model [20], by systematically varying the strength and
126 range of the competition between species. Our simulations show that evolu-
127 tionary cycling, where species are driven towards larger bodysizes, is natu-
128 rally present in the model considered – not only between single species but
129 also in large trophic communities. Thereby, we observe a plethora of regimes
130 with distinct dynamics. Besides static food webs, we observe evolutionary
131 single morph cycles, complex community cycles where different trophic levels
132 undergo separate coevolutionary cycles, as well as transient dynamics. Us-
133 ing invasion analysis and Pairwise Invasibility Plots (PIPs) we are able to
134 support the numerical observations, which allows us to explain the mecha-
135 nism underlying the evolutionary cycles. Our findings imply that ongoing
136 evolution in food webs may be more frequent than commonly believed.

137 **2. Model**

138 We follow the evolutionary food web model by Loeuille and Loreau [20].
 139 The model considers one basal resource, such as an inorganic nutrient, ($i =$
 140 0) and a variable number of evolving morphs ($i = 1, \dots, N$). We use the
 141 term morph, rather than species, since we are not considering the speciation
 142 process. Each morph is described by its population biomass density B_i and
 143 bodysize z_i . The resource has a total density B_0 and is associated with a non-
 144 evolving ‘bodysize’, which is fixed to the value $z_0 = 0$. The model consists of
 145 two components: population dynamics and evolutionary dynamics, each of
 146 which operate on different time scales. The population dynamics describe the
 147 trophic interactions among morphs and determine their respective growth,
 148 survival or extinction. On a longer time-scale, usually after the population
 149 dynamics have reached an attractor, new morphs are added to the community
 150 by an evolutionary algorithm.

151 *2.1. Population dynamics*

The change of biomass B_i of morph i is given by the Lotka-Volterra equations, accounting for reproduction, intrinsic mortality, and losses due to predation and interference competition [20]

$$\frac{dB_i}{dt} = B_i \left(\underbrace{f(z_i) \sum_{j=0}^N \gamma(z_i - z_j) B_j}_{\text{Reproduction}} - \underbrace{m(z_i)}_{\text{Mortality}} - \underbrace{\sum_{j=0}^N \gamma(z_j - z_i) B_j}_{\text{Predation loss}} - \underbrace{\sum_{j=1}^N \alpha(|z_i - z_j|) B_j}_{\text{Competition}} \right). \quad (1)$$

Here, the intrinsic mortality $m(z_i) = m_0 z_i^{-0.25}$ and the production efficiency $f(z_i) = f_0 z_i^{-0.25}$ scale according to allometric relations with bodysize [26]. The function $\gamma(z_i - z_j)$ describes the consumption rate exerted by predator i on prey j . The model assumes that the feeding efficiency decays with the bodysize difference as a one tailed Gaussian function

$$\gamma(z_i - z_j) = \begin{cases} \frac{\gamma_0}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(z_i - z_j - d)^2}{\sigma^2}\right), & z_i > z_j, \\ 0, & z_i \leq z_j, \end{cases} \quad (2)$$

152 where d is the optimal predator-prey bodysize distance, γ_0 can be used to
 153 scale the maximal consumption strength, and σ describes the feeding range

154 of a morph (i.e., the Gaussian function has standard deviation of $\sigma/\sqrt{2}$). The
 155 cut-off for $z_i \leq z_j$ in the feeding kernel implies that a predator is only able
 156 to consume prey with a strictly smaller bodysize. This causes an asymmetry
 157 in trophic interactions, giving the larger of two similar sized morphs a small
 158 advantage since it can consume, but cannot be consumed by, the smaller
 159 one. Additionally, we also tested a smooth feeding kernel. Our numerical
 160 simulations revealed that our main conclusions are valid also for a smooth,
 161 but asymmetrical feeding kernel (see Fig A.7).

The function $\alpha(|z_i - z_j|)$ describes interference competition between two
 morphs i and j . It is modelled as a symmetric rectangular function (the
 competition kernel) of bodysize differences

$$\alpha(|z_i - z_j|) = \begin{cases} \alpha_0, & |z_i - z_j| < \beta, \\ 0, & |z_i - z_j| \geq \beta, \end{cases} \quad (3)$$

162 where α_0 is the competition strength and β the competition range.

The change in the density of the resource $i = 0$ follows a chemostat
 equation

$$\begin{aligned} \frac{dB_0}{dt} = & I - eB_0 - \sum_{j=1}^N \gamma(z_j) B_j B_0 + \nu \sum_{j=1}^N \sum_{i=1}^N \alpha(|z_j - z_i|) B_j B_i \\ & + \nu \sum_{j=1}^N m(z_j) B_j + \nu \sum_{j=1}^N \sum_{i=1}^N (1 - f(z_j)) \gamma(z_j - z_i) B_j B_i, \end{aligned} \quad (4)$$

163 consisting of a constant resource inflow I , a relative outflow of rate e , losses
 164 due to consumption by morphs, and three terms describing the recycling of a
 165 fraction ν of dead biomass from interference competition, intrinsic mortality,
 166 and consumption.

167 In this model, the interaction kernels for feeding and competition are both
 168 discontinuous. This discontinuity could influence the population dynamics
 169 and thus the evolutionary behaviour. However, we find that our results are
 170 qualitatively unchanged when these discontinuous functions are replaced with
 171 continuous functions (see Fig A.7).

172 2.2. Evolutionary dynamics

173 The system is initialized with the resource (trait value $z_0 = 0$ and ini-
 174 tial biomass $B_0 = I/e$) and a single evolving morph of bodysize $z_1 = d$,

175 corresponding to a maximal consumption rate on the resource. Each morph
 176 mutates at a constant rate of ω_0 per unit biomass and unit time. At each mu-
 177 tation event of a morph k , a new morph is added to the system with bodysize
 178 z_M that is randomly chosen from the mutation interval $[0.8 z_k, 1.2 z_k]$. This
 179 interval is centred around, and increases linearly with, the bodysize of the
 180 mutating morph z_k . The new morph is introduced with an initial biomass of
 181 θ , which is also the extinction threshold. If due to the population dynamics
 182 the biomass B_k of any morph falls below this threshold θ , it is considered
 183 extinct and removed from the system.

184 *2.3. Parameter values, implementation, and cycle detection*

185 We varied the range β and the strength α_0 of the competition kernel
 186 as our main control parameters. The other model parameters are fixed to:
 187 $f_0 = 0.3$, $m_0 = 0.1$, $\gamma_0 = 1/\sqrt{2}$, $d = 2$, $I = 10$, $e = 0.1$, $\nu = 0.5$, and
 188 $\sigma = \sqrt{2}$. In contrast to Loeuille and Loreau [20] we increased the extinction
 189 threshold from $\Theta = 10^{-20}$ to $\Theta = 10^{-10}$ (see also Allhoff and Drossel [4])
 190 and the mutation rate from $\omega_0 = 10^{-6}$ to $\omega_0 = 10^{-5}$. Our robustness tests
 191 showed that these deviations from the original model formulation have no
 192 effect on the model outcome, but they allowed us to substantially increase
 193 the evolutionary time considered over our simulation runs. If not stated
 194 elsewhere, the simulations were carried out over 10^9 time-units. Numerical
 195 simulations were performed using a Runge-Kutta-Fehlberg method 4/5 [28]
 196 which was implemented in C++.

197 We say that we observe an evolutionary cycle if a simulated time series
 198 contains at least one whole period of a cycle after an initial build up phase of
 199 10^8 time-units. Therefore, the maximal observable period length is limited
 200 by the remaining $9 \cdot 10^8$ time-units. If the period length of a cycle is close
 201 to this limit, cycling is difficult to detect and can depend on the build-up
 202 phase. To aid detection, we consider 5 realisations per parameter set with
 203 different seeds for the random numbers in the evolutionary algorithm. If
 204 any of these runs displays cycling we classify the parameter set as producing
 205 cycling behaviour. Thus, the distinction between static and cycling food
 206 webs depends on the time interval and the threshold condition (one period)
 207 used, especially in the transition regions.

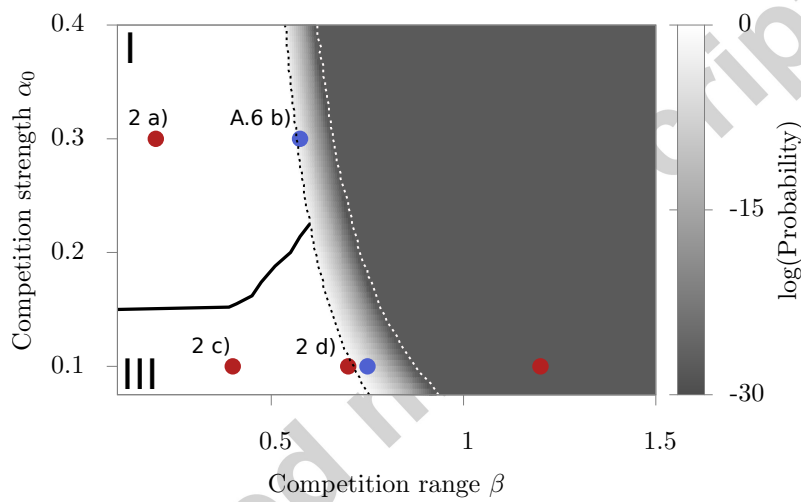


Figure 1: Map of the evolutionary behaviour in dependence of the competition parameters. The map splits into four regions of distinct dynamic behaviour: Static food webs (region I), single morph cycles (region II), complex community dynamics (region III), and a transition regime in which single morph cycles occur but the system eventually becomes polymorphic (region IV). The black solid line separates the regions of static (region I) and cyclic (region III) polymorphic food webs and is obtained from numerical simulations. The grey scale indicates the probability P for a monomorphic system to become dimorphic during one cycle period and is calculated by analysis of the invasion fitness in a monomorphic system (see section 3.2). The black dotted line shows the isocline of $P = 1$. To the right of this line single morph cycles can occur. The white dotted line indicates the isocline of $\log P = -30$ and separates regions II and IV. The red dots correspond to the examples shown in Fig. 2 and the blue dots to the transition states shown in Fig. Appendix A.6.

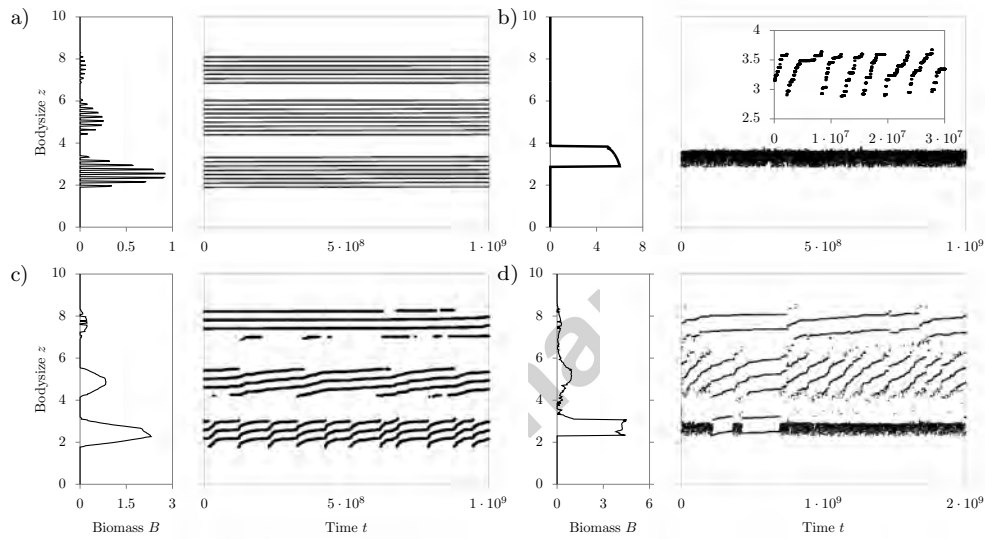


Figure 2: Evolutionary food web dynamics for different competition parameters β and α_0 . Each subplot (**a-d**) corresponds to the parameter combination of a red point in Fig. 1 and shows the time evolution of bodysizes of all morphs after the initial build-up phase (right) and the corresponding biomass-body size histograms (left). **a)** Static food web, as in [20], for $\alpha_0 = 0.3$ and $\beta = 0.2$. **b)** Single morph cycles ($\alpha_0 = 0.1$ and $\beta = 1.2$). The inset shows a close-up of the simulated cycle in bodysize for a shorter time range. **c)** Complex community dynamics, showing different coevolutionary cycles in each trophic level ($\alpha_0 = 0.1$ and $\beta = 0.4$). The vertical lines mark time-points at which the two largest morphs in the lowest trophic level are within competition range. **d)** Mixed evolutionary cycle, showing the coexistence of a single morph cycle in the lowest trophic level and coevolutionary cycles in the higher trophic levels ($\alpha_0 = 0.1$ and $\beta = 0.7$).

208 3. Results

209 3.1. Numerical simulations, revealing four dynamics regions

210 We used numerical simulations to study the dependence of the evolution-
 211 ary dynamics of the food web model on inter-species competition. Exploring
 212 the parameter space (β, α_0) of the competition kernel, we identified four
 213 distinct behavioural regimes (regions I - IV). The regions in which each of
 214 these behaviours occur are presented in Fig. 1 and exemplary time series for
 215 all regimes are shown in Figs. 2 and A.6. Region I is characterized by the
 216 build-up of evolutionary and convergence stable food webs, as introduced by
 217 Loeuille and Loreau [20]. Region II exhibits single morph cycles. In this
 218 region the community is composed of the resource and a monomorphic con-
 219 sumer with a bodysize that is not constant but undergoes evolutionary cycles
 220 within a narrow range. Region III features complex community dynamics.
 221 This region is characterized by co-occurring single morph and polymorphic
 222 coevolutionary cycles that cover several trophic layers. Region IV is a tran-
 223 sition area in which an initial period of single morph cycles eventually gives
 224 way to a polymorphic community. The resulting food webs can be evolu-
 225 tionarily static or dynamic. Our numerical simulations showed that the map
 226 of evolutionary outcomes in Fig. 1 is generic towards parameter variation
 227 (e.g. σ, γ_0). That is, while the size of the regions may change, as long as the
 228 parameters chosen allow trophic structure each of these types of behaviour
 229 can be found. We consider each state, and the transition between states, in
 230 more detail below.

231 *Static food webs: region I.* For small competition ranges β and high com-
 232 petition strengths α_0 (region I) we obtain food webs that are close to an
 233 evolutionarily and convergence stable state. This is exactly the behaviour
 234 observed by Loeuille and Loreau [20]. Fig. 2a shows an example time series
 235 for a static food web and its distribution of biomass relative to bodysize.
 236 After an initial build-up (not shown), the network structure and morph com-
 237 position of the food web is practically static. It consists of several distinct
 238 bodysize clusters, each centred at a bodysize which is a multiple of the op-
 239 timal feeding distance d . These clusters are analogous to trophic levels. In
 240 particular, a morph in a given cluster predominantly consumes morphs in the
 241 cluster immediately below it and, similarly, is mainly consumed by morphs
 242 in the cluster immediately above it. Trophic levels are further separated into
 243 sharp bodysize layers. That is, morphs in the same trophic level are sepa-
 244 rated by a bodysize distance of β , which allows them to avoid interference

245 competition (note that here β is much smaller than the optimal feeding dis-
 246 tance d). In the left panel of Fig. 2a, we plot the average biomass of morphs
 247 of a given bodysize throughout the simulation. This distribution is com-
 248 posed of single peaks indicating that the morph composition is static after
 249 the initial build up of the network. The envelope of all peaks within a trophic
 250 level is bell shaped. This arises due to differences in growth rate within the
 251 trophic level; morphs close to the centre of a trophic level are at the optimal
 252 feeding distance to the centre of the trophic level below and thus are able to
 253 grow faster. The total biomass of a trophic level decreases with increasing
 254 bodysize, due to efficiency losses.

255 In the example given, the trophic levels are distinct. Increasing the feed-
 256 ing range σ , or competition strength α_0 causes the trophic levels to widen
 257 until the trophic levels merge. As the competition range β increases, the
 258 bodysize distance between morphs within a trophic level increases and fewer
 259 morphs can coexist in each level. For sufficiently large β only a single morph
 260 can exist in the system and we enter region II.

261 *Single morph cycles: region II.* For large competition ranges β (region II) we
 262 observe a new dynamic regime for this model, which we term single morph
 263 cycles. This regime is characterized by a dynamic monomorphic community
 264 that consists of the basal resource (of bodysize $z_0 = 0$) and a single consumer
 265 morph with a bodysize that is not constant but undergoes an evolutionary
 266 cycle, see Fig. 2b. The inset shows a close-up of the time series which displays
 267 the bodysize cycle more clearly. In addition, a close-up of the temporal
 268 evolution of the bodysize and biomass over four complete periods of the cycle
 269 is shown in the Appendix (Fig. A.5). At the beginning of a cycle, starting
 270 with a small initial bodysize, the resident is repeatedly replaced by a slightly
 271 larger morph. As the resident's bodysize increases, its biomass decreases,
 272 as seen in the trapezoidal structure of the biomass-bodysize distribution in
 273 the left panel of Fig. 2b and in Fig. A.5b in the Appendix. At the end of a
 274 cycle, the now large resident is invaded and outcompeted by a small mutant
 275 and the single morph cycle resets. The mechanism underlying this behaviour
 276 is discussed in Section 3.2. In contrast to region I, the biomass-bodysize
 277 distribution is continuous and not composed of single peaks, because morphs
 278 occur across the whole bodysize range of a cycle.

279 With increasing competition strength α_0 the frequency and amplitude of
 280 the cycle decrease (not shown). The amplitude also decreases with decreasing
 281 feeding range σ , but cycles are still present for $\sigma < 0.5$. We note that the

282 competition range β always encompasses the entirety of the bodysize range of
 283 a single morph cycle. As β decreases we eventually reach a threshold where
 284 the system can support a polymorphic food web and enter either region I or
 285 region III.

286 *Complex community dynamics and coevolutionary cycles: regions III and*
 287 *IV.* For low competition strength α_0 and small to intermediate competition
 288 range β we obtain a regime of complex community dynamics (region III),
 289 characterized by polymorphic food webs which are evolutionarily dynamic.
 290 Example time series for this region are plotted in Figs. 2c and d. In this
 291 regime, each trophic level within the food web undergoes an evolutionary
 292 cycle. This can be a single morph cycle, as described in the previous section
 293 (e.g., the lowest trophic level in Fig. 2d), or a coevolutionary cycle, in which
 294 the trophic level consists of multiple coevolving morphs (e.g., the lowest
 295 trophic level in Fig. 2c).

296 A close-up of the temporal dynamics of bodysizes and biomasses during
 297 a coevolutionary cycle is shown in Fig. 3. At the beginning of the cycle,
 298 the bodysizes of all morphs within the trophic level increase gradually in
 299 successive interdependent mutational steps, while maintaining a constant
 300 bodysize distance equal to the competition range. Initially this increase is
 301 gradual until, eventually, the largest morph goes extinct. The remaining
 302 morphs then rapidly increase their bodysize to fill this vacated niche. This
 303 effect cascades down to each of the smaller morphs allowing them to increase
 304 their bodysizes at a similar rate. This upwards movement also leaves a niche
 305 at small bodysize which a new morph can invade, which functionally resets
 306 the cycle to its initial state. The biomasses of the larger two morphs decrease
 307 as their bodysize increases (e.g. red curve in Fig. 3). This is because as their
 308 bodysize increases they move away from the optimal distance at which to
 309 feed on the next lowest trophic level. In contrast, the biomass of the smallest
 310 morph increases (e.g. blue or yellow curves), as it approaches the optimal
 311 feeding distance. The biomass of the intermediate morph (e.g. black or blue
 312 curves) stays relatively constant, as its bodysize moves from one side of the
 313 optimal feeding distance to the other.

314 While this describes the coevolutionary cycle within a trophic layer, dif-
 315 ferent trophic levels within a food web undergo independent cycles. Fig. 2c,
 316 for example, shows a food web in which only coevolutionary cycles occur.
 317 The network has basically the same structure as in the static case, consisting
 318 of three trophic levels (Fig. 2a), but it is evolutionarily dynamic. Within a

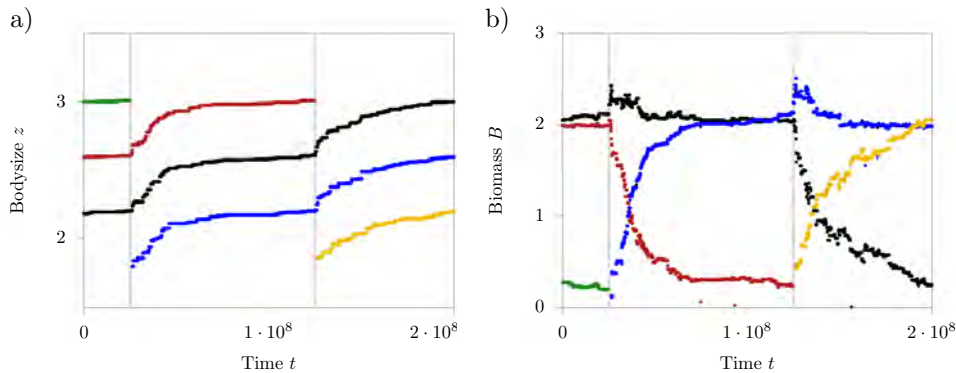


Figure 3: Evolutionary dynamics during a coevolution cycle. **a)** Close-up of the time evolution of morph bodysizes $z_i(t)$ within one trophic layer, here shown for the first trophic level of Fig. 2c. **b)** Corresponding time evolution of morph biomasses $B_i(t)$. Identical colours denote evolutionary akin morphs. The vertical lines mark time instances at which the two largest morphs in this trophic layer have a bodysize distance smaller than β . At these points the largest morph goes extinct and a new morph with smaller bodysize can invade the system.

319 trophic level, morphs coevolve, increasing their bodysize together, but these
 320 coevolutionary dynamics seem to be independent of the cycling within other
 321 trophic levels. In particular, the frequency of these cycles decreases with
 322 trophic level; about two or three cycles of the lowest trophic level occur for
 323 every single cycle of intermediate trophic level, while the highest trophic level
 324 is nearly static. This decrease reflects the fact that the overall mutation rate
 325 decreases with trophic level since, as observed in the static case (region I),
 326 the biomass of each successive trophic level is less than that of the previous
 327 one. In contrast to the static case, the cycling causes the biomass-bodysize
 328 distribution to become continuous as for single morph cycles (region II). This
 329 biomass distribution does not vary through a cycle, and, as a consequence
 330 the cycling of lower trophic levels does not influence higher trophic levels.

331 Coevolution cycles arise in food webs when the competition strength α_0
 332 and the competition range β are low (see Fig.1). They also occur if α_0
 333 is zero. As for single morph cycles, when α_0 increases the frequency and
 334 amplitude of a coevolution cycle decreases, until at sufficient large values of
 335 α_0 the different trophic layers of the food web become evolutionarily static
 336 in a series of successive infinite period bifurcations. Finally, when a critical
 337 threshold is passed the system enters region I. On the other hand, starting
 338 again in region III, with increasing β fewer morphs can exist in a trophic level
 339 (in an analogous way to that described in Section 3.1). As a consequence, the

340 frequency of these cycles slightly increases with β because with decreasing
 341 number of morphs but constant nutrient input, each morph can acquire a
 342 higher biomass, which increases the mutation rates and the evolutionary
 343 speed. Finally, for sufficiently large β we observe the collapse of the whole
 344 polymorphic system into a single morph cycle (region II).

345 For intermediate values of β , it is also possible for the lowest trophic level
 346 to transition to single morph cycles, while the other trophic levels are un-
 347 affected, see Fig. 2d. We call such cases mixed evolutionary cycles. Food
 348 webs undergoing mixed evolutionary cycling have clear similarities to those
 349 displaying purely coevolutionary cycling. In Fig. 2d we still see three distinct
 350 trophic levels with continuous biomass-bodysize distributions. However, the
 351 upper two trophic levels are much closer together than in the purely coevolu-
 352 tionary case. In addition, while the biomass-bodysize distributions of these
 353 levels remain bell shaped the distribution for the lower trophic level is ap-
 354 proximately rectangular, a clear precursor to the trapezoidal form obtained
 355 for single morph cycles, see Fig. 2b. Note that the lower trophic level can
 356 occasionally support a second resident, see Fig. 2d at time $t = 5 \cdot 10^8$. The
 357 single morph cycle stops and both residents increase in bodysize. Eventu-
 358 ally the bigger morph goes extinct, as in a coevolution cycle, and the single
 359 morph cycle starts again. The origin of mixed evolutionary cycles can be ex-
 360 plained by the observation that the lowest trophic level is subject to especially
 361 strong predation pressure because its residents can be consumed by morphs
 362 in all higher trophic levels. Predation and competition strength, α_0 , have
 363 the same structure, so the effect of higher predation is similar to imposing a
 364 higher value of α_0 on the lowest trophic level. As a consequence, by compar-
 365 ison with Fig. 1, this trophic level can collapse into a single morph cycle for
 366 a value of β at which the higher trophic levels still perform coevolutionary
 367 cycles.

368 The transition into region II, by further increase of β , is characterized
 369 by a region of transient single morph cycles (region IV). In this regime,
 370 we can observe single morph cycles that persist only for a finite time and
 371 eventually become polymorphic. The resulting polymorphism can be either
 372 evolutionarily static or dynamic, depending on the competition strength α_0 .
 373 If decreasing β returns the system to region III, as above, we obtain a mixed
 374 evolutionary cycle (see example time series in Fig. A.6a). Alternatively, if
 375 decreasing β returns the system to region I then we will obtain a static food
 376 web (see Fig. A.6b). As β increases, the probability that a polymorphic state
 377 emerges from these single morph cycles declines, eventually reaching zero as

378 the system enters region II.

379 *3.2. Invasion analysis*

Anatomy of a Single Morph Cycle. The existence of evolutionarily dynamic food webs has not previously been observed in this model. In this section we seek to develop an understanding of these dynamic states. We start by considering single morph cycles, which are characterized by a monomorphic system that undergoes a sequence of replacements of a resident, z_R , by a slightly larger mutant, z_M . Eventually this gradual increase in resident bodysize ends when a small morph is able to invade and the cycle resets (Fig. 2b). To gain insight into this process, we consider the invasion fitness $s(z_M, z_R)$ of a mutant z_M in a monomorphic system of bodysize z_R [14]. The invasion fitness $s(z_M, z_R)$ can be derived from Eq. (1) and is given by:

$$\begin{aligned} s(z_M, z_R) = & f(z_M) \gamma(z_M) B_0 + f(z_M) \gamma(z_M - z_R) B_R - m(z_M) \\ & - \gamma(z_R - z_M) B_R - \alpha(|z_M - z_R|) B_R. \end{aligned} \quad (5)$$

380

381 Here, B_0 and B_R denote the equilibrium biomasses of the resource and the
382 resident in the monomorphic system and are given by Eqs. (1) and (4). To
383 gain analytically tractable expressions for the invasion fitness, we neglect the
384 nutrient recycling terms in Eq. (4), that is we take ν equal to zero.

385 A positive invasion fitness $s(z_M, z_R) > 0$ indicates that the mutant is able
386 to invade and establish itself. Assuming that the population stays monomor-
387 phic, we can use Eq. (5) to construct the bodysize ranges which characterize
388 a viable mutant for a given resident bodysize. These ranges can be summa-
389 rized graphically using Pairwise Invasibility Plots (PIP) [14]. In Fig. 4a we
390 plot a PIP for the parameter set used to obtain Fig. 2b. Using this PIP
391 we find that the evolutionary cycle can be split into two phases as follows.
392 Phase 1: For small resident bodysizes ($z_R < 3.54$) only mutants with larger
393 bodysizes have positive fitness. Thus, the resident's bodysize increases over
394 evolutionary time via a series of replacements by a larger mutant (blue arrow
395 in Fig. 4a). Phase 2: When the resident's bodysize reaches a critical value
396 ($z_R \geq z_J = 3.54$), a second positive fitness region emerges corresponding
397 to mutants which are smaller than the resident. At this point a jump to a
398 smaller bodysize becomes possible (green arrows in Fig. 4a). Such a jump
399 can produce a resident morph small enough to return the cycle to its initial

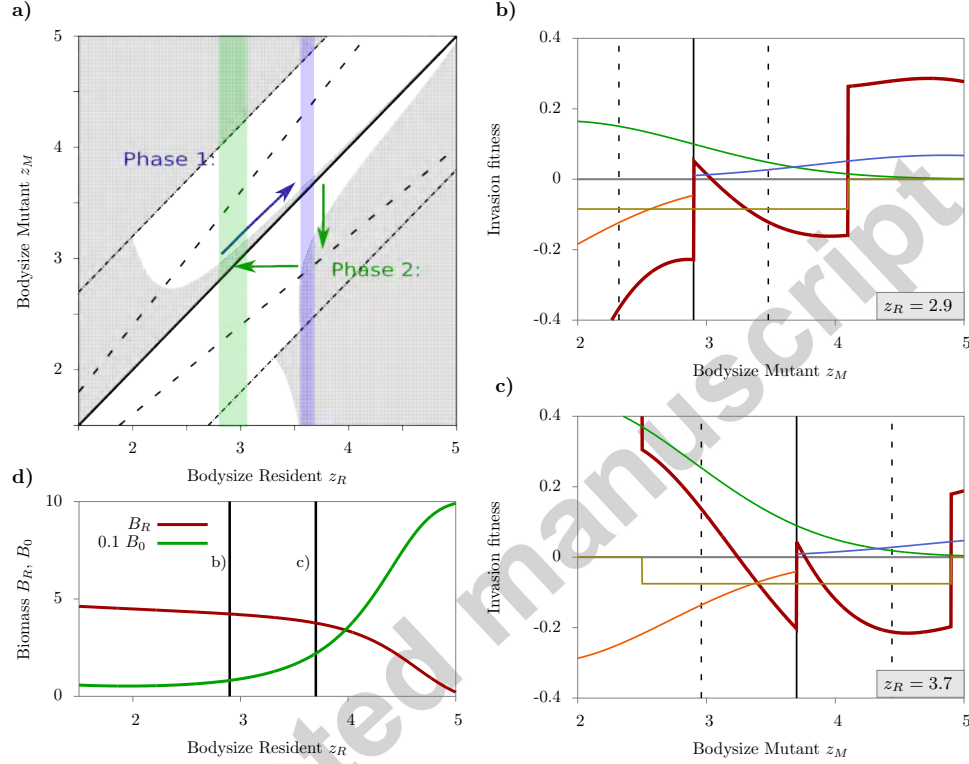


Figure 4: Invasion analysis of a single morph cycle. **a)** Pairwise Invasibility Plot (PIP) in dependence of the bodysize of the resident z_R and of the mutant z_M . Regions with negative invasion fitness, $s(z_M, z_R) < 0$, are marked in white and regions with $s(z_M, z_R) > 0$ in grey. The bold line designates the points at which mutant and resident have identical bodysizes ($z_M = z_R$), dashed lines enclose the mutation interval ($0.8z_R$ and $1.2z_R$), and dashed-dotted lines the competition range ($z_R \pm \beta$). The arrows outline trajectories during a single morph cycle. The shaded areas delineate the variance of bodysizes during a cycle, where a resident may exceed the jump point (blue shaded area) or have varying initial bodysize (green shaded area). **b, c)** Fitness landscape as a function of the mutant's bodysize z_M , at the beginning of a cycle for $z_R = 2.9$ (**b**) and close to the end for $z_R = 3.7$ (**c**). The plot shows the invasion fitness (red) and its composition by growth due to resource consumption (green) and predation (blue) and by losses due to predation (orange), and interference competition (yellow), according to Eq. (5). For visualization all growth terms are rescaled by a factor of 0.2. The vertical solid line marks the bodysize z_R of the resident and the two dashed lines border the mutation interval. **d)** Equilibrium biomass of the resident, B_R , and of the resource, B_0 , as a function of z_R . The vertical lines mark the values of z_R corresponding to panels **b**) and **c**). Parameter values are $\beta = 1.2$, $\alpha = 0.1$, corresponding to Point 2b in Fig. 1.

400 state. Having outlined the cycle we now consider its two phases in more
 401 detail.

402 In Fig. 4b we plot the invasion fitness (i.e., a cross-section of the PIP)
 403 for a typical point ($z_R = 2.9$) in Phase 1 of the cycle. The dependence of
 404 the invasion fitness $s(z_M, z_R)$ on the bodysize of the mutant z_M (red curve)
 405 shows a non-monotonic behaviour, which can be explained by the way in
 406 which $s(z_M, z_R)$ is composed by different gain and loss terms in Eq. (5). We
 407 see that the effects of intrinsic mortality (purple) and competition (grey)
 408 are relatively constant with respect to mutant bodysize, at least within the
 409 mutation interval. Note though, that the competition loss disappears for
 410 $z_M > z_R + \beta$, giving rise to the upward jump of the invasion fitness at
 411 $z_M = 4.1$. Here, this region of increased invasion fitness is outside of the
 412 mutation interval and does not interfere with the single morph cycle. Growth
 413 due to resource consumption (green) declines gradually with mutant size,
 414 as larger morphs have lower resource feeding efficiency (the size difference
 415 becomes larger than the optimal feeding distance $z_M - z_0 > d$). The most
 416 significant factor is the effect of asymmetry in the predation interactions. In
 417 particular, mutants that are larger than the resident are able to increase their
 418 growth by feeding on it (blue), while mutants smaller than the resident suffer
 419 from predation by the resident (orange). This results in an upward jump of
 420 the invasion fitness at $z_M = z_R$, which is sufficient to off-set the moderated
 421 decay in feeding efficiency creating a region of positive invasion fitness for
 422 increased bodysizes $z_M > z_R$. Consequently, the only viable evolutionary
 423 path in Phase 1 is increasing bodysize (blue arrow).

424 With increasing bodysize of the resident z_R , the decline in the feeding
 425 efficiency on the resource becomes more severe because the deviation from
 426 the optimal feeding distance to the resource increases. As a consequence,
 427 the invasion fitness is increasingly dominated by the relative contribution of
 428 the feeding efficiency (green). In contrast, the jump in the invasion fitness
 429 at $z_M = z_R$ due to the asymmetry of predation remains largely independent
 430 of z_R . As a consequence, the region of positive fitness for larger mutants
 431 ($z_M > z_R$) shrinks with increasing z_R (see Figs. 4a and c). Using analyti-
 432 cal and numerical calculations (not shown) we found that this region finally
 433 disappears for a resident bodysize of $z_{max} = 5.09$ (independent of the com-
 434 petition parameters α_0 and β). As such z_{max} is the maximal achievable
 435 bodysize of a morph in a monomorphic system for the given parameter val-
 436 ues. Furthermore note that the probability of an evolutionary change, and
 437 hence the speed of the evolutionary dynamics, is proportional to the ratio

438 of the positive fitness interval to the mutation interval. Thus, as the fitness
 439 interval for larger morphs shrinks, the rate of increase in resident bodysize
 440 decreases, going to zero as z_R approaches z_{max} .

441 These effects stem from the apparently paradoxical observation that,
 442 while increasing bodysize is evolutionarily favoured, it results in a less fit
 443 resident. The larger resident's lower feeding efficiency results in it being less
 444 able to exploit the remaining resource at z_0 . Consequently, as resident body-
 445 size, z_R , increases, resident biomass and utilization of the resource decline.
 446 This effect can be seen clearly by plotting resident and resource biomass
 447 against resident bodysize, see Fig. 4d.

448 The increased availability of the resource is responsible for the emergence
 449 of a second positive fitness interval found in Phase 2 of the cycle. A typical
 450 invasion fitness profile is plotted in Fig. 4c. The contributions of most growth
 451 factors are similar to those obtained in Phase 1 (Fig. 4b). However, now the
 452 growth due to resource consumption depends more strongly on mutant size
 453 and its maximum contribution is much higher. For sufficiently small mutants
 454 the extra growth gained from greater feeding efficiency is able to off-set the
 455 increased losses from predation, allowing a smaller mutant to displace the
 456 resident (green arrows). We refer to the smallest resident bodysize for which
 457 this is possible as the jump point z_J (for the chosen parameter values $z_J =$
 458 3.54). When a mutant with bodysize less than this threshold successfully
 459 invades the system, the system resets to Phase 1.

460 Note that, since mutational steps are random, the range of bodysizes dur-
 461 ing an evolutionary cycle varies. The resident's bodysize can exceed the jump
 462 point before the smaller mutant invades (blue shaded area in Fig. 4a). Fur-
 463 thermore, the smaller mutant can occur anywhere within the positive region
 464 of the fitness cross-section obtained for a given resident. The combination
 465 of these two effects allows the smaller mutant to emerge in a relatively wide
 466 range (green shaded area in Fig. 4a).

467 We observed previously that the frequency of single morph cycles was
 468 related to the competition strength α_0 . This can now be explained as fol-
 469 lows. Note first that once the jump point is reached the cycle can be reset
 470 in a single step. Furthermore, such a reset has a high probability, since the
 471 positive fitness region for the smaller mutant is bigger than that for a larger
 472 mutant. Thus, the system is unlikely to spend a significant amount of evo-
 473 lutionary time in Phase 2. Consequently, the length of a cycle is primarily
 474 determined by the number of evolutionary steps required to produce a resi-
 475 dent with bodysize greater than z_J . The region of positive fitness larger than

476 the resident, which is responsible for the upwards movement (see Figs. 4a
 477 and c), narrows with increasing competition strength α_0 (because the fitness
 478 landscape is shifted downwards within the competition range). Therefore
 479 increasing the competition strength reduces the evolutionary speed and thus
 480 the frequency of the cycle.

481 In summary, the intrinsic asymmetry in the feeding kernel $\gamma(\cdot)$ in Eq. (3)
 482 creates an evolutionary ratchet, which results in an increase in the resident's
 483 bodysize. However, the concomitant decrease in resident feeding efficiency
 484 generates a nutrient environment which ultimately allows the invasion of a
 485 small mutant. The interplay between these two processes results in a single
 486 morph evolutionary cycle.

487 *Transition region to dimorphic states.* While in single morph cycles the mu-
 488 tant always replaces the resident, we observed that in region IV single morph
 489 cycles can become polymorphic. While the dynamics of such a polymor-
 490 phic state are analytically intractable (at least using the techniques outlined
 491 above), we are able to determine conditions under which a dimorphic state
 492 can form. In particular, in this model two species are able to coexist only
 493 if they do not compete directly; that is if the distance between their body-
 494 sizes is greater than the competitive range, β . Thus a dimorphism becomes
 495 possible when the mutation interval, $[0.8z_R, 1.2z_R]$, contains the competition
 496 interval, $[z_R - \beta, z_R + \beta]$. We call the smallest resident bodysize where this
 497 condition holds the dimorphic point, z_D , and note that it is related to the
 498 competition range as follows, $z_D = 5\beta$. With this in mind the transitory sin-
 499 gle morph cycles found in region IV can be explained by the random nature
 500 of the mutational steps. In particular, when $z_D > z_J$ the resident bodysize
 501 must increase past z_J in order to reach the dimorphic point. Consequently
 502 the system must enter Phase 2 and thus the possibility of the cycle reset-
 503 ting before the system becomes polymorphic exists. The further above z_D
 504 from z_J the more likely it becomes that the cycle resets before it becomes
 505 dimorphic. This intuition is justified formally below.

506 In Fig. 1, we plotted the probability of a single morph cycle becoming di-
 507 morphic during a single cycle. This probability was estimated as follows: for
 508 a fixed resident bodysize, the probability for a given mutational step attain-
 509 ing a particular evolutionary outcome (dimorphism, upwards or downwards
 510 movement in bodysize) is given by the range in the invasion fitness that leads
 511 to the evolutionary event divided by the whole positive fitness area. The neg-
 512 ative fitness area is not considered since an unsuccessful invasion does not

513 alter the system. We start with a resident of a bodysize of z_J and calculate
 514 the probability of each evolutionary outcome (transition probability) for that
 515 resident bodysize. In the next step, we increase the resident bodysize by the
 516 expected mutational step-size of the upwards movement. (This is given by
 517 the centre of the positive fitness responsible for upwards movement.) Thus
 518 we calculate the transition probabilities at each of the expected bodysizes
 519 between z_J and z_{max} and by doing this consecutively we consider all possible
 520 evolutionary trajectories. These trajectories terminate when a dimorphism
 521 emerges or the cycle resets (which is assumed to happen via a downwards
 522 movement). The probability to become dimorphic along a given trajectory
 523 is equal to the product of the transition probabilities of the steps in that tra-
 524 jectory. The overall probability of reaching a dimorphic state is then given
 525 by summing over all trajectories which reach this state.

526 *Complex Community Dynamics.* In region III we observe food webs that
 527 contain coevolutionary, and occasionally single morph, cycles. We have pre-
 528 viously observed that the cycles in distinct trophic levels are independent. As
 529 such the behaviour of single morph cycles, even in a polymorphic system, can
 530 be adequately understood in a monomorphic context, see above. Moreover,
 531 the dynamic patterns of coevolutionary cycles can be understood in terms of
 532 the evolutionary behaviour of morphs in a single trophic level. The increase
 533 of a morph's bodysize in a coevolution cycle is due to the same mechanism as
 534 in single morph cycles. The asymmetry in the feeding kernel $\gamma(\cdot)$ (Eq. (3)),
 535 creates an evolutionary ratchet, which drives the morphs to higher bodysizes
 536 (see Fig. 3). However, the evolution of the morphs is limited by interference
 537 competition. Each morph, except the largest and the smallest morph, have
 538 two neighbours at a bodysize distance slightly bigger than the competition
 539 range β . Therefore mutants of the intermediate morphs inevitably compete
 540 with these neighbours and can not invade. While the smallest morph has only
 541 a larger neighbour, smaller mutants are not viable due to the decreasing abil-
 542 ity to feed on the lower trophic level and high intra trophic level predation.
 543 The largest morph in an coevolution cycle has only a smaller neighbour,
 544 thus it can increase its bodysize through the evolutionary ratchet. All other
 545 morphs follow one after another, since they are not bounded upwards any
 546 more. Therefore coevolution is a top-down process in this model. However,
 547 just as in the single morph case, increasing bodysize results in the largest
 548 morph reaching an unstable state where it can be invaded and outcompeted
 549 by smaller mutants. This is analogous to the jump point of a single morph

550 cycle.

551 In contrast to single morph cycles, the largest resident is not outcompeted
552 by a new offspring of its own, but by a mutant of the second largest resident.
553 The second largest resident is replaced by a slightly larger mutant, which is
554 within competition range β of the largest resident. (Time-points, at which
555 the two largest residents compete are marked by grey vertical lines in Figs. 2c
556 and 3.) This mutant is close enough to the optimal feeding distance that it
557 can outcompete, and thus replace, the largest resident. Thus the interference
558 competition from above is removed, allowing each of the resident morphs to
559 increase its bodysize. A new mutant, descended either from the smallest
560 resident, or from a resident in a lower trophic level, can invade either close
561 to the end, or at the beginning, of a cycle; when the interference competition
562 from the smallest resident is lowest.

563 4. Discussion

564 The model introduced by Loeuille and Loreau [20] is well known for evo-
565 lutionarily static food webs. We investigated a larger range of competition
566 parameters, and found novel evolutionary states: cycling of single morphs
567 (region II), cycling of complete food webs (region III), and transitory states
568 from single morph cycles to polymorphic food webs (region IV). We want to
569 discuss six main implications of our study:

570 First, the observed evolutionary cycles are based on coevolution, which is
571 driven by competition and trophic interactions between resident morphs and
572 also the invader. These coevolutionary processes are observed in empirical
573 studies, where they can also be driven by competition [9, 23] or trophic in-
574 teractions [1]. However, it is hard to study coevolution empirically in larger
575 communities, due to the high number of complex interactions which make
576 identification of the evolutionary dynamics and the coevolving traits very
577 difficult [33]. Our findings show that it is not necessary to consider all inter-
578 actions between species within the community to explain cycling. Instead,
579 it is sufficient to consider interactions between smaller, independently coe-
580 volving, subgroups. In our system, each trophic level represents a subgroup,
581 since each level evolves independently with a different frequency.

582 Second, we found that food web characteristics are remarkably robust
583 towards evolution. The network structure, number of morphs and links are
584 relatively constant during evolution. In addition, the network structures
585 of solely coevolving food webs and static food webs are similar. Therefore

586 they are not distinguishable on the time scale of the population dynamics.
587 However for mixed evolutionary food webs the network structure changes: the
588 number of species contained in each trophic level and the distance between
589 each level loses its regularity.

590 Third, our results are in agreement with Cope's rule [10]: During an
591 evolutionary cycle, morphs increase their bodysize, since a slightly larger
592 morph has a higher fitness than a smaller morph. In addition, our study
593 suggests a more natural explanation of the "Endless trends to gigantism"
594 paradigm [16] than mass extinction [18]. Large bodysizes are advantageous
595 over a wide range, especially towards similar sized morphs, but result in a
596 lower ability to consume the original resource, which finally increases the
597 vulnerability towards invasion of better adapted morphs.

598 Fourth, single morph cycles have similar characteristics to taxon cycles
599 [34, 45], suggesting that the down-regulation of the environmental quality
600 for the resident (decreasing resource consumption) is also responsible for
601 the arising evolutionary cycling: the increase in bodysize of the resident,
602 due to coevolution with invaders, results in morphs that are progressively
603 less suited to their environment. Thus, morphs that are better adapted to
604 the environment can invade. Furthermore, theoretical studies of competing
605 species on a niche axis have shown that this class of evolutionary community
606 cycles is related to the asymmetry in the competitive interaction (Rummel
607 and Roughgarden [35], Taper and Case [41], Matsuda and Abrams [24]). In
608 our study an asymmetry is introduced naturally via trophic interactions and
609 therefore we suggest that evolutionary cycling is an intrinsic phenomenon in
610 the model of Loeuille and Loreau [20], which can also occur in the absence
611 of competition. Evolutionary cycling might be a general phenomenon in
612 evolutionary size-structured food web models.

613 Fifth, our study provides a new avenue for the debate of whether ongoing
614 evolutionary changes and Red Queen dynamics are ecologically realistic.
615 Dieckmann et al. [12] proposed evolutionary limit cycles, e.g between predator
616 and prey species, as a theoretical framework for Red Queen dynamics,
617 but our study suggests an alternative mechanism. Thereby, in the simplest
618 case of single morph cycles, the resident species is evolutionarily driven towards
619 unfavourable positions in niche space, which reduces its viability and
620 ultimately leads to self-extinction - so that the community can be colonized
621 again by a mutant or invader at a different, more favorable, phenotypic trait.
622 In contrast, in even the simplest predator-prey limit cycle, both species are
623 present at all times.

624 Sixth, we propose that taxon cycles might be a transitory phase of island
 625 colonisation: we observe that single morph cycles can be transitory states,
 626 after which the community becomes polymorphic and large food webs emerge.
 627 These webs can be either static or dynamic. The latter can be a possible
 628 representation of cycling of larger communities – continental taxon cycles –
 629 which are hypothesised, but hard to study empirically, due the intertwining of
 630 the invasion processes [29]. Note that within the model used, the estimation
 631 of the time scale considered is not possible without relating it to empirical
 632 data, since all variables are treated as dimensionless.

633 As with all modelling studies, our results depend on the choice of pro-
 634 cess formulations and simplifications used in the model. Here, we have
 635 chosen to closely follow the formulation as defined by Loeuille and Loreau
 636 [20]. While many compelling refinements of this model have been proposed
 637 [21, 20, 4, 8, 5], our study shows that evolutionary community cycles are
 638 already a natural outcome in the original model. Using extensive numerical
 639 simulations we have confirmed that our main model results also hold in more
 640 refined model variants. We briefly mention the two most influential changes:
 641 to the competition and feeding kernels. First, following Loeuille and Loreau
 642 [20] we have used a box-shaped kernel $\alpha(\cdot)$ with a finite competition range β
 643 to describe the interference competition (Eq. (3)). Therefore, morphs either
 644 compete with a fixed, well-defined strength, or competition is absent. More
 645 realistically, competition strength should change continuously with bodysize
 646 distance which could be described by link overlap (e.g. a Gaussian kernel)
 647 sensu [22], as applied by [5, 8, 30]. Using numerical simulations we verified
 648 that evolutionary cycling still occurs if the box-shaped interference competi-
 649 tion is replaced by link overlap competition. Furthermore, the range of link
 650 overlap competition is closely related to the feeding range σ of the compet-
 651 ing morphs ($\propto \sqrt{2}\sigma$). Comparing link overlap competition with box-shaped
 652 competition shows that link overlap competition occurs over a wider bodysize
 653 distance. This justifies the investigated competition range β in our studies.

654 Second, following Loeuille and Loreau [20], our chosen feeding kernel $\gamma(\cdot)$
 655 consists of a truncated Gaussian. This discontinuity could be responsible for
 656 the cycling behaviour observed. However, when the discontinuous feeding
 657 and competition kernels were replaced with continuous functions, we still
 658 observed cycling see Fig. A.7. In particular, we note that it was necessary
 659 to use an asymmetric feeding kernel (the ability to consume morphs with a
 660 larger bodysize decreases faster than the ability to consume smaller morphs)
 661 e.g. the Ricker function [44], in order to obtain this behaviour. Thus, we

662 conclude that cycling behaviour arises from strong asymmetries in the feeding
663 kernel.

664 We have shown that evolutionary cycles occur in the evolutionary food
665 web model used, it is robust towards variation in the shape and range of the
666 feeding and competition kernels, and can manifest in various ways. However,
667 the underlying mechanism, leading to evolutionary cycling, is not restricted
668 to the model used. We suggest that evolutionary cycles might be a general
669 phenomenon in evolutionary food web models and also empirical food webs
670 and therefore conclude that evolutionary cycling in food webs may be more
671 frequent than commonly believed.

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806 **Appendix A. Appendix**

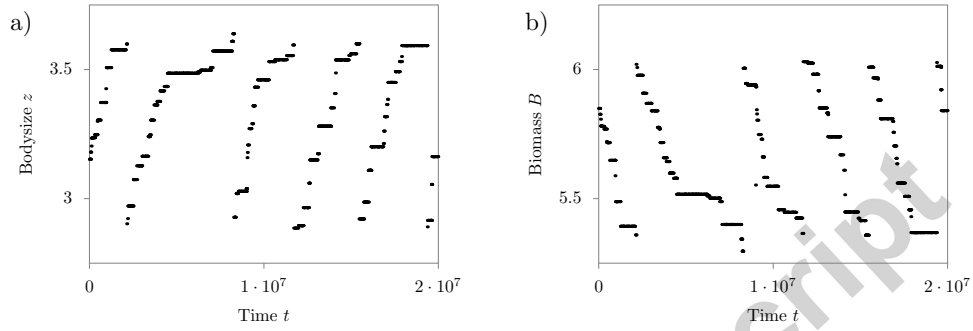


Figure A.5: Evolutionary temporal behaviour of a single morph cycle (Fig. 2b)). **a, b:** Close-up of the biomass B and bodysize z during a single morph cycle shown in Fig. 2b.

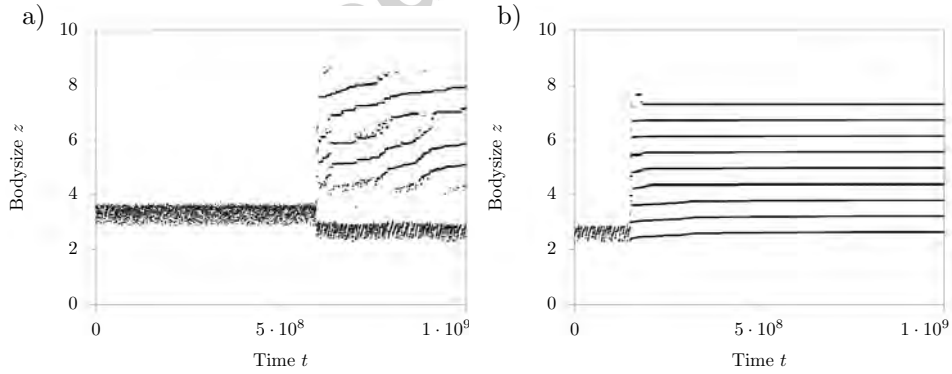


Figure A.6: Transient dynamic. After a transient of single morph cycles the system becomes polymorphic. **a:** Mixed evolutionary behaviour of a food web is visible after the transition. The competition parameters are set to $\alpha_0 = 0.1$ and $\beta = 0.75$. **b:** A static food web emerges after the transition. The competition parameters are set to $\alpha_0 = 0.3$ and $\beta = 0.58$.

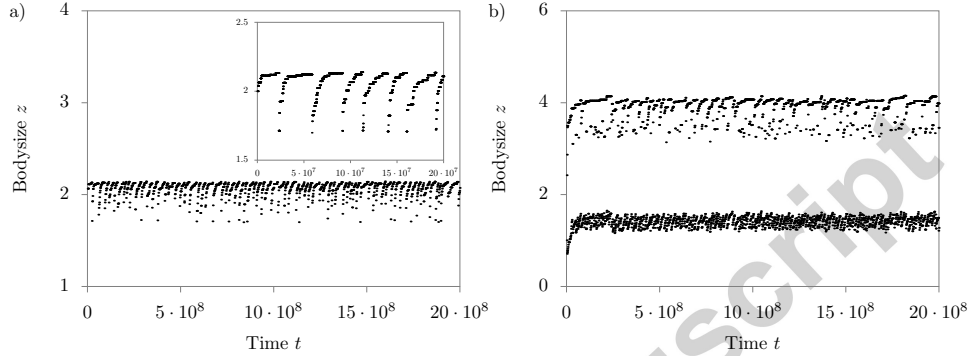


Figure A.7: Evolutionary food web behaviour for continuous feeding kernels. The interaction kernels are replaced by continuous functions. The original *feeding kernel* $\gamma(\cdot)$ (Eq. 2) is replaced by a more ecologically accurate Ricker function [44], $\gamma(z_i - z_j) = \frac{\gamma_0}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(\log(z_i - z_j) - \log(d))^2}{\sigma^2}\right)$, which is asymmetric in respect to bodysize: the ability to consume larger morphs decreases faster than the ability to consume smaller morphs. The box shaped *competition kernel* $\alpha(\cdot)$ (Eq. 3) is replaced by a Gaussian function, $\alpha(|z_i - z_j|) = \frac{\alpha_0}{\beta\sqrt{2\pi}} \exp\left(-\frac{(z_i - z_j)^2}{\beta^2}\right)$, similar to [8, 5, 30]. The Gaussian shape is motivated by competition due to link overlap as introduced by [22]. It is highest for identical bodysizes and decreases with the bodysize distance of the competing morphs. **a:** Single morph cycle for continuous interaction kernels, which is similar to the one observed in the original model, Fig. 2b ($\sigma = 2.3, \alpha_0 = 0.2, \beta = 2$). **b:** Complex community cycles, that commemorate complex community cycles, see Fig. 2c,d ($\sigma = 2.5, \alpha_0 = 0.2, \beta = 1.5$). All other parameters are set according to section 2.3.