1   **Online Dynamic Prediction of Potassium Concentration in Biomass Fuels through**

2   **Flame Spectroscopic Analysis and Recurrent Neural Network Modelling**

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8   **Abstract**

9   Biomass fuels are widely used as a renewable source for heat and power generation. Alkali

10   metals in a biomass fuel have an significant impact on furnace safety as such metals lead to

11   fouling and slagging in the furnace and corrosion of water pipes. This paper presents a technique

12   for dynamic predicting Potassium (K) concentration in a biomass fuel based on spectroscopic

13   analysis and different recurrent neural networks. A miniature spectrometer is employed to

14   acquire the spectroscopic signals of K in different biomass fuels, including peanut shell, willow,

15   corn cob, corn straw and wheat straw, and their blends. The spectroscopic features of K are

16   extracted. The factors that influence the spectral intensity of K in the biomass fuels are

17   investigated. A basic recurrent neural network (RNN), and its variants, i.e., long short-term

18   memory neural network (LSTM-NN) and deep recurrent neural network (DRNN), are

19   constructed using the spectroscopic signal of K from the spectrometer. The performances of the

20   neural networks for the dynamic prediction of K concentration are compared and analysed

21   theoretically and experimentally. It is found that the relative error in the K concentration

22   prediction through the use of the DRNN model is within 6.34% whilst the LSTM-NN and RNN

23   models give errors slightly greater than this.

24

25   **Keywords** - *biomass; potassium concentration; dynamic prediction; flame spectroscopy;*

26   *recurrent neural networks.*

27

List of symbols

b_c	Bias of the memory unit	V_o	Weight of output layer of the output gate
b_f	Bias of the forget gate	W_c	Weight of input layer of the memory unit
b_i	Bias of the input gate	W_f	Weight of input layer of the forget gate
b_o	Bias of the output gate	W_i	Weight of input layer of the input gate
c_t	Memory unit	W_o	Weight of input layer of the output gate
h_t	Output of the hidden layer	$W^{(hh)}$	Weight matrix from h_{t-1} to h_t
K	Kurtosis	$W^{(hx)}$	Weight matrix from x_t to h_t
N	Number of samples	$W^{(s)}$	Weight matrix from h_t to y_t
S	Skewness coefficient	x_i	Radiation intensity of the i-th sample
U_c	Weight of hidden layer of the memory unit	x_t	Input of the input layer
U_f	Weight of hidden layer of the forget gate	y_t	Output of the output layer
U_i	Weight of hidden layer of the input gate	μ	Mean value of the sample
U_o	Weight of hidden layer of the output gate	σ	Standard deviation of the sample
V_f	Weight of output layer of the forget gate	$\delta(\ )$	Sigmoid function
V_i	Weight of output layer of the input gate		

29

30

1 Introduction

As one of important renewable energy sources, biomass fuels have the advantage of abundant varieties and environmental friendliness [1]. It has been widely used either as a single fuel or a blend of different solid fuels for generating electricity or thermal power. In China, biomass power generation has grown steadily and accounted for about 2% of the total power field from 2006 to 2017, marking that China is the second largest country in the world in the biomass power generation, only after the United State [2]. However, biomass combustion systems often suffer from severe operation problems, including poor combustion stability, low combustion efficiency, and furnace fouling and slagging with potential safety concerns [3, 4]. It is known that a biomass fuel contains generally high volatile matter, high fixed carbon concentration, low moisture content and low ash concentration. It also has high alkali metal (Potassium and Sodium) concentrations which are main contributor to furnace fouling and slagging. The potassium concentration is relatively high in the ash and the melting point of the formed compounds is generally low. So, it is molten at a high temperature and easy to slag on the water-cooled wall, reducing the heat conduction efficiency of the boiler [5]. It is therefore highly desirable to detect on-line continuously the fouling and slagging in biomass-fired boilers.

Current techniques available for detecting fouling and slagging in a biomass-fired boiler are mostly off-line, where the samples of ash and slagging are taken, and the ash fusion temperature and alkali metal concentrations are analysed in laboratory. There are some laboratory-based methods which are commonly used off-line to analyse alkali concentration in biomass fuels. They include scanning electron microscopy (SEM), X-ray diffraction (XRD) and X-Ray fluorescence (XRF) [6, 7]. Although potassium (K) and sodium (Na) release characteristics during biomass combustion can be obtained, these methods require sophisticated and expensive

55 laboratory equipment and are unsuitable for online operation. As the type of biomass or their

56 blends may change unexpectedly during combustion, there is a pressing need to measure the K

57 concentration online continuously for combustion optimisation under flexible operation

58 conditions.

59

60 A burner flame contains extensive information about the fuel and the combustion process. The

61 spectroscopic information of the flame is closely related to flame temperature, fuel properties,

62 operation conditions, and pollutant emissions. Optical diagnostic techniques, such as laser-

63 induced break down spectroscopy (LIBS), have been used for the online measurement of K and

64 Na concentrations in flames. Hus *et al*. [8] measured the release concentrations of K and Na

65 during the combustion of pine wood pellet based on the LIBS technology, and analysed the peak

66 release concentrations of Na and K during different combustion stages. Liu *et al.* [9] conducted

67 multi-point LIBS measurement on the K release characteristics of poplar wood and corn straw.

68 Flame emission spectroscopy (FES) was also applied to detect alkali release from combustion.

69 Lim *et al*. [10] used optical emission spectroscopy to investigate alkali metal release from

70 biomass combustion. Sadeckas *et al*.[11] measured the emission intensities of Na, Ca, and K

71 from the combustion of single wood and straw pellets doped with known concentrations of Na,

72 Ca, and K by using the ICCD, and analyzed the alkali emission characteristics in terms of

73 relative intensity emission and integrated emission intensity at two different temperatures. With

74 the use of the FES technique and inductively coupled plasma mass spectrometer (ICP-MS),

75 Paulauskas *et al*.[12] studied the capability and the accuracy of chemiluminescence-based

76 sensors to measure the spontaneous emission of K and Na from the combustion of single wood

77 and straw pellets with different alkali concentrations at 1000 ℃. The results have shown that the

78 emission intensity of alkali radicals depends on alkali concentrations in the samples and K and

79 Na radical emission intensities increase with alkali concentrations in the samples. He *et al*. [13]

80   established the functional relationship between K concentration and radiation intensity of K

81   characteristic spectral lines in Camphorwood and rice husk flames. For the municipal solid waste

82   incinerators, they developed a portable spectral system to determine temperature and gaseous

83   phase Na and K concentrations. The experimental results have indicated that the released

84   gaseous phase Na and K correlated with both temperature and primary air in incinerators [14].

85   The functional model between the radiation intensity of Na, temperature, and Na concentration

86   was established based on the FES technique and calibration experiments. Yan *et al.* [15, 16]

87   analyzed the characteristics of the temperature and Na concentration in different combustion

88   stages. In the above methods, alkali metal concentration was measured and analyzed off-line

89   under different combustion stages (devolatilization stage, char, and ash stage). At the same time,

90   in order to obtain the concentration of gaseous phase Na and K in the flame, a calibration

91   procedure needs to be followed However, continuous variations in alkali metal concentration

92   during combustion are seldom considered. This paper proposes a method for the online

93   continuous measurement of K concentration through RNN modelling, aiming to achieve

94   continuous monitoring and optimization of combustion processes.

95

96   This paper presents the dynamic prediction of K concentration in biomass fuels through flame

97   spectroscopic analysis and recurrent neural network modelling. The spectroscopic information

98   of the biomass-fired flame is obtained using a miniature spectrometer on a lab-scale combustion

99   test rig under different operation conditions. Three recurrent neural networks, i.e., basic

100   recurrent neural network (RNN), long short-term memory neural network (LSTM-NN) and

101   deep recurrent neural network (DRNN) are constructed based on the spectroscopic features

102   extracted from the spectroscopic information obtained. The RNNs are capable of processing

103   the sequence data of the flame. The nodes between the hidden layers of such networks are

104   connected. The inputs of a hidden layer include not only the output of the input layer but also

105   the output of the previous hidden layer. These unique features enable the RNNs to remember

106   the information of the previous state and apply it to the computation of the current output of the

107   model, making the RNNs to be a potential soft computing approach to predict the K

108   concentration in biomass fuels based on the flame spectroscopic information. A series of

109   experiments were conducted to examine the performance of the RNN models for the dynamic

110   prediction of K concentrations in five typical biomass fuels. Meanwhile, data driven models

111   based on the conventional BP neural network (BP-NN) and support vector machine (SVM) are

112   also established and trained for purpose of a direct comparison with the RNNs. It should be

113   mentioned that, in this study, Sodium (Na), as another common alkali metal in a biomass fuel,

114   is also often regarded as a main contributor for fouling and slagging in biomass combustion.

115   However, the Na concentration in the tested biomass fuels is much lower than the K

116   concentration, and is thus not included in this study.

117

118   **2 Methodology**

119   **2.1 Technical strategy**

120   Fig. 1 shows the block diagram of the recurrent neural network models for the dynamic

121   prediction of the K concentration in biomass fuel. The spectroscopic signal of the flame is

122   obtained using a spectrometer over the spectral range from 200 nm to 1100 nm. The spectral

123   intensity of K is also acquired by the spectrometer at the wavelength of 769.89 nm. A set of

124   characteristic parameters, including oscillation frequency, radiant energy, mean, variance,

125   peak-to-peak value, skewness and kurtosis coefficient are then extracted from the signal. These

126   features, together with the flame temperature which is measured by a multi-channel

127   thermometer, are used as the inputs of the prediction models. The expected K concentration

128   (ground truth), which is determined through element analysis, is taken as the output of the

129   models. Three recurrent neural network (RNN) models, including the basic RNN, LSTM-NN

130　and DRNN are trained, validated and tested. It should be noted that the LSTM-NN and DRNN

131　are the variants of the RNN and are also considered for the intended application.
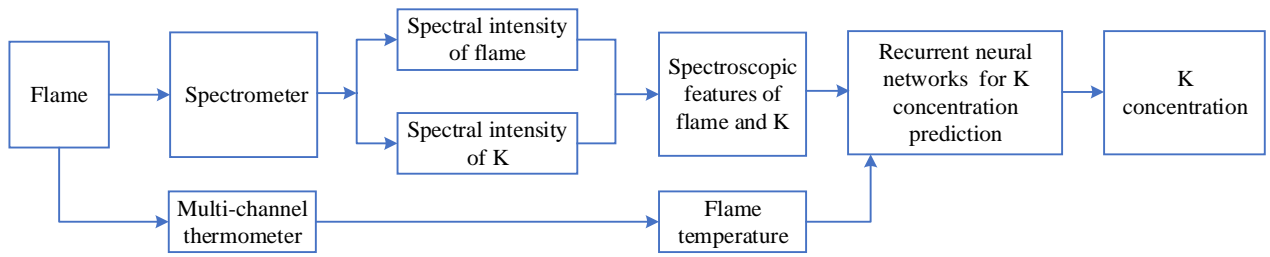

132

133　**Fig. 1 Block diagram of recurrent neural network models for K concentration**

134　**prediction.**

135　**2.2 Recurrent neural network**

136　The RNN is a type of neural network which has a memory function and can be used to process

137　sequential information [17]. The architecture of the RNN is shown in Fig. 2. The RNN has a

138　"memory" which captures information about what has been calculated at the present state. All

139　neurons in the hidden layer are linked in a chain. The output at the current time is not only

140　related to the current input but also depends on the network status in the past. The RNN is

141　widely used in text classification, machine translation, language recognition and image analysis

142　[18, 19].
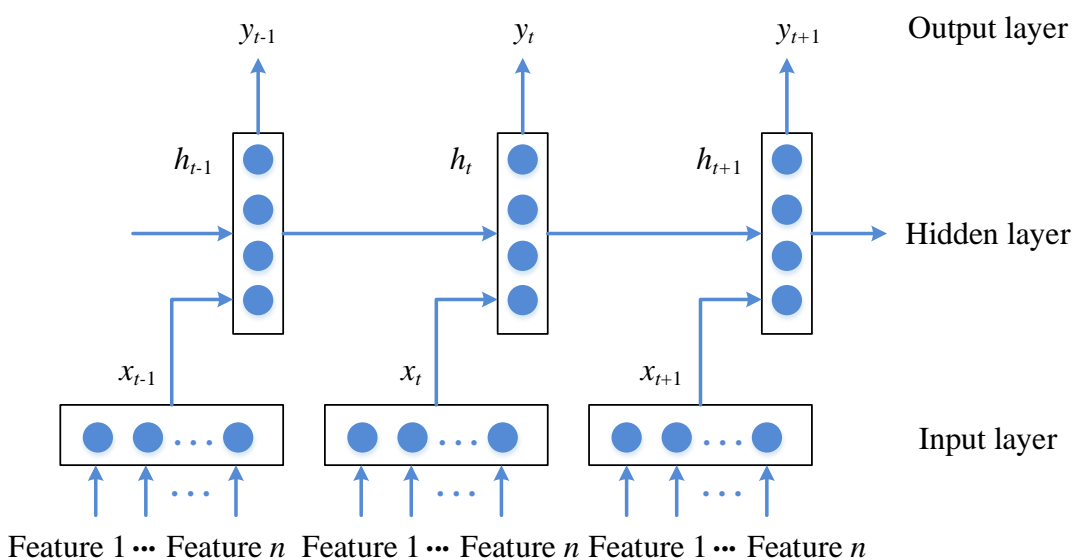
143

144　**Fig. 2 Architecture of the RNN.**

145 In Fig.2, x_t and h_t are the input and output of the hidden layer, respectively, and y_t is the output

146 of the output layer at the time t. During the training, the input data is forward-propagated for

147 calculation whilst the error is back-propagated to update weight parameters. The outputs of the

148 hidden layer and the output layer are expressed, respectively, as follows:

149 $$h_t = f\left(W^{(hh)}h_{t-1} + W^{(hx)}x_t\right) \qquad (1)$$

150 $$y_t = softmax\left(W^{(s)}h_t\right) \qquad (2)$$

151 where $W^{(hh)}$ is the input weight matrix from h_{t-1} to h_t, $W^{(hx)}$ is the input weight matrix from

152 x_t to h_t, $W^{(S)}$ is the weight matrix from h_t to y_t, and f is the activation function [20].

153

154 **2.3 Long short-term memory neural networks**

155 The LSTM-NN is an improved version of the RNN, which was proposed by Hochreiter and

156 Schmidhuber [21]. The LSTM-NN can effectively process long-distance sequence information

157 and overcome gradient disappearance, gradient explosion and lack of long-term memory ability

158 during the training process of an RNN. Fig.3 shows the schematic diagram of the LSTM-NN

159 architecture, which is composed of an input gate (i_t), a forget gate (f_t) and an output gate (o_t).

160 The forget gate is a key element, which decides whether to keep the information among neurons

161 during the information transmission. It takes the output of the previous moment and the input

162 of the current moment as inputs, and determines the degree of retention or forgetting through

163 the activation function. The input gate, forget gate and output gate are each connected to a

164 multiplier which controls the input and output of information and the state of each cell.
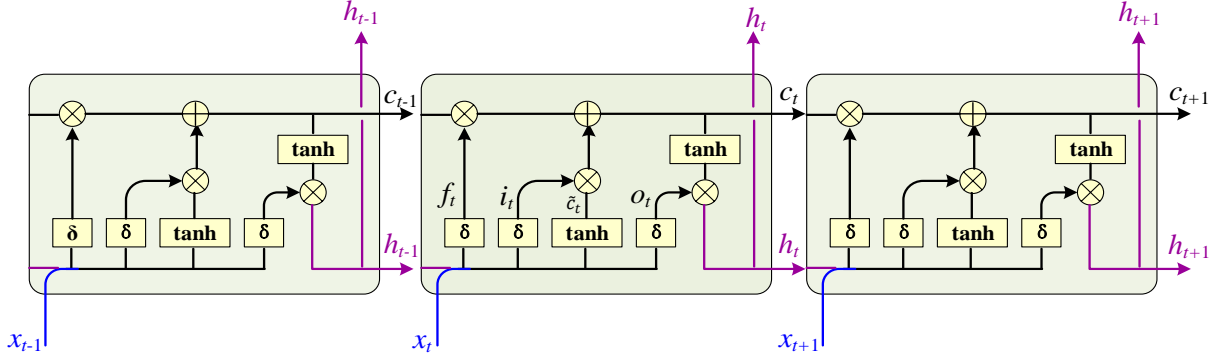
Fig. 3 Architecture of the LSTM-NN.

165

166

167   The x_t and h_{t-1}, which present the hidden state of the LSTM-NN at the previous time, are sent

168   to the LSTM-NN through the three gates. For each gate, the input information is calculated

169   using the logic function. The information at the input gate is processed by a nonlinear function,

170   and added with the state of the memory unit, which is processed by the forget gate, to form a

171   new state of the memory unit c_t. Then output h_t of the LSTM-NN cell is formed through the

172   operation of the nonlinear function and the dynamic control of the output gate by using the

173   following equations:

$$f_t = \delta(W_f x_t + U_f h_{t-1} + V_f c_{t-1} + b_f) \tag{3}$$

$$i_t = \delta(W_i x_t + U_i h_{t-1} + V_i c_{t-1} + b_i) \tag{4}$$

$$o_t = \delta(W_o x_t + U_o h_{t-1} + V_o c_t + b_o) \tag{5}$$

$$c_t = f_t c_{t-1} + i_t tanh(W_c x_t + U_c h_{t-1} + b_c) \tag{6}$$

$$h_t = o_t tanh(c_t) \tag{7}$$

179   where W_f, W_i, W_o, W_c, U_f, U_i, U_o, U_c, V_f, V_i and V_o are the parameters of the matrices, b_f,

180   b_i, b_o and b_c are the bias values, and $\delta(\ )$ is the Sigmoid function.

181

2.4 Deep recurrent neural network

183   The DRNN is another improved version of the original RNN. It has more than one hidden layers

184   and can be directly superimposed with multiple hidden layers or directly added one or more

185   fully connected layers between the two hidden layers. The dropout method [22] can be used to

186   prevent overfitting and improve the predictability of the network. For any hidden layer, the

187   neurons are discarded with a certain probability during training, which makes the neurons

188   inactivate randomly. In this way, not all the neurons are trained, and thus, it can avoid the

189   influence of individual neurons on the network. After training, all the neurons will still be used

190   in the calculation [23].

191

192   In comparison with the RNN, the DRNN has more network layers and parameters and is able

193   to complete large-scale computing tasks and improve the nonlinear capability of the network.

194   In general, if there is sufficient data, the performance of the DRNN is better than that of the

195   single-layer RNN [24].

196

197   **3 Results and Discussion**

198   **3.1 Experimental setup**

199   To examine the effectiveness of the proposed recurrent neural network models for the dynamic

200   prediction of K concentration in biomass fuels, a series of experiments were conducted on a

201   laboratory-scale biomass-air combustion test rig. The experimental setup along with the

202   arrangement of the equipment used is shown in Fig. 4. The test rig consists mainly of a burner

203   resided vertically in an enclosed combustion chamber, a precision screw feeder, and mass

204   flowmeters. A miniature spectrometer (Ocean Optics, USB2000+) with associated application

205   software was used to acquire the spectroscopic signal of the flame. The spectrometer has an

206   optical fibre probe with an angle of view of 25 °and a 2048-pixel linear array CCD, offering

207   good accuracy and repeatability over the considered spectral range (slit: 25 μm, optical

208   resolution: 1.7-2.1 nm at the full width at half maximum, signal-to-noise ratio: 250:1). The

209   height of biomass combustion flame is about 10-15 cm. The distance between the tip of the

210   optical fiber probe and the flame was measured to ensure the tip of the probe optically covers

211   the whole flame. Five typical biomass fuels, i.e., peanut shell, corn cob, corn straw and wheat

212   straw were used in the experiments. The pre-pulverised biomass in the hopper, in the form of

213   powder between 100 and 200 meshes, was fed into the fuel pipe system via the screw feeder

214   and then pneumatically conveyed to the burner before being injected into the combustion

215   reaction zone. The amount of fed biomass is controlled by varying the feeding frequency of the

216   feeder. Methane at a fixed flowrate of 0.5 L/min was used to support the combustion at the

217   initial stage of the biomass-air combustion. A variety of test conditions were then obtained

218   through the combination of different biomass and air supplies. The spectrometer acquired the

219   spectral intensity of the biomass-air flame under different combustion conditions over the

220   spectral range of 200 nm -1100 nm. The data acquisition and storage are realized using

221   SpectraSuite software (supplied by the spectrometer supplier). Through this software, the

222   spectral signal of the specified band is acquired with up to three decimal places at most. If the

223   decimal place of the specify band exceeds 1, the spectrometer will automatically locate the

224   signal closest to the specify band. A multi-channel thermometer with 8 k-type thermocouples

225   was also used to measure the temperature of the flame. Both the signals were transmitted to the

226   computer system for further computation.
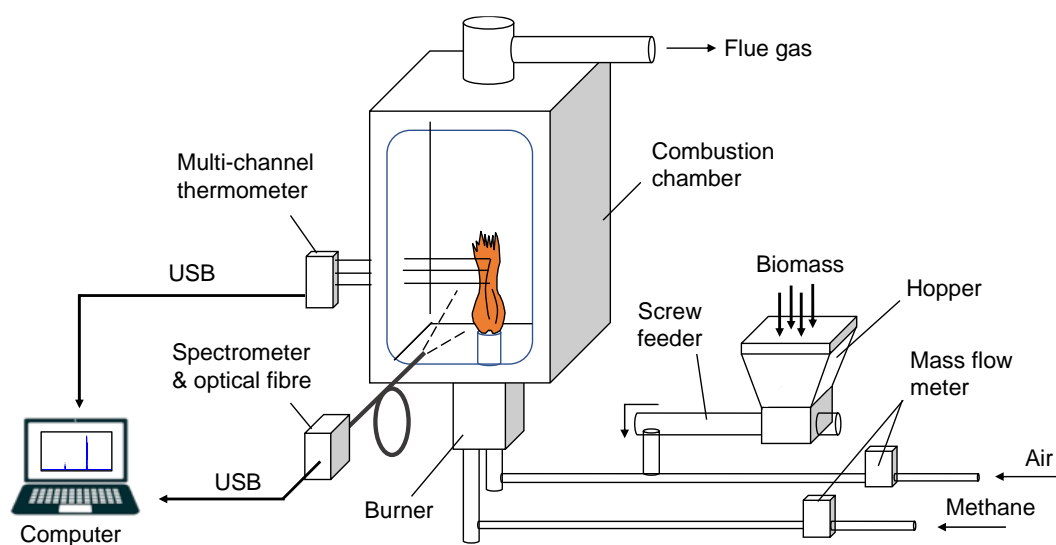
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228   **Fig. 4 Experimental setup.**

229   **3.2 Analysis of biomass fuels**

230   The proximate and ultimate analyses of the five biomass fuels are summarised in Table 1. The

231   volatile and fixed carbon are combustible components whereas moisture and ash are non-

232   combustibles. As can be seen, the wheat straw and corn straw have the highest ash content

233   among the five biomass fuels. The K concentration, which has significant influence on slagging,

234   exists in ash. The higher the ash content, the easier the slagging during combustion. The K

235   concentrations of biomass fuels and their blends were analysed with the support of a

236   professional testing agency. Each biomass sample was digested for the element analysis. Each

237   fuel sample had a total of 0.6 g and was split into three equal proportions to conduct three

238   repeated measurements. Each test was done by using firstly nitric acid and hydrofluoric acid to

239   digest the volatile elements of the sample in an enclosed Teflon digestion tank, and then boric

240   acid solution to remove fluoride. The remained solid sample was further digested by a digester

241   (SPEED-WAVE, Germany) to obtain clean solution. Finally, the K concentration in the

242   solution was measured by an inductively coupled plasma atomic emission spectrometer

243   (Leeman Labs Prodigy, USA). Table 2 summarizes the K concentrations of the tested biomass

244   fuels and their blends along with their measurement uncertainties. For each fuel, the K

245   concentration is the mean of the three repeated measurements whilst the measurement

246   uncertainty is the averaged deviation of the three measurements from the mean.

247   **Table 1. Proximate and ultimate analysis of the tested biomass fuels (as received).**

Biomass	Moisture (%)	Volatile (%)	Ash (%)	Fixed Carbon (%)	C (%)	O (%)	H (%)	S (%)	N (%)
Peanut shell	7.87	70.23	4.21	17.69	43.03	49.52	5.56	0.51	1.37
Willow	9.70	69.93	3.22	17.14	44.67	49.24	5.33	0.56	0.20
Corn cob	5.87	74.55	1.34	18.24	39.68	59.62	<0.1	0.51	0.19
Corn straw	9.50	64.73	9.06	16.70	38.57	44.59	5.17	0.46	1.19
Wheat straw	10.18	58.66	17.58	13.58	32.17	63.18	3.97	0.43	0.26

248

249 **Table 2. K concentrations of the tested biomass fuels and their blends.**

| Biomass	Peanut shell	Willow	Willow & Corn cob*	Corn cob	Corn cob & Corn straw*	Corn straw	Corn cob & Wheat straw*	Wheat straw
K concentration （μg/g）	2600	3400	5695	5845	10943	13265	16147	21495
Measurement uncertainty （μg/g）	±4.93	0.00	±9.93	±19.88	±2.49	±4.99	±2.49	±74.88

250 Note: * mixed equally (50:50) in mass.

251

252 3.3 Spectroscopic characteristics of K in biomass fuels

253 Fig.5 shows the spectral intensity distribution of a willow flame, where two peaks at 588.99 nm

254 and 769.89 nm attribute to Na and K elements, respectively. As can be seen, the spectral

255 intensities of Na and K are in the order of 10^4 with a reference to the spectral intensities of the

256 flame in other wavelength ranges.
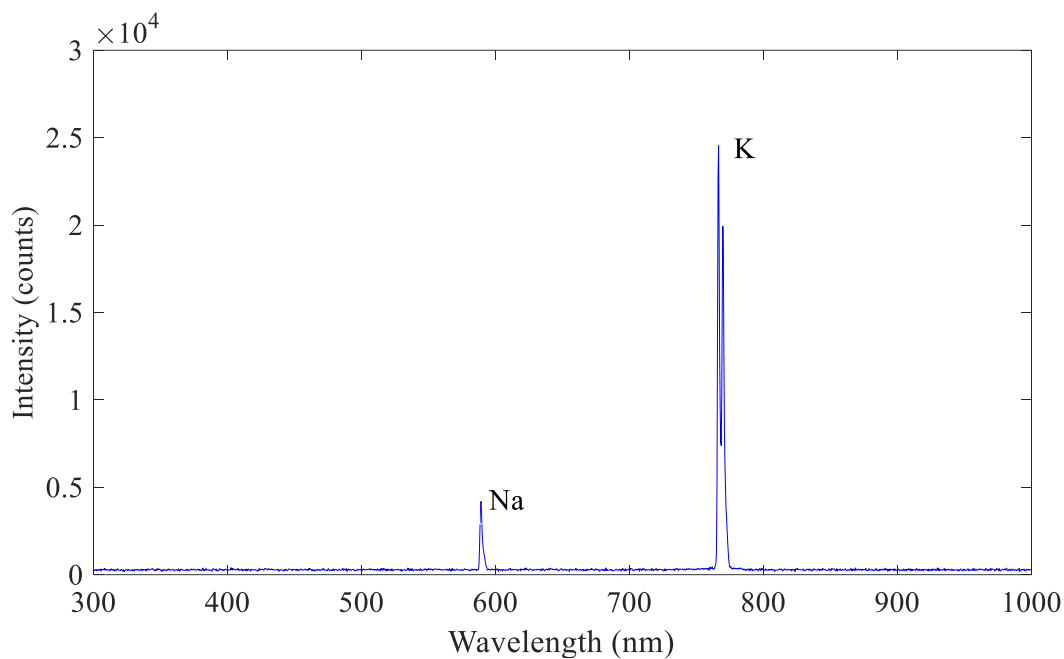
257

258 **Fig. 5 Spectral intensity distribution of a willow flame.**

259   In order to investigate the spectroscopic characteristics of K in biomass during the combustion

260   process, willow and wheat straw were fired on the test rig. Different fuel flowrates were

261   achieved by alternating the speed of the screw feeder whilst the methane and air flow rates

262   remained constant. The feeding frequency of the screw feeder was set to 3 levels, 2 Hz, 3 Hz

263   and 4 Hz. The miniature spectrometer collected the spectral intensities of the K for the two

264   biomass fuels, which the integration time is 10 ms.

265

266   In order to establish the relationship between the amount of fuel and feeding frequency,

267   calibration experiments were conducted. The range of feeding frequency of screw feeder is

268   from 0 Hz to 30 Hz. The amount of fuel was measured at a 5 Hz increment. The calibration test

269   was repeated for 10 times at each speed frequency. The feeding frequency, amount of fuel

270   supplied under different frequency, are plotted in Fig.6. There exists a linear relationship

271   between the amount of fuel supplied and the feed frequency. Because the diameter of the burner

272   is very small, the burner will be blocked if the fuel feed rate is too high during the test. Therefore,

273   the frequency of the feeder is set to 2 Hz, 3 Hz and 4 Hz in this study. Such feeder rates allow

274   the fuel to be fully injected to the burner for combustion.

275
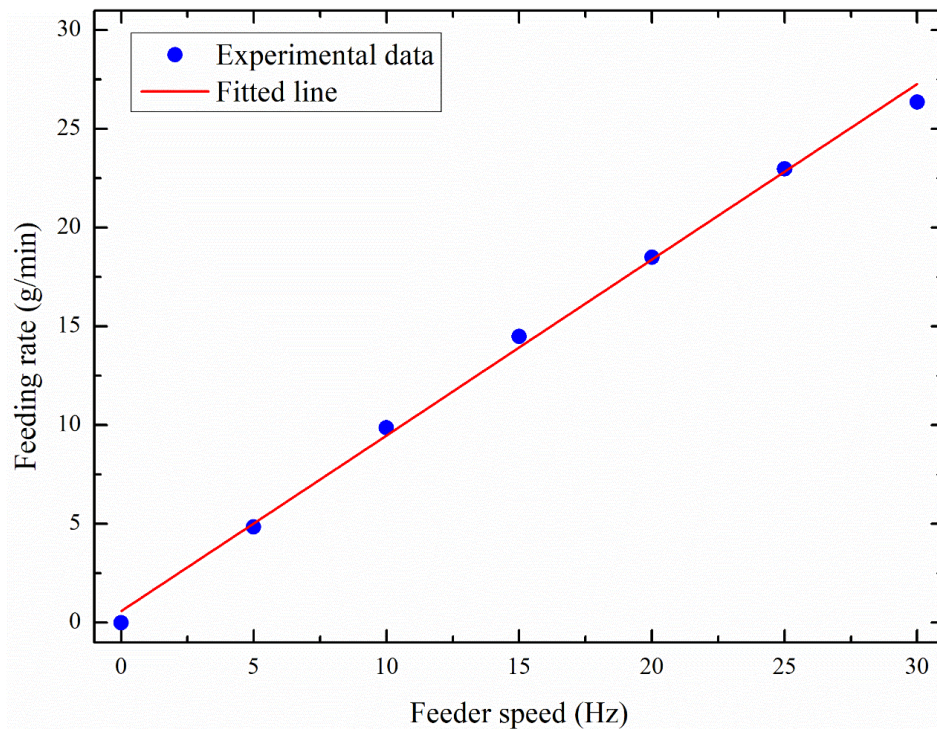
Fig. 6 Screw feeder calibration results.

The mean spectral intensities and standard deviations (as error bars) of K concentration in willow / wheat straw flames for three different fuel flowrates are plotted in Fig.7, where each data point was computed for 12,000 readings. It is evident that the spectral intensity of K in the wheat straw flame is higher than that in the willow flame. Table 2 shows that the K concentration in wheat straw is higher than that in willow. This also verified that emission intensity of alkali depends on alkali concentrations in the samples[12]. It is also clear that the spectral intensity of K has positive correlation with the fuel flowrate, i.e., the greater the fuel flowrate, the stronger the spectral intensity of K. The K concentration in the flame increases with the amount of fuel. For a large amount of fuel, more K concentration is released when the fuel is completely burnt under the same combustion conditions.
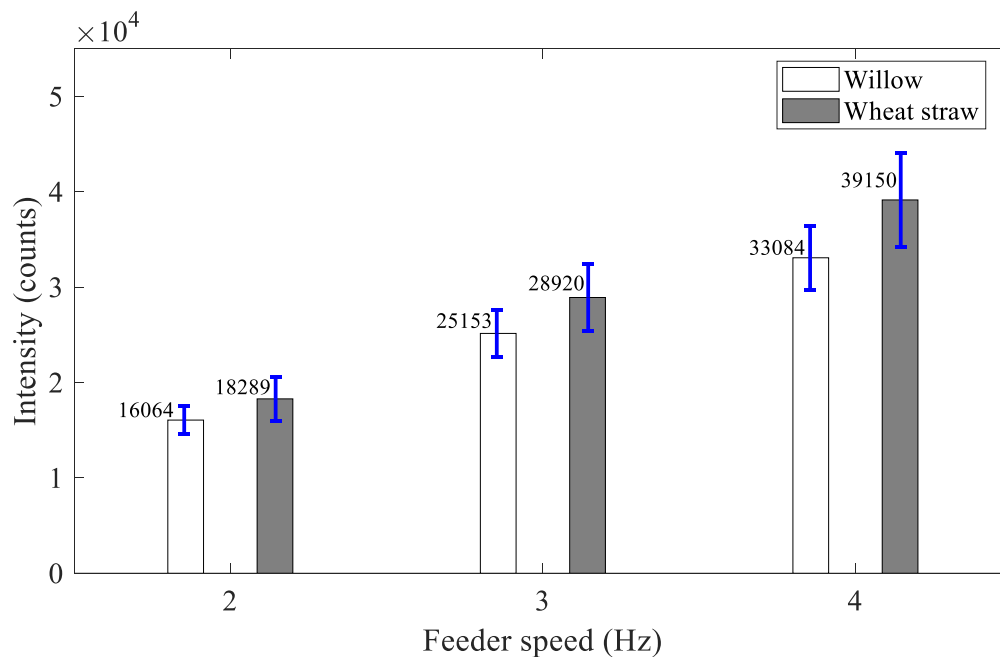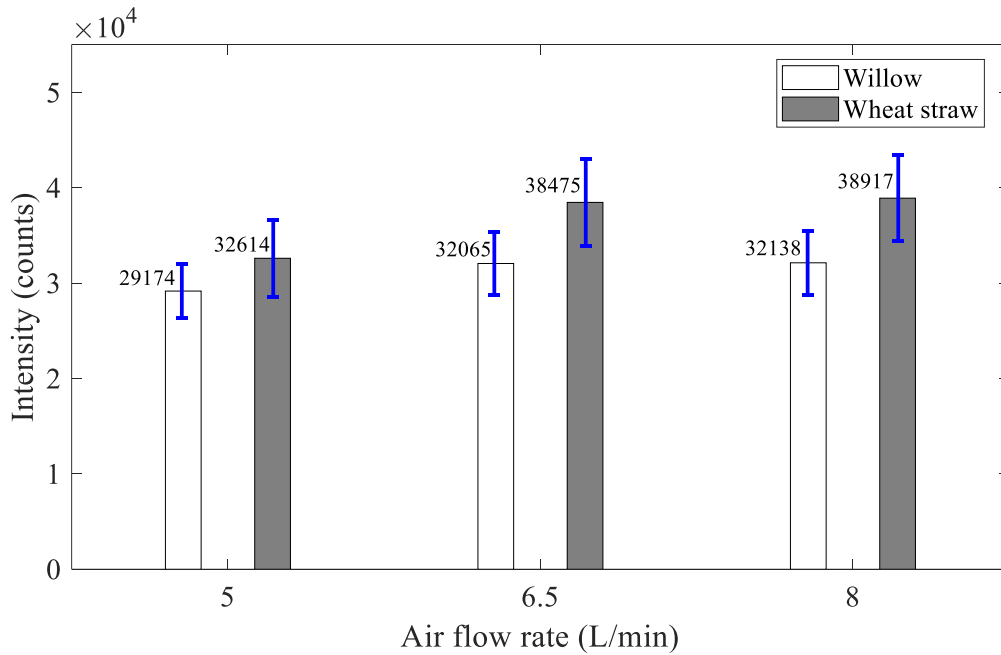
Fig. 7 Mean spectral intensities of K in willow and wheat straw flames under different fuel flowrates.

Similarly, Fig. 8 illustrates the means and standard deviations (as error bars) of the 12,000 readings in willow / wheat straw flames for three different air flowrates under the feeder speed of 3 Hz and the methane flow rate of 0.5 L/min. As can be seen, the spectral intensity of K in the wheat straw flame is still higher than that in the willow flame. It is related to the K concentration in the fuel. When the amount of fuel is constant, the complete combustion depends on the amount of air. The air flowrate has a little impact on the spectral intensity of K in both the biomass flames. The reason is that it is complete combustion under different air flowrates. It is also found that the spectral intensities of K in the willow / wheat straw flames under air flowrates of 6.5 L/min and 8.0 L/min are about 10% higher than that under 5.0 L/min, which is believed to be due to the increased combustion intensity under higher air flowrates. It illustrates that the spectral intensity of K is related to the biomass fuel type and combustion state.

302

303   **Fig. 8 Mean spectral intensities of K in willow and wheat straw flames under different**

304   **air flowrates.**

305   **3.4 Dynamic prediction of K concentration**

306   **3.4.1** *Data pre-processing and feature extraction*

307   Experimental data for the five biomass fuels and three blends, i.e., willow & corn cob, corn cob

308   & corn straw, and corn cob & wheat straw, mixed equally (50:50) in mass (Table 2), were used

309   to construct the RNN model for the dynamic prediction of the K concentration. Data pre-

310   processing was carried out to remove the dark noise, blackbody radiation and outlier data during

311   the data acquisition. The dark noise was caused by the weak dark current in the CCD sensor of

312   the spectrometer. It was filtered by applying appropriate thresholding values to the

313   spectroscopic signals. The continuous spectrum is excluded in the data pre-processing. It is

314   about 1% of the spectral intensity of K (refer to Fig. 5) in all the cases studied, which is removed

315   by subtracting it from the original signal in the application software.

316

317   After the data pre-processing, a total of 12000 flame spectroscopic data including flame

318   temperature and the corresponding K concentration (refer to Table 2), were created, where

319 every 30 spectroscopic data were grouped, making a total of 400 sets of sample data for each

320 biomass fuel under each test condition. Five single biomass fuels and three blends (refer to Table

321 1) were tested at a feeder rate of 3 Hz under the methane flow rate of 0.5 L/min and the air of

322 5.0 L/min, making a total of 3200 sets of data available for the construction and validation of the

323 three models.

324

325 The spectroscopic features of K, including mean, variance, peak-to-peak value, skewness and

326 kurtosis coefficients, were extracted from the spectroscopic signal. The skewness and kurtosis

327 coefficients reflect the asymmetry and steepness of the probability density function of the signal,

328 which are the third- and four-order moments of the signal, respectively, i.e.,

329
$$S_k = \frac{1}{N}\sum_{i=1}^{N}\frac{(x_i-\mu)^3}{\sigma^3} \tag{9}$$

330
$$K_u = \frac{1}{N}\sum_{i=1}^{N}\frac{(x_i-\mu)^4}{\sigma^4} \tag{10}$$

331 where x_i is the radiation intensity of the i-th sample of the signal, μ and σ are the mean and

332 standard deviation of the sample, respectively, and N is the number of samples and set to be 30

333 in this paper.

334

335 For each biomass fuel, the mean and standard deviation of flame temperatures, mean oscillation

336 frequency [25] , mean skewness coefficient and mean kurtosis coefficient are summarized in

337 Table 3. A multi-channel thermometer with 8 k-type thermocouples was used to measure the

338 temperatures at different points within the flame region. The thermocouples were arranged in

339 two levels around the flame. For each tested biomass fuel, the flame temperature is the mean of

340 the temperatures given by the 8 k-type thermocouples, which is presented in Table 3. The

341 properties of the biomass, such as moisture, volatile, ash and fixed carbon, all have certain

342 influence on the characteristics of the flame. For instance, the higher the ash content, the lower

343 the thermal efficiency, and hence the relatively lower flame temperature. The volatile and ash

344   content of corn cob is the highest and smallest, respectively, among the five single biomass

345   fuels (refer to Table 1), so the flame temperature of corn cob is higher than that of other biomass

346   fuel. For the five biomass fuels and their blends, the oscillation frequency of the wheat straw

347   flame is slightly higher than that of other fuels and the skewness coefficient of K spectral

348   intensity of the corn straw flame are the highest among the eight biomass fuels.

349   **Table 3. Flame temperature, oscillation frequency, skewness and kurtosis coefficients of**

350   **for biomass fuels and their blends.**

Biomass	Mean temperature (°C)	Standard deviation of temperature (°C)	Oscillation frequency (Hz)	Skewness coefficient	Kurtosis coefficient
Peanut shells	1024.09	57.05	2.885	-0.006	2.536
Willow	1021.38	43.88	2.912	0.020	2.493
Willow & Corn cob	1000.56	47.92	2.879	0.003	2.452
Corn cob	1051.59	49.39	2.870	0.014	2.430
Corn cob & Corn straw	983.22	55.99	2.953	0.001	2.316
Corn straw	1039.49	49.57	2.937	-0.033	2.393
Corn cob & Wheat straw	970.53	44.59	2.979	-0.027	2.423
Wheat straw	959.43	52.78	3.246	0.019	2.449

351

352   For each biomass fuel, the flame radiation energy, mean, variance and peak-to-peak value of

353   K spectral intensity are shown in Fig. 9. Figs. 9(a) and 9(b) indicate that there is a significant

354   difference in the flame radiation energy and mean of K spectral intensity between the biomass

355   fuels. The flame radiation energy and mean of K spectral intensity of wheat straw and corn cob

356   & wheat straw are significantly higher than those of peanut shells and willow. The flame

357   radiation energy and mean of K spectral intensity of the biomass fuels are consistent with the

358   K concentrations. It is noted that small step changes in the radiation energy and mean of K

359   spectral intensity (Figs. 9(a) and 9(b)) exist and this is believed to be related to the type of

360   biomass being fed and the operating characteristics of the screw feeder. The variance and peak-

361   to-peak value of K spectral intensity of the fuels are also very different, as shown in Figs. 9(c)

362 and 9(d). In addition, the variance and peak-to-peak value of the wheat straw and corn cob &

363 wheat straw flames fluctuate widely. The flame radiation energy and oscillation characterise

364 the combustion state of the biomass fuel whilst the flame temperature is related to the K

365 concentration. The characteristic parameters (e.g., mean, variance, peak-to-peak value,

366 skewness and kurtosis coefficients) of the K spectroscopic signal are good descriptors of the K

367 spectroscopic signal and thus can reflect the combustion behaviours of biomass fuels. Therefore,

368 they are selected for the prediction of K content in the models.
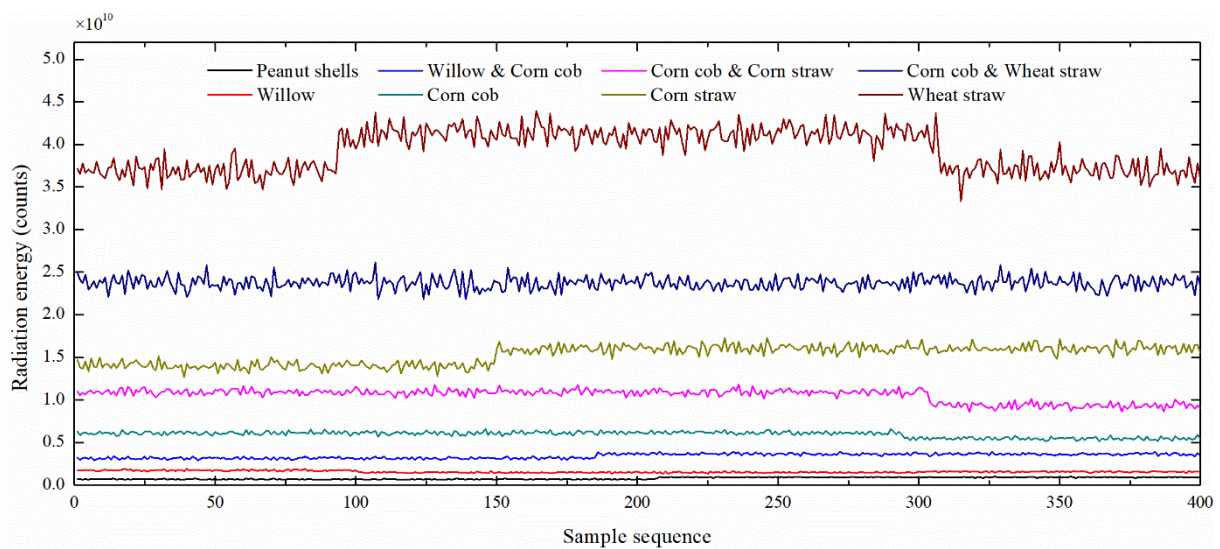
369

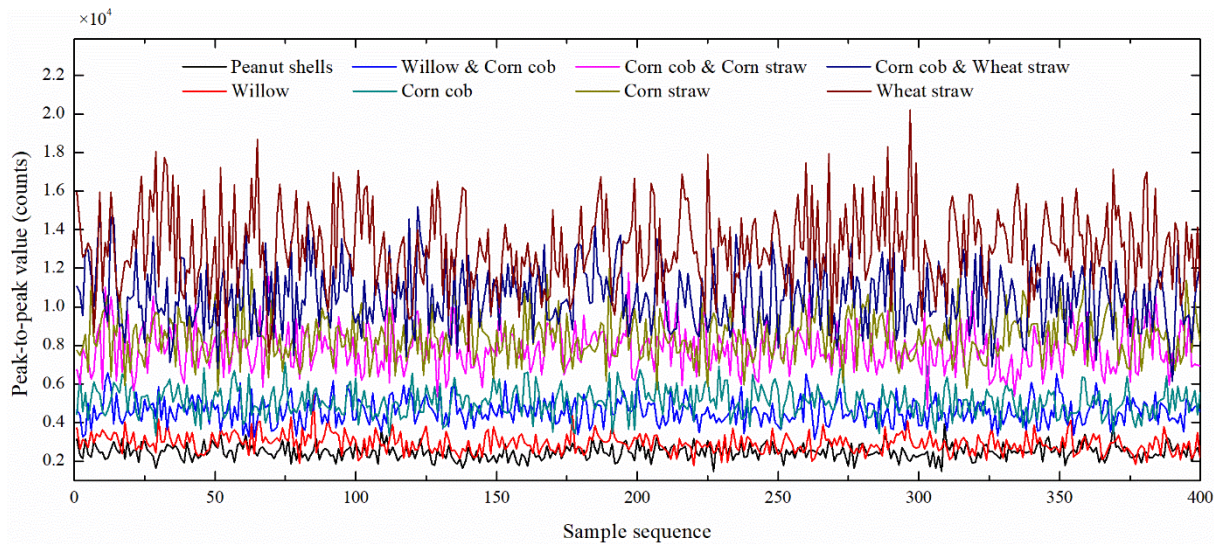370 **(a) Flame radiation energy.**
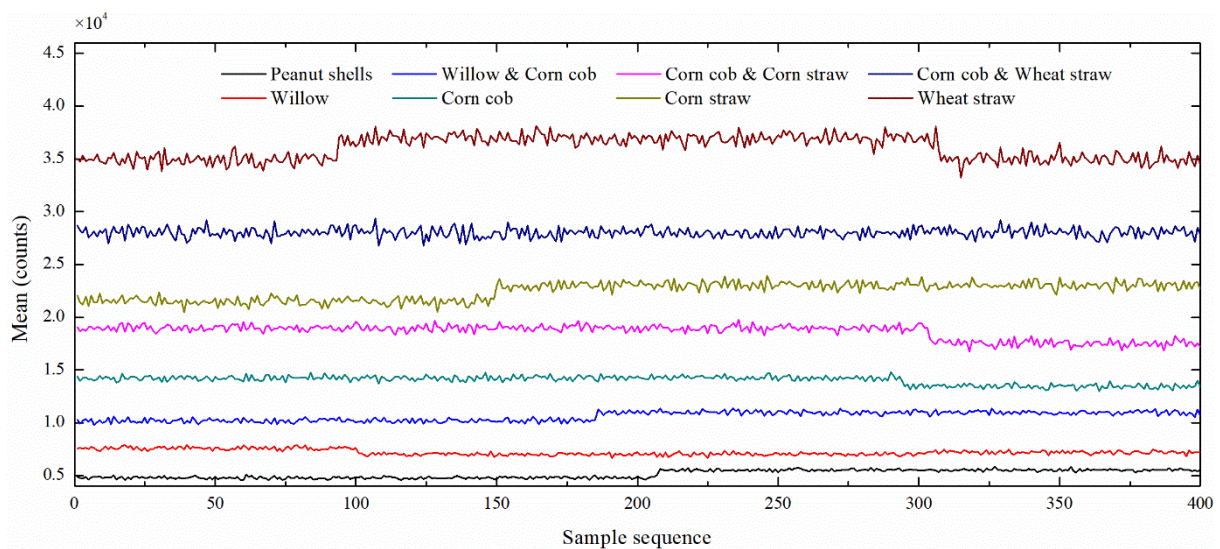
371

372 **(b) Mean of K spectral intensity.**
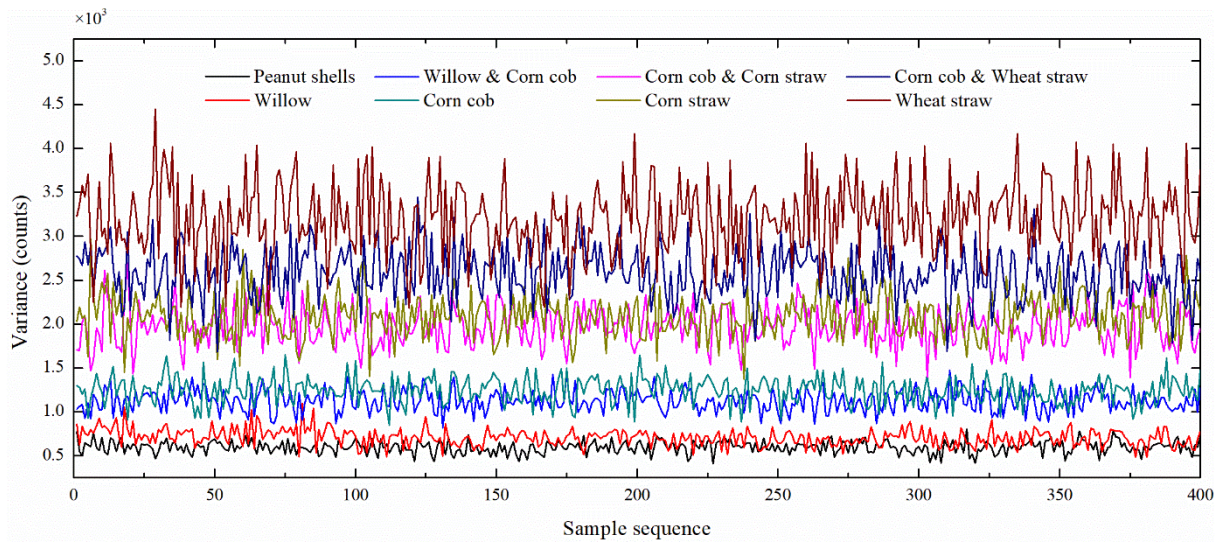
373

374   **(c) Variance of K spectral intensity.**

375

376   **(d) Peak-to-peak value of K spectral intensity.**

377   **Fig. 9 Radiation energy, mean, variance and peak-to-peak of K spectral intensity**

378

379   **3.4.2** *Construction and training of the RNN, LSTM-NN and DRNN models*

380   Table 4 summarized the network parameters of the three models to be constructed. The inputs

381   to the networks conclude the flame temperature, oscillation frequency, radiation energy and

382   spectroscopic features of K including mean, variance, peak-to-peak value, skewness and

383   kurtosis coefficients. The output of each network is the predicted K concentration. The

384   activation functions of the hidden layer and the fully connected layer are the tanh function and

385 the Leaky ReLU function, respectively. The Leaky ReLU increases the non-linear capability of

386 the network, which makes the networks trained easier and prevents possible neuron inactivation.

387 The key features that are identified to train the models are plotted in Fig.9. However, since

388 some of the features such as flame temperature, oscillation frequency and skewness and kurtosis

389 coefficients appear very similar between the biomass fuels, only their mean values are listed in

390 Table 3.

391 **Table 4. Structural parameters of the models.**

| Model	RNN	LSTM-NN	DRNN
Number of hidden layers	1	1	5
Number of neurons in hidden layer	20	20	20×5
Number of fully connected layers	6	6	6
Number of fully connected layer neurons	20×2, 30×2, 10×2		
Activation function	tanh，Leaky ReLU		

392

393 **3.4.3.** *Prediction of K concentration in biomass*

394 The prediction results of the K concentration using the RNN, LSTM-NN and DRNN models

395 and the corresponding errors are plotted in Figs. 10-13. The *k*-fold cross-validation method was

396 used to evaluate the performance of the models. In this method, the sample data were divided

397 into *k* sets, one of which was selected randomly to test the model, and the rest to train the model.

398 The test set was selected randomly for *k* times, and the accuracy of three prediction models are

399 the average of the prediction accuracies for *k* times. The *k*-fold cross-validation method has an

400 advantage of non-repeated sampling and is often used to optimise the hyper-parameter so that

401 the model has the best generalisation performance. In this study, *k* was selected to be 10, i.e.,

402 the 10-fold cross-validation was implemented. A total of 2880 sets of data were used as the

403 training set, and 320 as the test set for 10 times. The final results from the three models for each

404 biomass fuel were the average of 10 readings. The short horizontal bars at each data point in
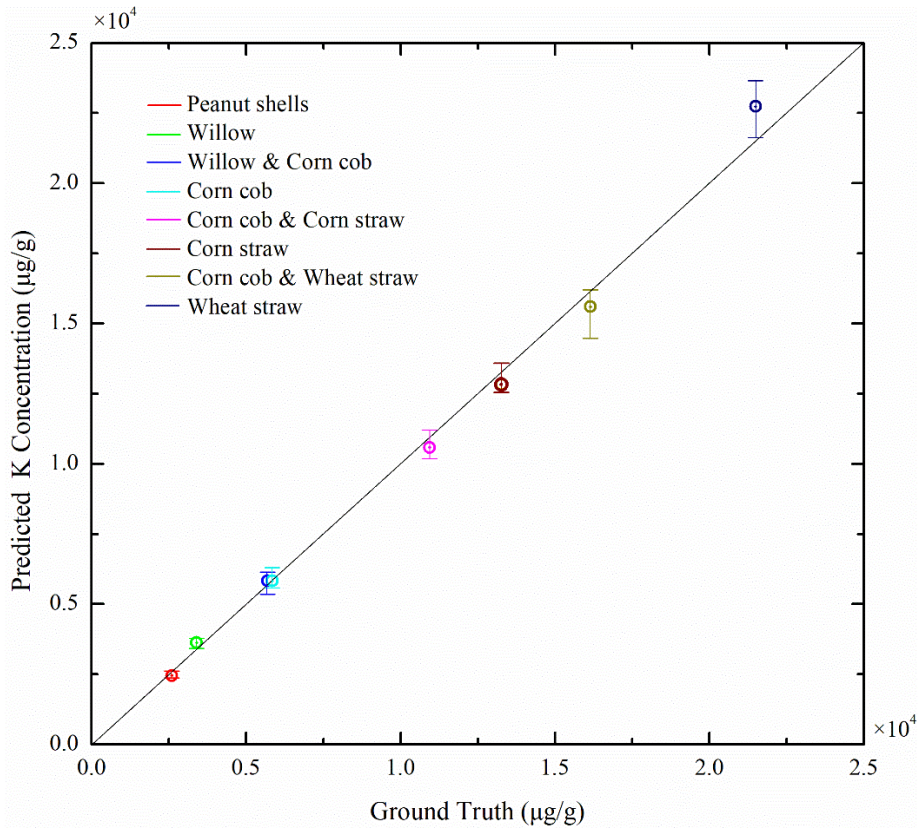
405   Figs.10-12 indicate the upper and lower limits of the 10 repeated tests for each biomass fuel.

406   Fig. 13 shows a quantitative comparison of the relative errors for the three models.
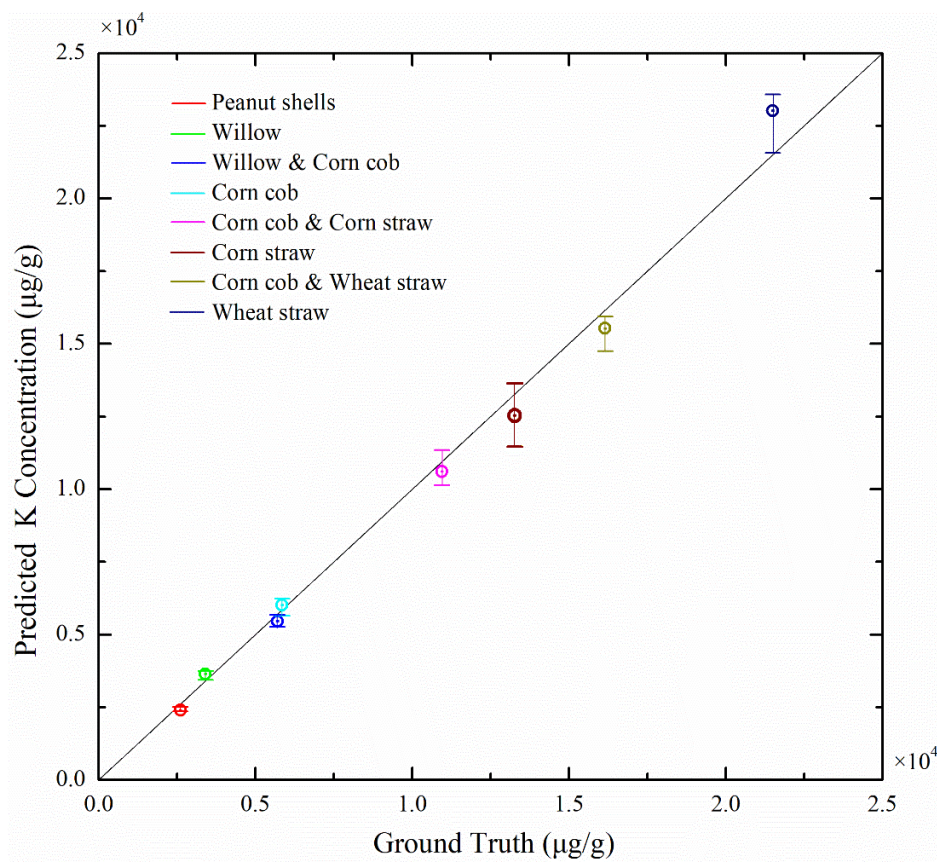
407

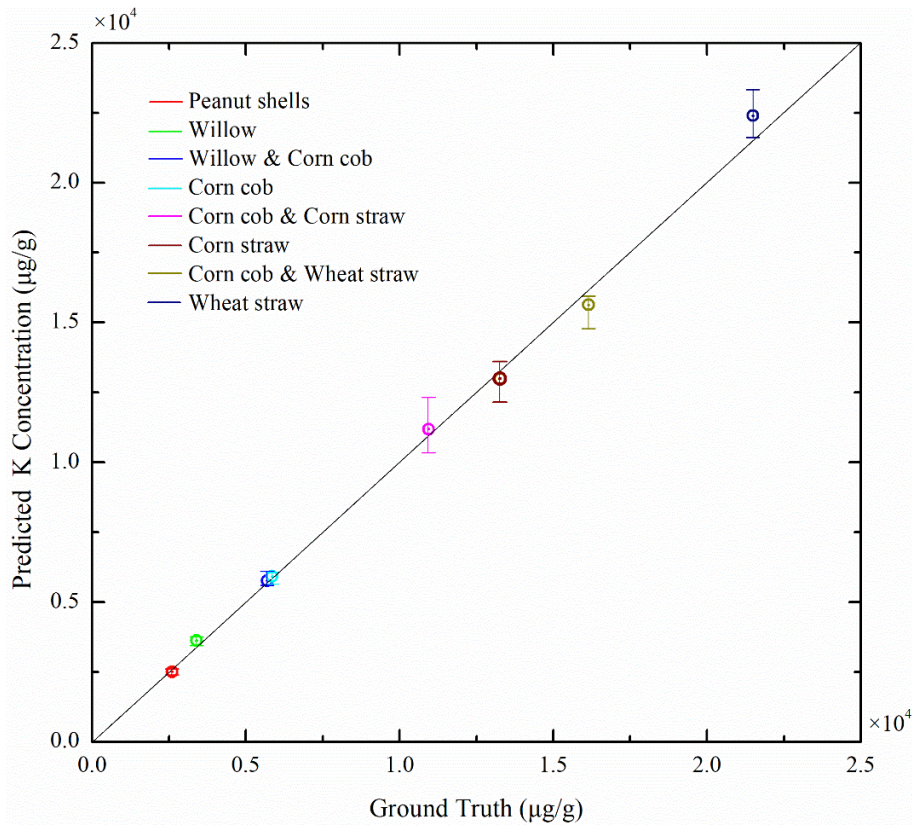408   **Fig.10 Predicted K concentration based on RNN with reference to the ground truth.**

409

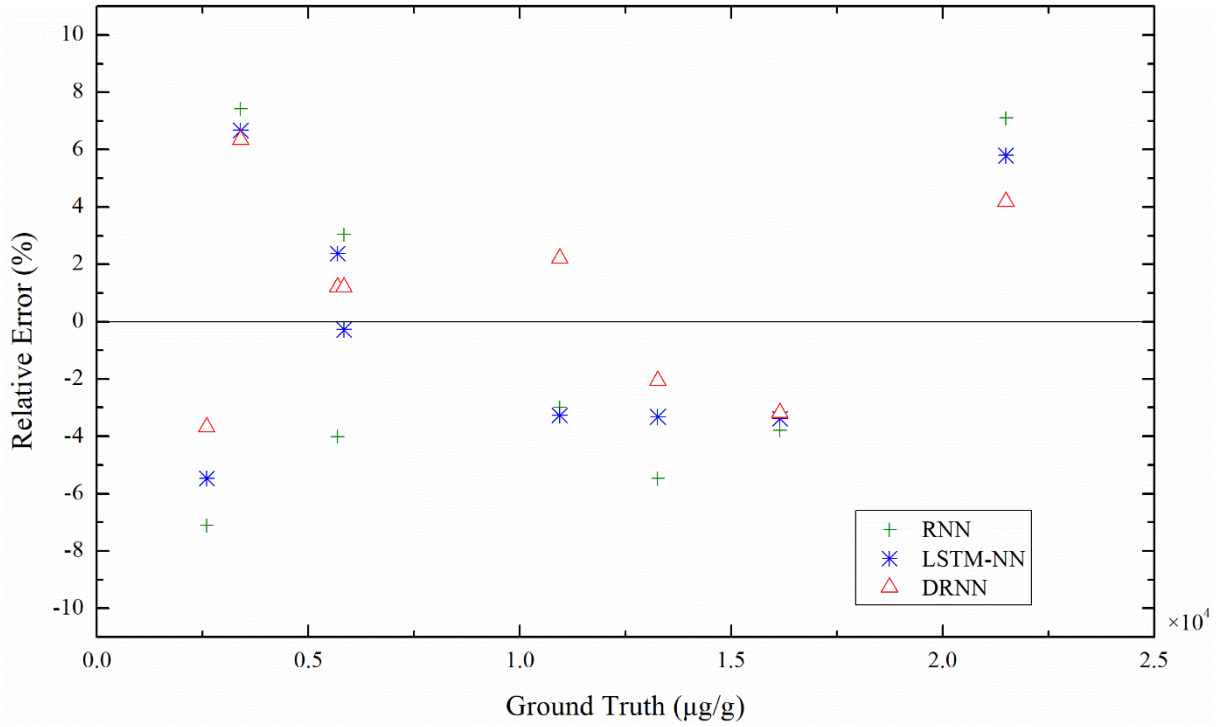Fig.11 Predicted K concentration based on LSTM-NN with reference to the ground
truth.

Fig.12 Predicted K concentration based on DRNN with reference to the ground truth.

414

Fig.13 Relative errors of the three RNN models.

Fig.13 shows that the three RNNs can predict the K concentration in the biomass fuels with a relative error range of (-7.11%, 7.43%), (-5.47%, 6.67%), (-3.18%, 6.34%), respectively, It is clear that the DRNN model yields the smallest error among the three models under all the test conditions. In addition, the relative error for the biomass with higher K concentration (e.g., wheat straw and corn straw) is smaller than that for the biomass with low K concentration (Table 2). This may attribute to a greater signal-to noise ratio of the spectral intensity signal under that conditions.

The following metrics are employed to evaluate the prediction performance of the RNN, LSTM-NN and DRNN models.

$$\delta_{\mathrm{MAE}} = \frac{1}{n}\sum_{i=1}^{n}\left|y_i - y_i'\right| \tag{11}$$

$$\delta_{\mathrm{MAPE}} = \frac{1}{n}\sum_{i=1}^{n}\left|\frac{y_i - y_i'}{y_i}\right| \times 100\% \tag{12}$$

$$\delta_{\mathrm{RMSE}} = \sqrt{\frac{1}{n}\sum_{i=1}^{n}(y_i - y_i')^2} \tag{13}$$

429 Where δ_{MAE} is the mean absolute error (MAE), δ_{MAPE} is the mean absolute percentage error

430 (MAPE), δ_{RMSE} is the root mean square error (RMSE), y_i is the ground truth, y_i' is the K

431 concentration predicted by the different recurrent neural networks, and n is the total number of

432 test samples.

433

434 Table 5 shows a comparsion of the evaluation metrics for the RNNs. For the tested biomass

435 fuels and their blends, the K concentration ranges from 2,600 μg/g to 21,495 μg/g. The ratio

436 between the maximum and minimum K concentrations is around 8. The difference in the ground

437 truth of the K concentration between the tested biomass fuels (Table 2) is very large and so is

438 the RMSE of the three prediction models. The MAPE of the three RNN models are all small,

439 indicating good performance of the models. The training time and computational time for each

440 model are also evaluated, as summarised in Table 5. It is found that the DRNN and LSTM-NN

441 models have a longer computational time than the RNN. It is thought that the architecture of

442 the DRNN model is more complex than those of the RNN and LSTM-NN models, resulting in

443 a longer computational time.

444 **Table 5. Performance comparison of three recurrent neural networks.**

	RNN	LSTM-NN	DRNN
RMSE (μg/g)	574.15	563.01	515.29
MAE (μg/g)	481.37	490.99	435.92
MAPE (%)	4.72	4.52	4.04
Maximum errors (%)	7.42	6.67	6.34
Training time (s)	10^1	10^2	10^2
Computational time (s)	10^{-3}	10^{-2}	10^{-2}

445

446 In comparison with the work presented in references [11-16], the online measurement of K

447 concentration is realized through the prediction models instead of experimental analysis of fuels.

448 Other researchers [13,15] established a functional relationship between the spectral intensity of

449 alkali metal, flame temperature, and alkail metal concentration based on experimental data,

450 where the emission characteristics of alkali materials at different combustion temperatures and

451 during different combustion stages were examined. In this paper, however, the models for the

452 prediction of K concentration in a biomass fuel have been established through feature extraction

453 of K spectroscopic signals.

454

455 For purpose of a direct comparison with the RNNs, data driven models based on the

456 conventional BP neural network (BP-NN) and support vector machine (SVM) are also

457 established and trained to predict the K concentration of biomass fuels. The BP-NN has a

458 structure of a 7-layer full connection layer with an activation function of Leaky ReLU. In the

459 SVM algorithm the kernel function used is RBF function with kernel parameter of 0.7017 and

460 penalty factor of 0.3536. The comparative results and relative error of all models for the

461 prediction of K concentration are plotted in Fig. 14 and Fig. 15, respectively. The relative error

462 range in the K concentration prediction using the BP-NN and SVM models are (-7.29%, 7.86%)

463 and (-8.71%, 8.91%), respectively. The average errors for the BP-NN and SVM models, i.e.

464 5.87% and 7.31%, respectively, are consistently greater than those of the three RNNs, which

465 are 5.12%, 3.82% and 3.01%, respectively. It is clear that the RNNs have all outperformed the

466 BP-NN and SVM.

467
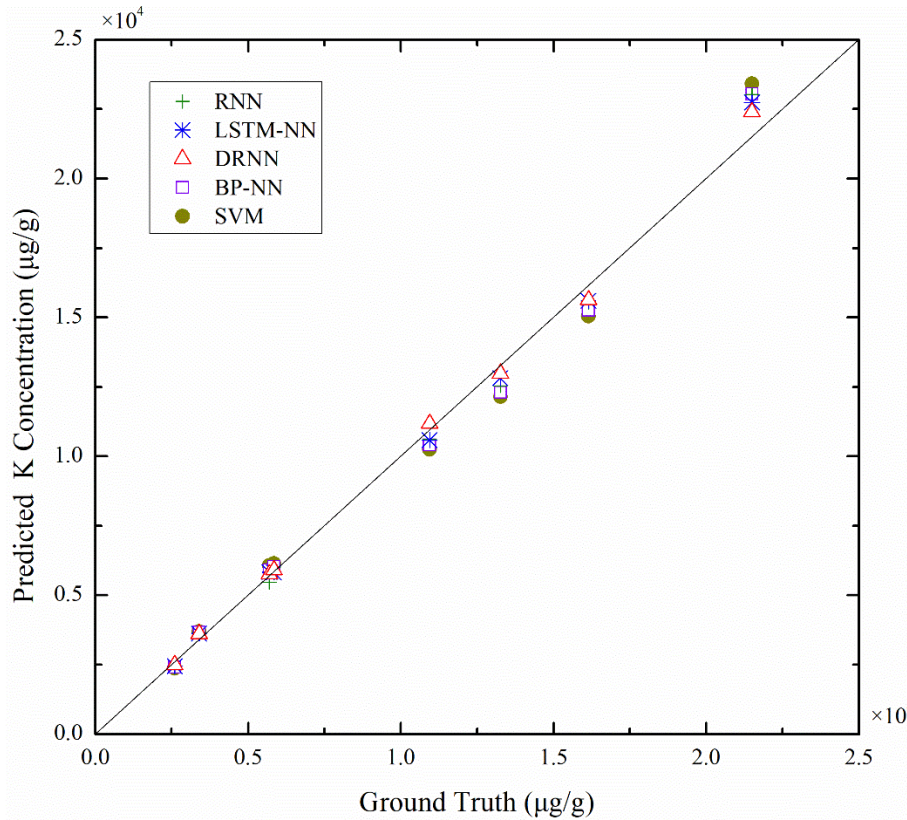
Fig.14 Predicted K concentration based on the BP-NN, SVM and RNN models.

469
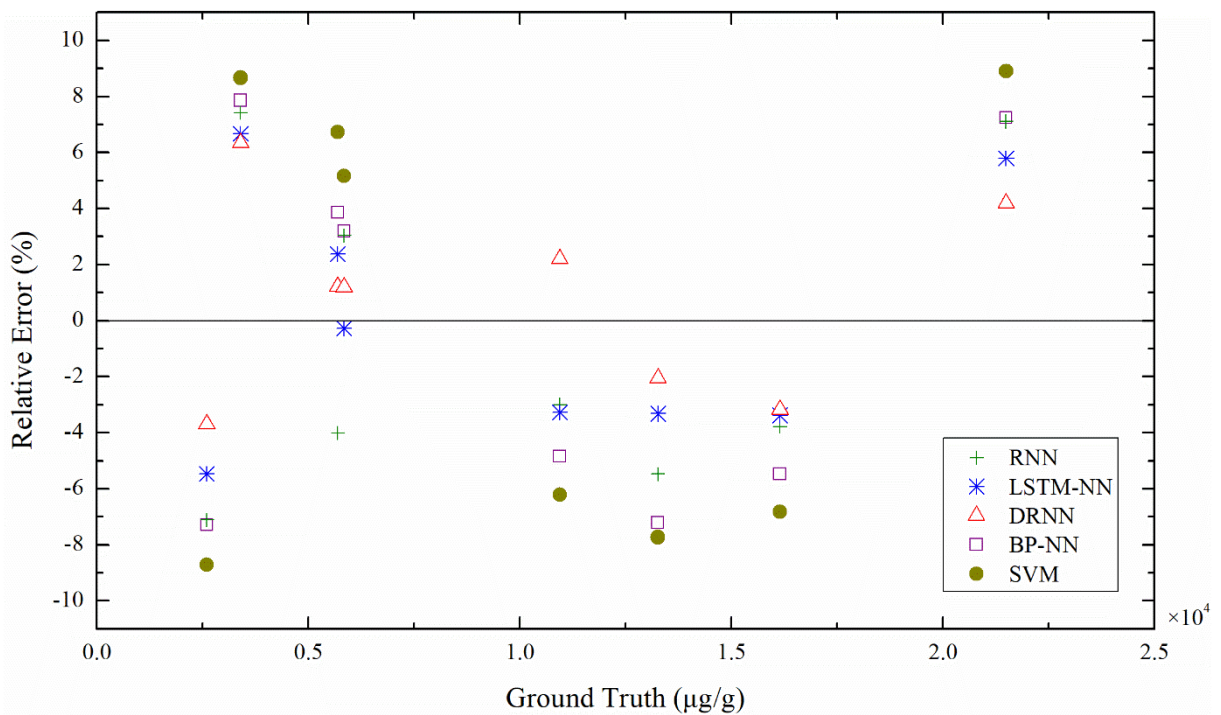
Fig.15 Relative errors of the RNN models in comparison with the BP-NN and SVM

4 Conclusions

The recurrent nerual networks for the dynamic prediction of K concentration in biomass fuels based on the spectroscopic characteristics of flames have been presented. For willow and wheat straw, experimental tests were conducted under different feeder speeds and air flowrates. The results have verified that the emission intensity of alkali depends on alkali concentration in the fuel and that the spectral intensity of K has positive correlation with the fuel flowrate, i.e., the greater the fuel flowrate, the stronger the spectral intensity of K. For the five single biomass fuels and three blends, the spectroscopic distribution of the flame and hence the K concentration are obtained and analysed. The characteristic parameters are analysed, including the flame radiation energy, oscillation frequency, flame temperature and other parameters (e.g., mean, variance, peak-to-peak value, skewness and kurtosis coefficients) of the K spectroscopic signal. The results have demonstrated that these characteristic parameters are good descriptors of the K spectroscopic signal and can thus reflect the combustion behaviours of the biomass fuels. The comparative results in terms of the evaluation metrics have demonstrated that the prediction models, RNN, LSTM-NN and DRNN, have all performed well in predicting the K concentration with the DRNN model slightly outperforms the other two with a relative error within 6.34%. The three RNN models have consistently outperformed the BP-NN and SVM models. In future work the likelihood of slagging in a biomass furnace will be predicted from the K concentration in order to minimise unexpected downtime of the combustion process.

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