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Interpretable Ensembles of Classifiers for Uncertain Data with Bioinformatics Applications

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Abstract—Data uncertainty remains a challenging issue in many applications, but few classification algorithms can effectively cope with it. An ensemble approach for uncertain categorical features has recently been proposed, achieving promising results. It consists in biasing the sampling of features for each model in an ensemble so that less uncertain features are more likely to be sampled. Here we extend this idea of biased sampling and propose two new approaches: one for selecting training instances for each model in an ensemble and another for sampling features to be considered when splitting a node in a Random Forest training. We applied these approaches to classify ageing-related genes and predict drugs’ side effects based on uncertain features representing protein-protein and protein-chemical interactions. We show that ensembles based on our proposed approaches achieve better predictive performance. In particular, our proposed approaches improved the performance of a Random Forest based on the most sophisticated approach for handling uncertain data in ensembles of this kind. Furthermore, we propose two new approaches for interpreting an ensemble of Naive Bayes classifiers and analyse their results on our datasets of ageing-related genes and drug’s side effects.

Index Terms—Classification, interpretability, data uncertainty, bioinformatics, the biology of ageing.

1 INTRODUCTION

Data uncertainty can be categorised into existential uncertainty, which occurs when the existence of some data record is uncertain, and value uncertainty, which can be further categorised into class-label uncertainty or feature-value uncertainty. This work addresses feature-value uncertainty, which occurs when some feature values in a data record (instance) are not precisely known. This uncertainty can naturally arise due to the limited precision of data collection technology, particularly in bioinformatics or biomedical domains. An uncertain feature value is usually represented by a probability distribution on the corresponding feature’s domain.

It has been shown that incorporating information on uncertainty into classification algorithms can improve predictive performance [1], [2], [3], [4], [5], but this is still an under-explored research topic, particularly for categorical features, since most previous methods focus on uncertain numerical features. Hence, this work proposes new ensemble methods for coping with uncertain categorical features.

We focus on ensemble methods that learn many base classifiers independently on random subsets of the original training set and then aggregate the base classifiers’ predictions. In general, such ensemble methods usually have better predictive performance and are more robust to slight data variations than any single base classifier. In particular, Bagging methods randomly sample subsets of the instances in the dataset with replacement (which is called bootstrap sampling) [6], and Random Subspaces methods randomly sample subsets of the features in the dataset [7].

An ensemble approach for uncertain categorical features, named Biased Random Subspaces (BRS), has recently been proposed by Maia et al. [3]. It consists in biasing the random sampling of features for each model in an ensemble, based on the principle that features with lower uncertainty degrees should have better class-discrimination potential since the confidence about their actual values is higher.

Relying on the same hypothesis, this work extends the idea of biased random sampling by proposing two new approaches for building ensembles of classifiers that cope with uncertain categorical features. The first is a Biased Bootstrap (BB) approach for selecting training instances for each model in an ensemble. The second is a Biased Splitting (BS) approach for sampling features to be considered when splitting a node while building the trees of a Random Forest.

We evaluate our proposed approaches by using them to build Naive Bayes (NB) classifiers ensembles and Random Forests and performing experiments on ten classification datasets with real uncertain information. This uncertainty consists of feature values’ probability distributions extracted from real-world databases – unlike previous work, which typically used datasets with artificially generated uncertainty [1], [2], [4], [5].

Out of these 10 datasets, 4 were also used in [3]. In these datasets, each instance is an ageing-related gene. The class labels indicate whether a gene has a pro-longevity or anti-longevity effect on a particular organism’s lifespan, as recorded in the GenAge database [8], and the features represent protein-protein interaction (PPI) information. The feature uncertainty is represented by probabilities of interactions between two proteins, obtained from the STRING database [9].

The other 6 datasets are introduced in this work. In these
datasets, each instance is a drug (chemical). The class labels
indicate whether or not a drug has a particular side effect,
as recorded in the SIDER database [10], and the features represent
protein-chemical interaction (PCI) information. The feature uncertainty is represented by probabilities of
interactions between a chemical (drug) and a protein, obtained
from the STITCH database [11].

We report two types of results. First, we compare the
predictive performance of the ensemble methods using the
aforementioned uncertainty-handling approaches (BRS, BB
and BS) against the accuracy of the corresponding baseline
ensemble methods (without the BRS, BB and BS
approaches), using two well-known predictive performance
measures: the Area Under the ROC curve (AUROC) and
the geometric mean of Sensitivity and Specificity [12]. In
general, the proposed ‘biased-sampling’ ensemble methods
outperformed the baseline ‘unbiased-sampling’ methods.

Additionally, we report the results of interpreting the
best ensemble models learned from the ageing-related
datasets. Model interpretation is an increasingly important
topic in machine learning [13], and it has led to novel
biological insights in bioinformatics domains [14], [15].

Although a single NB classifier is naturally interpretable,
interpreting an NB ensemble is not trivial. We are aware of
only one approach in the literature for interpreting an NB
ensemble: transforming it into a single NB model by linear
approximation (with some loss of predictive accuracy) and
then interpreting that NB model [16], [17].

Hence, we propose two new approaches for interpreting
an NB ensemble as a further contribution. The first measures
the importance of a feature based on conditional probability
differences, whereas the second is a more sophisticated
approach based on finding a minimal set of features that
is sufficient to preserve the class predicted for an instance
(so that changes to the values of other features in that
instance do not change the class predicted by the model). We
use these two interpretation approaches for NB ensembles
and a conventional feature importance measure for
random forests to learn feature rankings for the ageing-
related datasets, identifying the most important features for
predicting such genes’ effects on an organism’s lifespan.

In summary, this paper extends the initial work from [3]
by providing four new contributions. First, we propose two
new approaches – Biased Bootstrap (BB) and Biased Split-
ing (BS) – for learning from uncertain categorical features,
which complement the Biased Random Subspace (BRS) one
introduced in [3]. Second, in [3] the BRS approach was
used to create NB ensembles only; whilst in this paper, we
create several types of ensembles, including NB ensembles
with the BB approach and random forests with the BS and
BB approaches. Third, the experiments in [3] used only 4
datasets of ageing-related genes, whilst in this paper, we
use 10 datasets: those 4 datasets and 6 new datasets for
predicting drugs’ side effects. Fourthly, this paper introduces
two approaches for interpreting an ensemble of Naïve Bayes
classifiers, whilst no such interpretation was attempted
in [3]. We also use these interpretation approaches to analyse
the best models learned from the ageing-related datasets,
discussing the results from the perspective of the biology of
ageing as an interdisciplinary contribution.

2 METHODS
2.1 Definitions
Let \( F = \{f_1, f_2, \ldots, f_m\} \) be the set of predictive features,
where \( m \geq 1 \), and \( C = \{c_1, c_2, \ldots, c_q\} \) be the set of classes,
where \( q \geq 2 \). The domain of a feature \( f_j \) is \( \text{dom}(f_j) \).
A dataset \( D = \{(X_1, y_1), (X_2, y_2), \ldots, (X_n, y_n)\} \) consists of \( n \)
labelled instances. Each instance in \( D \), identified by an index
\( i \), is associated with a feature vector \( X_i = (x_{i1}, x_{i2}, \ldots, x_{im}) \)
and a class label \( y_i \in C \). In the classification problem, the
objective is to construct a model from \( D \) capable of predicting
the class of an unlabelled instance given its corresponding
feature vector.

Let \( U \subseteq F \) be the set of uncertain features, assumed
to be categorical in this work. The domain of a cata-
gorical feature \( f_j \) is a finite set of values \( \text{dom}(f_j) = \{v_{j1}, v_{j2}, \ldots, v_{jk}|\text{dom}(f_j)|\} \).
If \( f_j \) is not uncertain, its value \( x_{ij} \) for an instance \( i \) is represented by a single
value. Otherwise, it is a discrete probability distribution
represented by a probability vector \( P_{ij} \), i.e.:

\[
x_{ij} = \begin{cases} x_{ij} \in \text{dom}(f_j), & \text{if } f_j \in F \setminus U \\
P_{ij} = (p_{i1j}, p_{i2j}, \ldots, p_{ijk}|\text{dom}(f_j)|), & \text{otherwise}
\end{cases}
\]

where, if \( f_j \in U \), \( p_{ijk} \in [0, 1] \) represents the probability that
\( x_{ij} \) takes the value \( v_{jk} \) and \( \sum_{k=1}^{|\text{dom}(f_j)|} p_{ijk} = 1 \).

2.2 Coping with uncertainty in ensemble models
Recently, an ensemble approach for coping with uncertainty
in categorical features, named Biased Random Subspaces
(BRS), has been proposed by Maia et al. [3]. It consists in
biasing the random sampling of features for each model in
an ensemble. Here we extend the idea of biased random
sampling to two new approaches: a Biased Bootstrap (BB)
approach for selecting training instances for each model in
an ensemble (which can be used with any bagging-based
ensemble algorithm) and a Biased Splitting (BS) approach
for sampling features to be considered when splitting a node
while building the trees of a Random Forest.

From [3], we have the definition of the bias value for a feature
\( f_j \), given by:

\[
b_{sj} = \left( 1 - \frac{1}{|I \setminus M_{sj}|} \sum_{i \in I \setminus M_{sj}} E_{ij} \right) \times \frac{|I \setminus M_{sj}|}{|I|}
\]

where \( I = \{1, 2, \ldots, n\} \) is the set of indices of all instances in \( D \), \( M_{sj} \) is the set of indices of instances in \( D \) with a
missing value for the feature \( f_j \), and \( E_{ij} \) is the normalized
entropy of the probability distribution represented by \( P_{ij} \) if
\( f_j \) is an uncertain feature (or zero, otherwise), that is:

\[
E_{ij} = \begin{cases} \sum_{k=1}^{|\text{dom}(f_j)|} \frac{p_{ijk} \log(p_{ijk})}{\log(|\text{dom}(f_j)|)}, & \text{if } f_j \in U \\
0, & \text{otherwise}
\end{cases}
\]

The feature bias values are normalized over all features,
deﬁning a probability distribution \( B = (\beta_1, \beta_2, \ldots, \beta_m) \),
where a probability \( \beta \), associated with a feature \( f_j \) is given by
\( \beta_j = b_{sj}/\sum_{j=1}^{m} b_{sj} \).

Instead of the default uniform distribution from the
general Random Subspaces strategy, the BRS approach uses
the probability distribution $B$ to sample the features to train each base classifier in the ensemble.

Random Forests usually do not sample features before generating each tree. Nonetheless, they sample a subset of features to be considered candidate features when splitting each tree node. Hence, we propose the Biased Splitting (BS) approach for this sampling, which uses the probability distribution $B$ to sample the candidate features.

Finally, we propose the Biased Bootstrap (BB) approach for instance sampling, which is analogous to the BRS and BS approaches for feature sampling. Hence, we define the bias value for an instance identified by index $i$, given by:

$$b_{is} = \left(1 - \frac{1}{|F \setminus M_{is}|} \sum_{j \in F \setminus M_{is}} E_{ij}\right) \times \frac{|F \setminus M_{is}|}{|F|}$$

where $M_{is}$ is the set of features in $D$ with a missing value for instance $i$.

The instance bias values are normalized over all instances, defining a distribution $\Gamma = (\gamma_1, \gamma_2, \ldots, \gamma_n)$, where a probability $\gamma_i$ associated with an instance identified by index $i$ is given by $\gamma_i = b_{is} / \sum_{i=1}^{n} b_{is}$.

The BB approach uses probability distribution $\Gamma$ to sample the instances for training each base classifier.

### 2.3 Interpreting NB ensembles via conditional probabilities

The first approach we propose for interpreting an ensemble of NB classifiers relies on the influence that a feature value $x_{ij} \in \text{dom}(f_j)$ has for determining the most likely class to be predicted for an instance by a single NB classifier, which we compute as an importance score. We then combine the importance scores from all the classifiers into the ensemble's importance scores.

This approach does not address feature uncertainty. It assumes the base models of the ensemble are standard NB classifiers. Therefore, in this context, $x_{ij}$ is always represented by a single value.

Given a feature vector $X_i = (x_{i1}, x_{i2}, \ldots, x_{im})$ associated with an unlabelled instance identified by index $i$, an NB classifier predicts the class $y \in C$ that maximizes the value given by $P(y|X_i) \propto P(y) \prod_{j=1}^{m} P(x_{ij}|y)$.

We first present our definition of importance for binary classifiers, where $C = \{c_1, c_2\}$. The importance of a feature value $x_{ij}$ in a given NB classifier is estimated by the following difference between conditional probabilities:

$$\text{Diff}(x_{ij}, c_1, c_2, e) = |P(x_{ij}|c_1) - P(x_{ij}|c_2)|$$

where $e$ is the classifier for which the difference is computed. Clearly, the higher the difference in the class-conditioned probability of a feature value between the two class labels, the more importance (influence) that feature value will have for determining the most likely class to be assigned to the testing instance.

For datasets with more than two class labels, this idea can be generalised by summing the differences between all pairs of class labels in $C$:

$$\text{Importance}(x_{ij}, C, e) = \sum_{r=1}^{q-1} \sum_{s=r+1}^{q} \text{Diff}(x_{ij}, c_r, c_s, e)$$

The importance of a feature value $x_{ij}$ for an ensemble of NB classifiers is computed by averaging its importance across all classifiers in the ensemble. However, different NB classifiers will generally use different feature subsets (due to the random subspaces approach). Intuitively, other things being equal, the larger the number of classifiers in the ensemble that use a feature, the larger the importance of the value of that feature. Therefore, we assume that, if a classifier $e_u$ does not use a feature $f_j$, then $\text{Importance}(x_{ij}, C, e_u) = 0$. Hence, we define the ensemble-wide importance as:

$$\text{Importance}(x_{ij}, C) = \frac{\sum_{u=1}^{t} \text{Importance}(x_{ij}, C, e_u)}{t}$$

where $e_u$ is the $u$-th classifier and $t$ is the total number of classifiers in the ensemble.

This approach is appropriate when the predicted class returned by the ensemble is computed by a simple majority vote of all classifiers, i.e., all classifiers have the same weight in the voting. If weighted voting is used instead (where the weight of a vote is proportional to the classifier’s confidence in its prediction), then the importance equation could be easily modified to compute a correspondingly weighted average over the $t$ classifiers.

Finally, once the importance value has been computed for all feature values $x_{ij}$, we rank all feature values in decreasing order of importance. Then a user (domain expert) can focus on interpreting the top-ranked feature values, i.e., the most important ones for predicting the class variable in the ensemble.

Note that for binary domain features, where $\text{dom}(f_j) = \{v_{j1}, v_{j2}\}$, the importance computed for both values will be the same due to the complementarity of the probabilities in use. Given two class labels $c_r$ and $c_s$ such that $c_r \in C$, $c_s \in C$ and $c_r \neq c_s$, the following relations apply:

$$P(v_{j1}|c_r) = 1 - P(v_{j2}|c_r) \quad (1)$$

$$P(v_{j1}|c_s) = 1 - P(v_{j2}|c_s) \quad (2)$$

The difference of the class-conditioned probabilities of the value $v_{j1}$ between $c_r$ and $c_s$ for a classifier $e$ would be:

$$\text{Diff}(v_{j1}, c_r, c_s, e) = |P(v_{j1}|c_r) - P(v_{j1}|c_s)| \quad (3)$$

By replacing (1) and (2) in (3), we obtain:

$$\text{Diff}(v_{j1}, c_r, c_s, e) = |(1 - P(v_{j2}|c_r)) - (1 - P(v_{j2}|c_s))|$$

$$= |1 - P(v_{j2}|c_r) - 1 + P(v_{j2}|c_s)|$$

$$= |P(v_{j2}|c_s) - P(v_{j2}|c_r)|$$

$$= |P(v_{j2}|c_r) - P(v_{j2}|c_s)|$$

$$= \text{Diff}(v_{j2}, c_r, c_s, e)$$

Therefore, for binary domain features (like the PPI and PCI features in our datasets), the importance computed for both values in the domain is the same. Then, the importance computed for any of the values in a feature’s domain can be interpreted as that feature’s importance.
Algorithm 1. MinimalSufficientSet($X_i$, $e$)
1: $c_i \leftarrow$ class predicted by $e$ for $X_i$
2: $\text{SuppSet} \leftarrow \{ f_i | P(x_{ij}|c_i) > P(x_{ij}|y), \forall y \in C \setminus \{c_i\} \}$
3: $S \leftarrow \text{SuppSet}$
4: Calculate $\text{Importance}(x_{ij}, C, e)$ for all $f_j \in S$
5: $\text{SortedFeats} \leftarrow \text{SortByImportance}(\text{SuppSet})$
6: $e' \leftarrow e$
7: for each feature $f_j$ in $\text{SortedFeats}$ do
8: Remove $f_j$ from $e'$
9: if $e'_i = c_i$ then $S \leftarrow S \setminus \{f_j\}$
10: else Exit loop
11: return $S$

2.4 Interpreting NB ensembles via minimal sufficient features

The approach based on conditional probability differences measures the importance of each feature value separately, ignoring its importance in the context of all other feature values. This is consistent with NB assuming that each feature is independent of all others conditioned on the class variable, but it does not directly measure the influence of a feature value on class prediction. Naïve Bayes makes class predictions using the formula: $P(y|X_i) \propto P(y) \prod_{j=1}^{m} P(x_{ij}|y)$. Therefore, whether or not a conditional probability will make a difference in the choice of the predicted class depends on the entire set of conditional probabilities and the prior class probability.

Hence, we propose a second approach that considers sets of feature values. The principle we rely on is the same adopted in the definitions of anchors by Ribeiro et al. [18] and minimal sufficient factors by Watson et al. [19]. We seek to find, for each instance, a minimal set of features sufficient to preserve the class prediction, such that changes to the other feature values of the instance would not change the class predicted by the model.

Note that the larger the value of $\text{Importance}(x_{ij}, C, e)$, the higher the influence of $x_{ij}$ for a class prediction in model $e$, but even the feature with the highest $\text{Importance}$ value may still not be sufficient for a given prediction.

However, we can use this notion to find a minimal sufficient set of features. The basic idea is to sort all features in increasing order of their $\text{Importance}$ values and then identify the minimal set of top features in that sorted list which, together, are sufficient for preserving the class prediction made by the classifier.

Let $c_i$ be the class predicted by the classifier for instance $i$. A feature value $x_{ij}$ is said to “support” the prediction of $c_i$ if and only if $P(x_{ij}|c_i) > P(x_{ij}|y), \forall y \in C \setminus \{c_i\}$. That is, the feature value $x_{ij}$ becomes more likely if instance $i$ has class $c_i$ than if that instance has another class. Naturally, when searching for a minimal sufficient set of features, we only need to consider feature values that support the class predicted by the classifier.

A method for identifying a minimal sufficient set of features for the class prediction for a given instance is presented in Algorithm 1.

Based on the sufficiency criterion, we define a measure of the importance of a feature $f_j$ for a classifier $e$ given the set of instances $X$, denoted $SI_{\text{Importance}}(f_j, e, X)$, as the proportion of instances in $X$ for which $f_j$ is in the minimal sufficient set returned by Algorithm 1.

The importance of a feature for the entire ensemble is computed by simply averaging its importance across all classifiers in the ensemble:

$$SI_{\text{Importance}}(f_j, X) = \frac{\sum_{t=1}^{t} SI_{\text{Importance}}(f_j, e_t, X)}{t}$$

where $e_t$ is the $t$-th classifier and $t$ is the total number of classifiers in the ensemble.

2.5 Datasets

We have evaluated the proposed approaches on real data from two application domains. The first domain is the classification of ageing-related genes regarding their effect on the lifespan of an organism, which may be positive (prolongevity) or negative (anti-longevity). From this domain, we used the 4 datasets generated by Maia et al. [3], which integrate data from the GenAge database (Build 20) [8] and the STRING database (Version 11.0) [9]. Each dataset contains data regarding ageing-related genes of one of the 4 major model organisms from the GenAge database: *Caenorhabditis elegans* (roundworm), *Drosophila melanogaster* (fruit fly), *Mus musculus* (mouse), and *Saccharomyces cerevisiae* (baker’s yeast). Each feature in these datasets refers to a protein-protein interaction (PPI) extracted from the STRING database.

The second domain involves the prediction of drugs’ side effects. For this domain, we have generated 6 new datasets by integrating data from the SIDER database (Version 4.1) [10] and the STITCH database (Version 5.0) [11]. The SIDER database contains information on marketed medicines and their recorded side effects (adverse drug reactions). STITCH is a database of protein-chemical interactions (PCI) that stem from computational predictions, knowledge transfer between organisms, and interactions aggregated from other databases.

Each side-effect dataset refers to one of the 6 frequent side effects in the SIDER database: nausea, headache, dermatitis, rash, vomiting and dizziness. Each instance in these datasets refers to a protein-protein interaction (PPI) or a binary class variable indicating whether the corresponding drug has the side effect represented in the dataset (positive) or not (negative). Each PCI feature refers to one protein and has a binary domain, indicating whether or not an interaction between the corresponding chemical (drug) and the protein referred by the feature has been observed. As uncertain features, they are represented by probability distributions.

A value $x_{ij}$ of an uncertain binary feature $f_j$ for an instance $i$ in a dataset is represented by a probability distribution $P_i = (p_{ij1}, p_{ij2})$, where $p_{ij1}$ and $p_{ij2}$ are the complementary probabilities of $x_{ij}$ taking each of the two values in dom$(f_j)$. Therefore, each probability distribution representing a PCI or PPI feature value is encoded by a single value $p_{ij}$, and $P_i = (p_{ij}, 1 - p_{ij})$. In our datasets, $p_{ij}$ is the confidence score (interaction probability) obtained from the STRING or STITCH databases for the corresponding PCI or PPI features, respectively.

Table 1 presents detailed information about the datasets. They are particularly challenging for having many features,
a small number of instances, and a very high percentage of missing values (when there is no information regarding a specific interaction in the STRING or STITCH databases). To avoid overfitting, we have discarded PPI and PCI features with low support (annotating less than 10 instances). As usual in the literature using PPIs as features for classifying genes, we represent missing values as zeros.

### 2.6 Ensemble methods

We consider three baseline ('unbiased-sampling') ensemble methods: two kinds of NB ensembles and one Random Forest (RF). Although these baseline methods do not use an uncertainty-based random sampling bias, they handle uncertainty at the individual classifiers’ level.

The baseline NB ensembles, ENB-NV and ENB-EV, were also used by Maia et al. [3]. In ENB-NV (Ensemble of NB classifiers with Numeric Values), the NB classifiers treat each uncertain value (an interaction probability) as a numeric value and assume that the feature values’ probability distributions are Gaussian. In ENB-EV (Ensemble of NB classifiers with Expected Values), the NB classifiers binarize each uncertain value into an expected value using the threshold 0.5 and consider multivariate Bernoulli distributions for the data.

To the best of our knowledge, there is no work in the literature coping with uncertain categorical features using RFs. Among papers coping with uncertain numerical features using RF (or single decision trees), the most sophisticated approach is distributing fractions of examples (DFE) over the child nodes when splitting a node on an uncertain feature [4], [20], [21], [22]. The DFE approach provided RFs with mildly positive results in [21] and mildly negative results in [22]. Although only evaluated in the literature for numerical features, RFs using the DFE approach (RF-DFE) also apply to categorical ones. Since RF-DFE is the most sophisticated available RF that can handle uncertain categorical features, we use it as our baseline RF.

The baseline ensembles perform a standard unbiased sampling of instances and features. For each of them, we build three versions by incorporating different combinations of our proposed approaches: BB, BRS and BB+BRS for NB ensembles; BB, BS and BB+BS for Random Forests.

We have coded the algorithms’ implementations from the scikit-learn library [23]. We have set the number of base classifiers (NB or decision trees) in each ensemble to 500 and the number of instances used to build each one to \( n \). The number of features sampled (to train each NB classifier or to split a tree node in an RF) has been set to \( \sqrt{m} \). Since our RFs distribute fractions of examples using instance weights, instead of defining a minimum number of instances required to be at a leaf node, we defined the minimum sum of instance weights required at a leaf node as 0.01 (1\% of the number of instances).

### 2.7 Predictive performance measures

We have assessed the predictive performance of the algorithms using two metrics: the Area Under the Receiver Operating Characteristic curve (AUROC) and the geometric mean of sensitivity and specificity (G-mean) [12].

We evaluated each algorithm using the well-known 10-fold cross-validation. Furthermore, we have assessed the statistical significance of the differences in the predictive performance measures between each pair of algorithms, using a paired Wilcoxon signed-rank test for each dataset, with a significance level of 0.05.

### 2.8 Simpson’s paradox

Let \( X \) be a binary feature, taking values \( x_1 \) or \( x_2 \), and \( Y \) be the class variable in a dataset. Let the dataset’s instances be divided into two groups: those with \( X = x_1 \) and those with \( X = x_2 \). Consider a class label of interest, \( y_1 \) (e.g., the pro-longevity or anti-longevity label in our ageing-related datasets). Let \( P(y_1|x_i) \) and \( P(y_2|x_i) \) denote the conditional probabilities of \( y_1 \) for the corresponding groups of instances. Consider the scenario where each group of instances is further divided according to the values of another binary feature \( Z \), called a confounder, taking values \( z_1 \) or \( z_2 \) (in our datasets, the confounders are binary, but this condition could be relaxed). Simpson’s paradox occurs when \( P(y_1|x_1, z_1) > P(y_1|x_2, z_1) \) and \( P(y_1|x_1, z_2) < P(y_1|x_2, z_2) \), for \( j \in \{1, 2\} \) or vice-versa: \( P(y_1|x_1) < P(y_1|x_2) \) and \( P(y_1|x_1, z_j) > P(y_1|x_2, z_j) \), for \( j \in \{1, 2\} \). That is, the paradox occurs if the conditional probability of the class label of interest \( y_1 \) ‘increases’ (‘decreases’) from the former to the latter group, both for instances with \( Z = z_1 \) and instances with \( Z = z_2 \) [24], [25], [26]. Hence, the paradox shows a reversal of the direction of association between the values of a feature and the probability of a class label of interest in the context of a confounder.

# 3 Results

### 3.1 Assessing predictive performance

#### 3.1.1 Experiment 1

This experiment evaluated NB ensembles using NB-NV as base classifiers (i.e., Gaussian NB with Numeric Values of features). We have compared four ensembles: the baseline ensemble of NB-NVs, denoted ENB-NV, and three biased-sampling ensembles, combining ENB-NV with the biased sampling approaches, denoted ENB-NV+BB, ENB-NV+BRS, and ENB-NV+BB+BRS.
Table 2 shows the AUROC and G-mean results on the 10 datasets. The best values (for each metric and dataset) are in bold. The last row shows each ensemble’s average rank (per metric). Superscript symbols indicate the statistically significant advantages (SSA). Based on these results, ENB-NV+BRS is the best ensemble regarding AUROC and G-mean, with an average rank of 1.6 for both metrics.

3.1.2 Experiment 2
This experiment evaluated NB ensembles using NB-EV (which binarises uncertain values into Expected Values) as base classifiers. Again, we have compared four ensembles: the unbiased-sampling baseline ensemble of NB-EVs, denoted ENB-NV; and three biased-sampling ensembles combining ENB-EV with the biased sampling approaches, denoted ENB-EV+BB, ENB-EV+BRS and ENB-EV+BB+BRS. Table 3 presents the results for this group of enssembles. ENB-EV+BRS is the best ensemble for AUROC and G-mean, with the average ranks of 1.4 and 1.6, respectively.

3.1.3 Comparing the best NB ensembles
Table 4 presents the results for ENB-NV+BRS and ENB-EV+BRS, the best ensembles from Experiments 1 and 2, respectively. ENB-EV+BRS obtained the best AUROC results, with an average rank of 1.4, whereas ENB-NV+BRS was the best for G-mean, with an average rank of 1.0.

3.1.4 Experiment 3
This experiment evaluated four RFs: RF-DFE (distributing fractions of examples among child nodes), the most sophisticated available RF that can handle uncertain categorical features; and three biased-sampling RFs, combining RF-DFE with the biased sampling approaches: RF-DFE+BB, RF-DFE+BS, RF-DFE+BB+BS. Table 5 presents the results. RF-DFE+BB obtained the best AUROC results, with an average rank of 2.0; whereas RF-DFE+BS obtained the best G-mean results, also with an average rank of 2.0.

3.1.5 Comparing the best NB ensembles and the best RFs
This last comparison aimed at determining the best overall method regarding each of the AUROC and G-mean metrics. Table 6 presents the results. RF-DFE+BB obtained the best AUROC results (average rank: 1.1), whereas RF-DFE+BS obtained the best G-mean results (average rank: 1.3).

In general, the results of these three experiments support the hypothesis that the BB, BRS and BS approaches can improve the predictive performance of ensembles on uncertain data. A limitation of the BB approach was that it produced poor results when applied to NB ensembles. However, the BB and BS approaches proposed in this paper worked well with RFs, and they obtained the best overall results since RF-DFE+BB and RF-DFE+BS were the best overall ensembles for the AUROC and G-mean metrics, respectively, outperforming RF-DFE.

3.2 Identifying the top-ranked PPI features
We have applied our two proposed approaches for interpreting NB ensembles to the four ageing-related datasets to identify the top-ranked PPI features for classification. Among all NB ensembles evaluated in our experiments, ENB-EV+BRS and ENB-NV+BRS have achieved the best overall AUROC and G-mean values, respectively. We have selected ENB-EV+BRS for model interpretation since it uses binarised features, facilitating interpretation.

We have trained a model applying ENB-EV+BRS to each dataset’s whole set of instances. Then, we used this model to produce rankings of features in decreasing order of importance.

Table 7 presents the top-10 features for each organism (dataset) regarding the importance measure based on conditional probabilities. For each feature, columns 2–5 present its importance-based rank, the corresponding protein ID from the STRING database, and the corresponding gene’s symbol and name. Columns 6 and 7 present the absolute and relative frequencies of value 1 (considering the threshold of 0.5 used) for the corresponding feature in the instances of the Pro-longevity and Anti-longevity classes. The last column shows whether or not the feature is involved in occurrences of Simpson’s paradox [24], [25] (discussed in Subsection 3.4).

Interestingly, out of the 40 top-ranked PPI features in Table 7, 15 represent ribosomal proteins, namely 5 of the top-10 PPI features for the worm dataset and all the top-10 PPI features for the yeast dataset. It is also worth observing in Table 7 the relative frequency of genes (dataset instances) of each class (Pro- vs Anti-longevity) that interact with the gene associated with each of these 15 ribosomal proteins (PPI features). In all those 15 table rows, the relative frequency of Anti-longevity genes interacting with the corresponding ribosomal protein is substantially higher than that of Pro-longevity genes interacting with that ribosomal protein. The relative frequency differences are clearly striking for 9 of the 10 yeast PPI features in the table, which have a frequency of 0% for Pro-longevity genes and frequencies varying from 14.0% to 18.2% for Anti-longevity genes.

Despite this strong pattern, none of these 9 yeast ribosomal proteins is included in GenAge [8] – the most comprehensive database of ageing-related genes. By itself, this strong pattern does not allow us to conclude that those 9 ribosomal proteins have an anti-longevity effect on yeast, which in principle could be confirmed only via appropriate biological experiments. However, the pattern seems strong enough to justify further investigation of some of those 9 ribosomal proteins in future work.

Among the 5 ribosomal proteins in Table 7 for worm, 4 (rps-0, rps-5, rps-11, rpl-3) are included in the GenAge database. Actually, among the top-10 PPI features, 8 are associated with genes included in GenAge – the exceptions are atp-1 and rps-30.

Regarding the top-10 PPI features for mice, only the top-ranked one, igf1, is included in GenAge. Interestingly, igf1 is annotated as having an “unclear” effect on longevity in GenAge, whilst its closely related igf1r (igf1 receptor) is annotated as Anti-longevity. In Table 7, the relative frequency of Anti-longevity genes interacting with the igf1 gene is 51.6%, which is much larger than the relative frequency of such interaction in the Pro-longevity class: 19.6%.

Finally, out of the top-10 PPI features for fly in Table 7, 4 are associated with genes included in GenAge, namely Sod1, FOXO, Sod2, park. Among the 6 genes not included in GenAge, there are 3 heat shock proteins. Two of them,
Hsp70Ab and Hsp70Aa, have a relative frequency of only 5.8% for the Anti-longevity class, with a much larger relative frequency of 19.0% and 19.8%, respectively, for the Pro-longevity class.

Table 8 presents the top-10 features for each organism regarding the importance measure based on minimal sufficient features. Most features from Table 7 are also in Table 8: 8 features for worm, 9 for fly, 6 for mouse and 6 for yeast.

As RF-DFE+BB+BRS achieved the best predictive performance on the ageing-related datasets, we also produced feature rankings using it. We have used the default RF feature importance measure from the scikit-learn’s implementation, based on the Gini index. Table 9 presents the top-10 features for each organism. Consistently with Tables 7 and 8, many of the top-10 PPI features for worm and yeast in Table 9 represent ribosomal proteins, which are mainly associated with the anti-longevity class.

### 3.3 Confirming the relevance of the top-ranked features for the biology of ageing

Overall, the top-ranked features fit well with current knowledge on longevity/ageing and previous similar analyses, as follows. The top-ranked features for worms include daf-16, a key regulator of longevity in worms. Mutations in daf-16 suppress the longevity effects caused by several parameters.

2. The Gini feature importance measure is biased towards features with many values [27]. However, since all features in our datasets are binary, this limitation is not an issue in this work.

---

**TABLE 2**

**Experiment 1 Results**

<table>
<thead>
<tr>
<th>Dataset</th>
<th>AUROC (%)</th>
<th>G-mean (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ENB-NV</td>
<td>ENB-NV</td>
<td>ENB-NV</td>
</tr>
<tr>
<td>ENB-NV+BB+BB+BR</td>
<td>ENB-NV</td>
<td>ENB-NV</td>
</tr>
<tr>
<td>AG-Worm</td>
<td>71.46</td>
<td>72.32</td>
</tr>
<tr>
<td>AG-Fly</td>
<td>65.62</td>
<td>65.94</td>
</tr>
<tr>
<td>AG-Mouse</td>
<td>66.73</td>
<td>63.66</td>
</tr>
<tr>
<td>AG-Yeast</td>
<td>61.62</td>
<td>63.81</td>
</tr>
<tr>
<td>SE-Nausea</td>
<td>58.89</td>
<td>56.53</td>
</tr>
<tr>
<td>SE-Headache</td>
<td>56.35</td>
<td>54.64</td>
</tr>
<tr>
<td>SE-Dermatitis</td>
<td>58.06</td>
<td>56.05</td>
</tr>
<tr>
<td>SE-Rash</td>
<td>56.98</td>
<td>55.24</td>
</tr>
<tr>
<td>SE-Vomiting</td>
<td>60.64</td>
<td>58.24</td>
</tr>
<tr>
<td>SE-Dizziness</td>
<td>61.63</td>
<td>55.21</td>
</tr>
<tr>
<td>Avg. Rank</td>
<td>2.7</td>
<td>2.7</td>
</tr>
</tbody>
</table>

+ SSA (vs ENB-NV), † SSA (vs ENB-NV+BB), ‡ SSA (vs ENB-NV+BB+BRS), † SSA (vs ENB-NV+BB+BRS)

**TABLE 3**

**Experiment 2 Results**

<table>
<thead>
<tr>
<th>Dataset</th>
<th>AUROC (%)</th>
<th>G-mean (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ENB-EV</td>
<td>ENB-EV</td>
<td>ENB-EV</td>
</tr>
<tr>
<td>ENB-EV+BB+BB+BR</td>
<td>ENB-EV</td>
<td>ENB-EV</td>
</tr>
<tr>
<td>AG-Worm</td>
<td>76.91</td>
<td>75.39</td>
</tr>
<tr>
<td>AG-Fly</td>
<td>64.05</td>
<td>66.24</td>
</tr>
<tr>
<td>AG-Mouse</td>
<td>69.26</td>
<td>70.03</td>
</tr>
<tr>
<td>AG-Yeast</td>
<td>75.55</td>
<td>75.77</td>
</tr>
<tr>
<td>SE-Nausea</td>
<td>50.45</td>
<td>46.81</td>
</tr>
<tr>
<td>SE-Headache</td>
<td>52.25</td>
<td>48.86</td>
</tr>
<tr>
<td>SE-Dermatitis</td>
<td>54.55</td>
<td>51.07</td>
</tr>
<tr>
<td>SE-Rash</td>
<td>53.65</td>
<td>49.19</td>
</tr>
<tr>
<td>SE-Vomiting</td>
<td>56.43</td>
<td>46.27</td>
</tr>
<tr>
<td>SE-Dizziness</td>
<td>57.72</td>
<td>46.07</td>
</tr>
<tr>
<td>Avg. Rank</td>
<td>2.4</td>
<td>3.1</td>
</tr>
</tbody>
</table>

+ SSA (vs ENB-EV), † SSA (vs ENB-EV+BB), ‡ SSA (vs ENB-EV+BB+BRS), † SSA (vs ENB-EV+BB+BRS)

**TABLE 4**

**Comparison of the Best NB Ensembles**

<table>
<thead>
<tr>
<th>Dataset</th>
<th>AUROC (%)</th>
<th>G-mean (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ENB-NV</td>
<td>ENB-NV</td>
<td>ENB-NV</td>
</tr>
<tr>
<td>ENB-NV+BB+BB+BR</td>
<td>ENB-NV</td>
<td>ENB-NV</td>
</tr>
<tr>
<td>AG-Worm</td>
<td>72.33</td>
<td>74.81</td>
</tr>
<tr>
<td>AG-Fly</td>
<td>65.03</td>
<td>69.00</td>
</tr>
<tr>
<td>AG-Mouse</td>
<td>65.81</td>
<td>69.30</td>
</tr>
<tr>
<td>AG-Yeast</td>
<td>61.22</td>
<td>76.79</td>
</tr>
<tr>
<td>SE-Nausea</td>
<td>65.16</td>
<td>57.06</td>
</tr>
<tr>
<td>SE-Headache</td>
<td>56.92</td>
<td>54.86</td>
</tr>
<tr>
<td>SE-Dermatitis</td>
<td>59.83</td>
<td>58.57</td>
</tr>
<tr>
<td>SE-Rash</td>
<td>59.78</td>
<td>57.71</td>
</tr>
<tr>
<td>SE-Vomiting</td>
<td>65.19</td>
<td>65.91</td>
</tr>
<tr>
<td>SE-Dizziness</td>
<td>65.01</td>
<td>65.20</td>
</tr>
<tr>
<td>Avg. Rank</td>
<td>1.6</td>
<td>1.4</td>
</tr>
</tbody>
</table>

* SSA
ribosomal proteins, which, as mentioned earlier, have been among top features, particularly with a high frequency of repair pathways and mechanisms that protect against stress important for longevity [33]. Interestingly, in flies, we see particular, antioxidant protection has long been considered tant for healthy ageing and longevity [32]. There are also an-pathway in invertebrates, including in worms [31].

is atg-7, an autophagy regulator that is a major longevity and longevity regulation [30]. Lastly, one of the top genes

Mitochondrial genes are also among the top hits, which also mutations [28]. Other top genes in worms include various ribosomal proteins, which is not surprising given that they control translation, which has been strongly associated with longevity regulation in worms and other organisms [29]. Mitochondrial genes are also among the top hits, which also fits current knowledge of the role of mitochondria in ageing and longevity regulation [30]. Lastly, one of the top genes is atg-7, an autophagy regulator that is a major longevity pathway in invertebrates, including in worms [31].

There are heat shock proteins and genes related to stress response among the top genes in flies. This fits well with the long-established observation that stress resistance is important for healthy ageing and longevity [32]. There are also antioxidant enzymes, like superoxide dismutase, thioredoxin and glutathione peroxidase; in invertebrates and flies, in particular, antioxidant protection has long been considered important for longevity [33]. Interestingly, in flies, we see repair pathways and mechanisms that protect against stress among top features, particularly with a high frequency of pro-longevity interactions. In yeast, most top features are ribosomal proteins, which, as mentioned earlier, have been related to longevity regulation in model organisms.

In mice, the top gene is igf-1, with a strong anti-longevity frequency. The growth hormone/insulin/IGF1 pathway is the major longevity pathway in mammals [34], [35], so this result fits our knowledge of longevity well. Also, other players in the pathway like forkhead box proteins, Plikcd, Ins2 and Irs2 are among the top predictions. Some brain and neuronal factors (e.g., Src) are also among the top features, which could fit GH/IGF1's neuroendocrine regulation [34]. Alternatively, they could be related to ageing changes in the brain. As Src is not in GenAge, it could be an interesting target for future studies.

Overall, the top-ranked features fit nicely into pro- and anti-longevity pathways enriched in GenAge [31]. Of note, in worms, ribosomal proteins and mitochondrial proteins involved in oxidative phosphorylation have been previously found enriched in anti-longevity processes [31], while in flies, responses to oxidative stress (like antioxidant en-zymes) are among enriched pro-longevity processes. In mice, the insulin signalling pathway is a top enriched anti-longevity pathway [31], in line with our results.

### 3.4 Detecting occurrences of Simpson’s paradox

When interpreting an association between each top-ranked feature and a class label (pro- or anti-longevity), it is important to consider that the direction of that association might be misleading due to Simpson’s paradox. By direction of association we mean whether the presence of a PPI is associated with an increased probability of the pro-longevity or, conversely, the anti-longevity class.

Simpson’s paradox occurs when the direction of an association between two variables X and Y at the population (aggregated) level is reversed in all the sub-groups produced by partitioning that population according to the values of a third variable, Z, called a confounder [24], [25]. In other words, the direction of the association between variables X and Y is reversed when conditioning on each value of the confounder Z. In our classification task, X and Z are predictive features, whilst Y is the class variable.

Table 10 shows an example of this paradox in the fly dataset. Looking only at the aggregated data in the first row of the table, ignoring the interaction between the values of the Hsp83 and Hsc70-4 PPI features, we would conclude

<table>
<thead>
<tr>
<th>Dataset</th>
<th>AUROC (%)</th>
<th>G-mean (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RF-DFE</td>
<td>ENB-NV</td>
</tr>
<tr>
<td>AG-Worm</td>
<td>76.62*</td>
<td>56.55*</td>
</tr>
<tr>
<td>AG-Fly</td>
<td>68.57*</td>
<td>59.14*</td>
</tr>
<tr>
<td>AG-Mouse</td>
<td>77.44*</td>
<td>52.46*</td>
</tr>
<tr>
<td>AG-Yeast</td>
<td>69.33*</td>
<td>56.29*</td>
</tr>
<tr>
<td>SE-Nausea</td>
<td>68.55†</td>
<td>66.86†</td>
</tr>
<tr>
<td>SE-Headache</td>
<td>65.11‡</td>
<td>66.66‡</td>
</tr>
<tr>
<td>SE-Dermatitis</td>
<td>64.83‡</td>
<td>66.11‡</td>
</tr>
<tr>
<td>SE-Rash</td>
<td>68.02‡</td>
<td>67.83‡</td>
</tr>
<tr>
<td>SE-Vomiting</td>
<td>68.55‡</td>
<td>69.67‡</td>
</tr>
<tr>
<td>Avg. Rank</td>
<td>2.7</td>
<td>2.1</td>
</tr>
</tbody>
</table>

TABLE 5
Experiment 3 Results

<table>
<thead>
<tr>
<th>Dataset</th>
<th>AUROC (%)</th>
<th>G-mean (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RF-DFE</td>
<td>ENB-NV</td>
</tr>
<tr>
<td>AG-Worm</td>
<td>75.41‡</td>
<td>55.83‡</td>
</tr>
<tr>
<td>AG-Fly</td>
<td>71.81‡</td>
<td>56.33‡</td>
</tr>
<tr>
<td>AG-Mouse</td>
<td>70.66‡</td>
<td>52.46‡</td>
</tr>
<tr>
<td>AG-Yeast</td>
<td>78.51‡</td>
<td>59.14‡</td>
</tr>
<tr>
<td>SE-Nausea</td>
<td>69.08‡</td>
<td>56.92‡</td>
</tr>
<tr>
<td>SE-Headache</td>
<td>66.66‡</td>
<td>56.88‡</td>
</tr>
<tr>
<td>SE-Dermatitis</td>
<td>62.89‡</td>
<td>56.66‡</td>
</tr>
<tr>
<td>SE-Rash</td>
<td>63.45‡</td>
<td>56.66‡</td>
</tr>
<tr>
<td>SE-Vomiting</td>
<td>68.15‡</td>
<td>56.87‡</td>
</tr>
<tr>
<td>SE-Dizziness</td>
<td>69.67‡</td>
<td>60.23‡</td>
</tr>
<tr>
<td>Avg. Rank</td>
<td>2.7</td>
<td>2.1</td>
</tr>
</tbody>
</table>

*SSA (vs RF-DFE), †SSA (vs RF-DFE+BB), ‡SSA (vs RF-DFE+BS), §SSA (vs RF-DFE+BB+BS)

TABLE 6
Comparison of the Best NB Ensembles and the Best RFs

<table>
<thead>
<tr>
<th>Dataset</th>
<th>AUROC (%)</th>
<th>G-mean (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>RF-DFE</td>
<td>ENB-EV</td>
</tr>
<tr>
<td>AG-Worm</td>
<td>75.41‡</td>
<td>55.83‡</td>
</tr>
<tr>
<td>AG-Fly</td>
<td>71.81‡</td>
<td>56.33‡</td>
</tr>
<tr>
<td>AG-Mouse</td>
<td>70.66‡</td>
<td>52.46‡</td>
</tr>
<tr>
<td>AG-Yeast</td>
<td>78.51‡</td>
<td>59.14‡</td>
</tr>
<tr>
<td>SE-Nausea</td>
<td>69.08‡</td>
<td>56.92‡</td>
</tr>
<tr>
<td>SE-Headache</td>
<td>66.66‡</td>
<td>56.88‡</td>
</tr>
<tr>
<td>SE-Dermatitis</td>
<td>62.89‡</td>
<td>56.66‡</td>
</tr>
<tr>
<td>SE-Rash</td>
<td>63.45‡</td>
<td>56.66‡</td>
</tr>
<tr>
<td>SE-Vomiting</td>
<td>68.15‡</td>
<td>56.87‡</td>
</tr>
<tr>
<td>SE-Dizziness</td>
<td>69.67‡</td>
<td>60.23‡</td>
</tr>
<tr>
<td>Avg. Rank</td>
<td>2.7</td>
<td>2.1</td>
</tr>
</tbody>
</table>

*SSA
that the feature value “interaction with Hsp83 = yes” is more associated with the pro-longevity class than “interaction with Hsp83 = no”. Actually, among the genes/proteins (instances) in our dataset that interact with Hsp83, 72.2% are pro-longevity genes, whilst among the genes/proteins that do not interact with Hsp83, 60.4% are pro-longevity genes. So, interacting with Hsp83 is associated with an increased probability of the pro-longevity class label.

However, when we look at the data partitioned by the values of the “interaction with Hsc70-4” feature in the second and third rows of the table, a different pattern emerges. Among genes/proteins that do not interact with Hsc70-4, the relative frequency of the pro-longevity class is higher among genes/proteins that do not interact with Hsp83 (58.4%) than among genes/proteins interacting with Hsp83 (50%). The same pattern is observed among genes/proteins interacting with Hsc70-4 (83.3% for Hsp83-no vs 76.7% for Hsp83-yes). Hence, in both sub-groups of genes/proteins (interacting or not with Hsc70-4), interacting with Hsp83 is associated with decreased probability of the pro-longevity class label, the reverse of the direction of association observed for the aggregated data.

Tables 7 and 8 indicate Simpson’s paradox occurrences for the feature Hsp83 in the fly dataset and features Rem1 and Ngf in the mouse dataset. Hence, when interpreting the association between those features and the class variable, one should be aware of those paradox occurrences to avoid drawing wrong conclusions about the data.

### 4 Conclusion

This work addresses classification with uncertain categorical features, whose values are represented by probability distributions. We have proposed two new ensemble approaches called Biased Bootstrap (BB) and Biased Splitting (BS) for coping with this type of uncertainty, based on the principle that features with lower uncertainty degrees have better class-discrimination potential since there is higher confidence in their actual values across the dataset.

Our experiments have evaluated these two approaches on 10 datasets in the domains of ageing-related genes.
and drugs’ side effects. For this evaluation, we have used real data with uncertain features referring to probabilities of protein-protein and protein-chemical interactions. Our results show that the ensembles using the proposed BB and BS approaches achieved higher predictive performance than baseline methods without uncertainty-based random sampling bias, with the caveat that the BB approach did not produce good results when applied to NB ensembles. These results support the hypothesis that the proposed approaches can effectively cope with uncertainty in categorical features. In particular, our proposed approaches improved the performance of RF-DFE, a Random Forest method that applies sophisticated, is based on the concept of a minimal set of conditional probability differences, while the second, more sophisticated, is based on the concept of a minimal set of sufficient features for classifying each instance. We have applied these two feature-ranking approaches to the ageing-related datasets and compared them to the feature ranking produced with a conventional feature importance measure for random forests. An analysis of the top-ranked features showed that, overall, they fit the current knowledge about the influence of genes/proteins on ageing well. Besides, we have also pointed out some strong patterns involving longevity effects and genes that are not included in GenAge [8]. These findings suggest some targets for future biological experiments that could confirm the longevity effects of some genes/proteins.

Furthermore, we have proposed two new approaches for interpreting an ensemble of Naive Bayes classifiers based on feature importance measures used to rank features in decreasing order of their influence in the ensemble’s predictions. The first approach is straightforwardly based on.

**ACKNOWLEDGMENTS**

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REFERENCES


