

Quantitative theory of triplet pairing in the unconventional superconductor LaNiGa₂

Sudeep Kumar Ghosh^{ⓧ,1,*} Gábor Csire,^{2,3,†} Philip Whittlesea,¹ James F. Annett,² Martin Gradhand,²
Balázs Újfalussy^{ⓧ,4} and Jorge Quintanilla^{1,‡}

¹*Physics of Quantum Materials, School of Physical Sciences, University of Kent, Canterbury CT2 7NH, United Kingdom*

²*H. H. Wills Physics Laboratory, University of Bristol, Tyndall Avenue, Bristol BS8 1TL, United Kingdom*

³*Catalan Institute of Nanoscience and Nanotechnology (ICN2), CSIC, BIST, Campus UAB, Bellaterra, Barcelona, 08193, Spain*

⁴*Institute for Solid State Physics and Optics, Wigner Research Centre for Physics, Hungarian Academy of Sciences, P.O. Box 49, H-1525 Budapest, Hungary*



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The exceptionally low-symmetry crystal structures of the time-reversal symmetry-breaking superconductors LaNiC₂ and LaNiGa₂ lead to an internally antisymmetric nonunitary triplet state as the only possibility compatible with experiments. We argue that this state has a distinct signature: a double-peak structure in the density of states (DOS) which resolves in the spin channel in a particular way. We construct a detailed model of LaNiGa₂ capturing its electronic band structure and magnetic properties *ab initio*. The pairing mechanism is described via a single adjustable parameter. The latter is fixed by the critical temperature T_c allowing parameter-free predictions. We compute the electronic specific heat and find excellent agreement with experiment. The size of the ordered moment in the superconducting state is compatible with zero-field muon spin relaxation experiments and the predicted spin-resolved DOS suggests the spin splitting is within the reach of present experimental technology.

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The superconducting state is a condensate of electron pairs characterized by an order parameter Δ . Usually Δ is a complex scalar, its phase being a manifestation of spontaneously broken gauge symmetry. This is responsible for the macroscopic quantum coherence underpinning quantum devices such as superconducting qubits [1] and superconducting quantum interference devices (SQUIDs) [2]. On the other hand, in so-called “unconventional” superconductors additional symmetries may be broken leading to more complex order parameters with extra degrees of freedom. Of all the features of unconventional superconductors, broken time-reversal symmetry (TRS) is perhaps the most surprising one as it challenges our view of superconductivity and magnetism as antagonistic states of matter. In spite of this, the phenomenon has been detected in numerous systems using zero-field muon spin rotation/relaxation (μ SR). Prominent examples include (U, Th)Be₁₃ [3], Sr₂RuO₄ [4], UPt₃ [5], (Pr, La)(Ru, Os)₄Sb₁₂ [6,7], PrPt₄Ge₁₂ [8], LaNiC₂ [9], LaNiGa₂ [10,11], SrPtAs [12], Re₆(Zr, Hf, Ti) [13–16], Lu₅Rh₆Sn₁₈ [17], and La₇(Ir, Rh)₃ [18,19]. Many of these systems have other unconventional features, while in some cases an independent, direct observation of broken TRS has been made: optical Kerr effect measurement in Sr₂RuO₄ [20] and UPt₃ [21], and bulk SQUID magnetization measurement in LaNiC₂ [22].

Unfortunately it has been difficult to establish the structures of order parameters of these superconductors. This is because, on the one hand, our knowledge of the electron pairing mechanism is not sufficiently detailed to make a prediction. On the other hand, their crystal structures tend to be highly symmetric, leading to many different possible ways of breaking TRS, which limits our ability to work by elimination. TRS-breaking superconductivity requires a degenerate instability channel [23,24] which, for a uniform superconductor, must come from a multidimensional irreducible representation (irrep) of the point group of the crystal. As an example, the point group of Sr₂RuO₄ is D_{4h} , which leads to 22 possible order parameters breaking TRS [23,24]: 20 under the assumption of weak spin-orbit coupling (SOC) and two more in the strong-SOC limit. The family formed by LaNiC₂ [9] and LaNiGa₂ [10] is an exception to this rule, as their crystal structures have exceptionally low symmetry. Their crystal point groups only have four irreps, all of them one dimensional. This precludes TRS breaking in the strong-SOC case and leaves only four possible pairing states, all of them nonunitary triplets [10,25]. One additional complication is the multiband nature of these systems: two [26] and five [27] bands cross the Fermi level of LaNiC₂ and LaNiGa₂, respectively. In fact, both systems show thermodynamic properties that can be fitted with a model assuming fully gapped, two-band superconductivity [11,28,29]. This is inconsistent with the line nodes implied by the earlier symmetry analyses [10,25]. On the other hand, the two-band model does not predict TRS breaking. To resolve the discrepancy it was proposed that only an internally antisymmetric nonunitary triplet pairing (INT) state is compatible with the experimental

*S.Ghosh@kent.ac.uk

†gabor.csire@icn2.cat

‡J.Quintanilla@kent.ac.uk

observations [10,11,25,30]. Here we show that such a state has a very distinct experimental signature: a double-peak structure in the density of states (DOS) which resolves in the spin channel. We construct a model of LaNiGa₂ capturing detailed electronic band structure *ab initio*, with the pairing interaction in the INT state reduced to a single, adjustable parameter. The known value of the critical temperature T_c fixes this single parameter, allowing us to make parameter-free predictions. We obtain the electronic specific heat and find an excellent agreement with experiment [11]. We compute the spin-resolved DOS having a double-peak structure with each peak corresponding to a single spin channel. We find that the splitting is ~ 0.2 meV—within the reach of present experimental technology.

The triplet pairing in the INT state relies heavily on the interband pairing, which enables an isotropic gap function and equal-spin pairing breaking TRS [11]. The Cooper pair wave function is symmetric in the crystal momentum and spin channels but it is antisymmetric with respect to the orbital degree of freedom. Recent studies [11,31–42] in several materials, including the iron-based superconductors, half-Heusler compounds, UPt₃ and Sr₂RuO₄, have also pointed out the importance of internal degrees of freedom of electrons (coming from, e.g., sublattice or multiple orbitals) in determining the pairing symmetries of superconducting ground states.

A convenient toy model of low-energy excitations in the INT state proposed in Ref. [11] is provided by the following Bogoliubov–de Gennes (BdG) Hamiltonian:

$$\mathcal{H} = \begin{pmatrix} \mathcal{H}_0(\mathbf{k}) & \hat{\Delta} \\ \hat{\Delta}^\dagger & -\mathcal{H}_0(\mathbf{k}) \end{pmatrix}. \quad (1)$$

Here \mathbf{k} is the crystal momentum of the excitation,

$$\mathcal{H}_0(\mathbf{k}) = \mathbb{1}_2 \otimes \begin{pmatrix} \epsilon_0(\mathbf{k}) - \mu - s & \delta \\ \delta & \epsilon_0(\mathbf{k}) - \mu + s \end{pmatrix} \quad (2)$$

is the normal-state, single-electron Hamiltonian with the chemical potential μ , and

$$\hat{\Delta} = i(\mathbf{d} \cdot \boldsymbol{\sigma})\sigma_y \otimes i\tau_y \quad (3)$$

represents the pairing potential. In the tensor products, the first sector represents the spin channels $\sigma = \uparrow, \downarrow$ while the second represents the two orbital channels. For the purpose of initial discussion, we have assumed a very simple band structure with two bands labeled by $m = +$ and $-$, one emerging from each orbital, that are related by a rigid energy shift $2s$ and with a \mathbf{k} -independent hybridization factor δ . The pairing matrix describes \mathbf{k} -independent triplet pairing but is antisymmetric in the orbital channel in order to ensure the fermionic antisymmetry of the Cooper pair wave function [11,31]. Here, $\boldsymbol{\sigma}$ and $\boldsymbol{\tau}$ are the vectors of Pauli matrices in the spin and orbital sectors, respectively. Writing the triplet \mathbf{d} vector in the form $\mathbf{d} = \Delta_0 \boldsymbol{\eta}$, where $|\boldsymbol{\eta}|^2 = 1$ and Δ_0 is a pairing amplitude, the nonunitarity of the triplet state is characterized by a nonzero real vector $\mathbf{q} = i(\boldsymbol{\eta} \times \boldsymbol{\eta}^*)$ which in general has $|\mathbf{q}| \leq |\boldsymbol{\eta}|^2 = 1$.

Diagonalizing \mathcal{H} yields the quasiparticle spectrum $E_{\mathbf{k}}$ shown, for a particular choice of parameters, in Fig. 1(a). The plot is representative of cases where $s, \delta \ll \Delta_0$. This is the physically relevant regime for the toy model as in a mean-field picture the pairing amplitude (Δ_0) has to be able to overcome

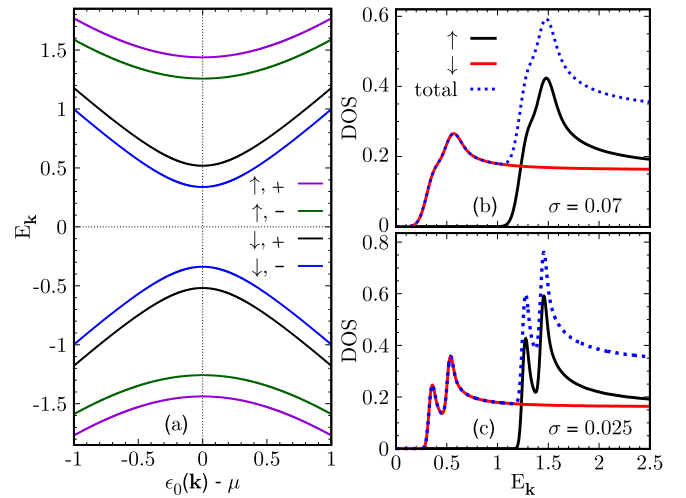


FIG. 1. Properties of quasiparticles in the INT state with $s = 0.05$, $\delta = 0.075$, $|\Delta_0| = 1$, and $|\mathbf{q}| = \sqrt{2/3}$ in arbitrary units. (a) Quasiparticle spectrum for the $+$ and $-$ bands for \uparrow and \downarrow spins. (b) and (c) show the corresponding DOS calculated from this spectrum using the same parameters. The DOS features have been artificially broadened by convolution with a Gaussian of width $\sigma = 0.07$ in (b) and $\sigma = 0.025$ in (c).

the band splitting $\sim \delta, s$. This unrealistic requirement is relaxed when the band splitting is allowed to be k dependent, as in the more detailed model discussed below. As indicated in the plot, each excitation has well-defined band and spin indices. The Bogoliubov bands are paired up, with each member of the pair sharing the spin index but differing in the band index. The corresponding DOS is displayed in Figs. 1(b) and 1(c). Here we have introduced two different levels of broadening to simulate different experimental resolutions in the two figures. The DOS is fully gapped, with four pairs of coherence peaks that are grouped in two doublets, depending on the level of broadening. Crucially, the *spin-resolved* DOS shows only one of the two doublets in each spin channel. This qualitative feature distinguishes this double-peak structure from that which would be obtained, for example, in a multi-band superconductor. The observation of such a spin-resolved feature would provide definitive proof of the INT state.

An analytical formula for $E_{\mathbf{k}}$ can be easily obtained in the limits $s \rightarrow 0$ or $\delta \rightarrow 0$. In either case, the result is

$$E_{\mathbf{k}} = \pm \left[\pm a + \sqrt{\{\epsilon_0(\mathbf{k}) - \mu\}^2 + |\Delta_0|^2(1 \pm |\mathbf{q}|)} \right], \quad (4)$$

where $a = \delta$ or s , respectively. Note that both δ and s play similar roles. This shows that our toy model does not rely on the two bands being orthogonal. The above formula can be used to estimate the ratio between the gaps in the energy spectrum for spin-up ($\mathcal{E}_{\uparrow\uparrow}$) and spin-down ($\mathcal{E}_{\downarrow\downarrow}$) quasiparticles. In the limit $a \ll \Delta_0$, it is

$$\frac{\mathcal{E}_{\uparrow\uparrow}}{\mathcal{E}_{\downarrow\downarrow}} = \frac{\sqrt{1+|\mathbf{q}|}}{\sqrt{1-|\mathbf{q}|}} = 1 - |\mathbf{q}| + O(|\mathbf{q}|^2). \quad (5)$$

The above toy model assumes that an isotropic, equal-spin pairing potential can lower the free energy in spite of the need for it to breach the energy gap between the bands. We explicitly show this by considering the toy many-body

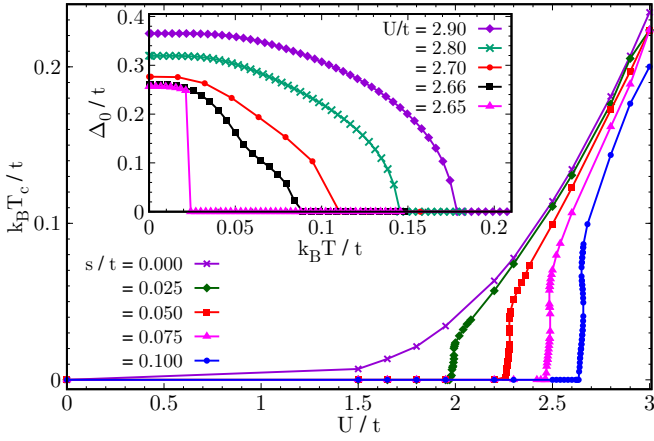


FIG. 2. Superconducting phase diagram of the toy model in Eq. (6). T_c is the critical temperature where interorbital, equal-spin pairing sets in. Each curve shows the dependence of T_c on the interaction strength U for a different value of the band splitting $2s$, as indicated. The inset shows the temperature dependence of the pairing amplitude Δ_0 for the largest splitting $s/t = 0.1$ and a few values of U just above the critical value U_c at which T_c becomes finite.

Hamiltonian

$$\hat{H} = \sum_{\mathbf{k}} \hat{\Psi}_{\mathbf{k}}^\dagger \mathcal{H}_0(\mathbf{k}) \hat{\Psi}_{\mathbf{k}} + \hat{H}_I. \quad (6)$$

Here $\Psi_{\mathbf{k}} = (\hat{c}_{\mathbf{k},+,\uparrow}, \hat{c}_{\mathbf{k},+,\downarrow}, \hat{c}_{\mathbf{k},-,\uparrow}, \hat{c}_{\mathbf{k},-,\downarrow})$, where $\hat{c}_{\mathbf{k},m,\sigma}$ creates an electron in the m th band with crystal momentum \mathbf{k} and spin σ . The single-electron Hamiltonian $\mathcal{H}_0(\mathbf{k})$ is given in Eq. (2) where for simplicity we take $\delta = 0$ and $\epsilon_0(\mathbf{k}) = -2t[\cos(k_x) + \cos(k_y)]$. We consider an on-site, interorbital, equal-spin pairing interaction proposed in Ref. [11], which can be written [43] as

$$\hat{H}_I = -U \sum_{\mathbf{k}, \mathbf{k}', \sigma} c_{\mathbf{k},+,\sigma}^\dagger c_{-\mathbf{k},-,\sigma}^\dagger c_{-\mathbf{k}',-,\sigma} c_{\mathbf{k}',+,\sigma} \quad (7)$$

with $U > 0$ being the effective attraction strength. A standard mean-field treatment of this model [44] yields the phase diagram shown in Fig. 2. In the limit $s \rightarrow 0$, the theory is formally equivalent to two copies of a BCS theory, but with the band index m playing the role of the spin index (one copy corresponding to each value of the real spin). For finite s , a critical interaction strength U_c is necessary for the critical temperature T_c to be finite, but for $U \gg U_c$ the results are very similar to the case $s \rightarrow 0$. This is confirmed by the inset, showing the temperature dependence of the pairing amplitude Δ_0 . While the superconducting transition can be of first order and even reentrant (not shown; see Ref. [44]) for a very narrow window $U \gtrsim U_c$, and displays some shoulders for slightly larger U , BCS-like behavior is recovered for $U \gg U_c$.

The above simple calculation shows that an equal-spin pairing potential can, in principle, breach a band gap to lead to a fully gapped triplet pairing state. On the other hand, our simple mean-field theory yields $\boldsymbol{\eta} = (0, 1, 0)$, i.e., a unitary triplet pairing state with $\mathbf{q} = 0$. A more realistic theory must treat the pairing and exchange fields on equal footing. Symmetry arguments [10] show that any triplet instability leads to a subdominant magnetization, which lowers the free energy of

the nonunitary state with $|\mathbf{q}| \neq 0$ [10,45]. We now therefore build a more sophisticated, realistic description which not only incorporates an accurate description of the exchange field, but also a realistic prediction of the normal-state electronic structure of LaNiGa₂, making quantitative predictions of superconducting properties possible.

Density-functional theory (DFT) in the local-density approximation (LDA) shows that LaNiGa₂ is a multiband superconductor with several bands crossing the Fermi level giving rise to multiple Fermi surface sheets [27]. None of the bands can be obtained from one another through a simple rigid shift as in our toy model. There are, however, several regions within the Brillouin zone where the pairs of Fermi surface sheets are parallel and very close to each other, that is, nearly degenerate [44]. Moreover, the five bands have mixed Ni 3*d*, La 5*d*, and Ga 4*p* characters. As a result, the Fermi surfaces have strong orbital degeneracy. To capture these details, we adopt a semiphenomenological strategy [46]. We consider the relativistic version of the BdG Hamiltonian in Eq. (1) together with the realistic LDA band structure and a phenomenological pairing interaction of the type given by Eq. (7). This leads to the Kohn-Sham-Dirac-BdG Hamiltonian [47]

$$\mathcal{H}_{\text{DBdG}} = \begin{bmatrix} H_D & \hat{\Delta}(\mathbf{r}) \\ \hat{\Delta}^\dagger(\mathbf{r}) & -H_D^* \end{bmatrix}, \quad (8)$$

where H_D is the effective normal state Dirac Hamiltonian given by

$$H_D = cp\hat{\alpha}_1 + (\hat{\alpha}_2 - \mathbb{1}_4)c^2/2 + [V_{\text{eff}}(\mathbf{r}) - E_F]\mathbb{1}_4 + \mathbf{B}_{\text{eff}}(\mathbf{r})\hat{\alpha}_3. \quad (9)$$

Here, $\hat{\alpha}_1 = \hat{\sigma}_x \otimes \hat{\sigma}$, $\hat{\alpha}_2 = \hat{\sigma}_z \otimes \mathbb{1}_2$, and $\hat{\alpha}_3 = \mathbb{1}_2 \otimes \hat{\sigma}$ with $\hat{\sigma}$ being the Pauli matrices and $\mathbb{1}_n$ being the identity matrix of order n . $V_{\text{eff}}(\mathbf{r})$ and $\mathbf{B}_{\text{eff}}(\mathbf{r})$ are the effective electrostatic potential and the effective exchange field, respectively. $\hat{\Delta}(\mathbf{r})$ is the 4×4 pairing potential matrix due to the four-component Dirac spinors. Requiring self-consistency in the electrostatic potential, exchange field, and pairing potential, the solution is provided by our recently developed method [47] which generalizes the Korringa-Kohn-Rostoker (KKR) formalism. Within the KKR formalism intraorbital and interorbital pairings could be described both in the singlet and triplet channel by transforming the (L, σ) representation of the pairing potential into a relativistic basis set, where L refers to the real spherical harmonics assuming that the z direction is perpendicular to the layered structure of LaNiGa₂. The technical details are given in Ref. [44].

It is important to note that the ground state does not show ferromagnetism in the normal state, although there is a significant contribution from the Ni 3*d* states at the Fermi level [27]. Since it is known that Hund's rule coupling plays an important role on the Ni atoms [48,49], and on the other hand Hund's coupling can also produce local pairing [50], it is physically reasonable to assume an interorbital equal-spin pairing involving two orbitals on the same Ni atom. We describe this by a two-body on-site attractive interaction $U_{L,L'}$ between electrons with equal spins in only two of these orbitals ($L \neq L'$) with the pairing potential satisfying the self-consistency equation: $\Delta_{L\sigma,L'\sigma}(\mathbf{r}) = U_{L,L'}\chi_{L\sigma,L'\sigma}(\mathbf{r})$ where $\chi_{L\sigma,L'\sigma}(\mathbf{r})$ is the corresponding pairing amplitude. Since all

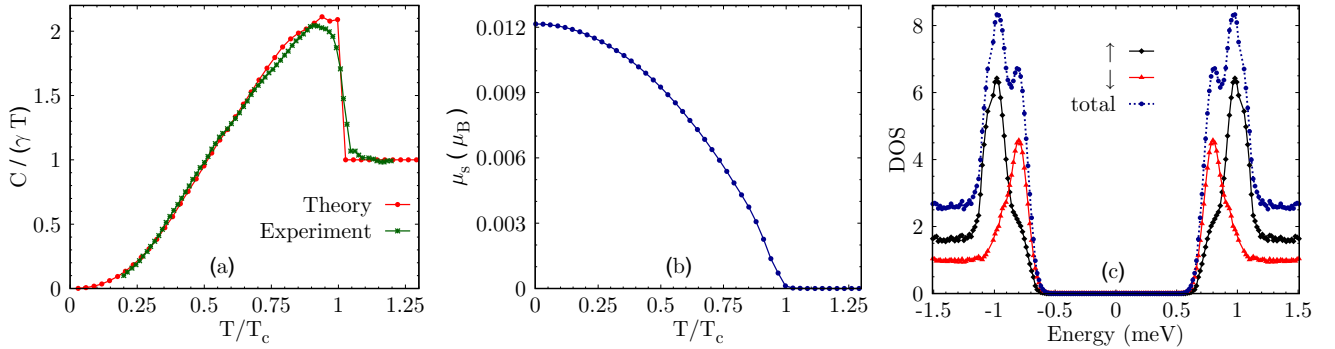


FIG. 3. Properties of the superconducting ground state corresponding to a phenomenological interorbital equal-spin pairing interaction between the (d_{z^2} - d_{xy}) orbitals in the $3d$ sector of the Ni atom in LaNiGa_2 . (a) Variation of the specific heat with temperature (γ is the Sommerfeld coefficient). We note an excellent agreement between the theoretical result and the experimental data taken from Ref. [11]. (b) Variation of the spontaneous magnetic moment (μ_s) as a function of temperature. A clear increase in the magnetic moment below T_c is an indication of the imbalance between two spin species due to migration of Cooper pairs. (c) Spin-resolved density of states (arbitrary units) of the Bogoliubov quasiparticles as a function of energy. We note that the two coherence peaks correspond to up and down species of Cooper pairs leading to two gaps in the quasiparticle spectrum.

of the Ni d orbitals contribute to the density of states at the Fermi level, there are ten possible pairing models within this approach. Only one of the ten possible combinations, namely, pairing between d_{z^2} and d_{xy} , yields a fully gapped quasiparticle spectrum (all the other possibilities have nodes on at least one of the Fermi surface sheets; see Ref. [44]). The strength $U_{d_{z^2}, d_{xy}}$ of the interaction between these two orbitals is the *only* adjustable parameter in our theory, to be fixed by requiring T_c to be the same as in experiments [11]. Then we can make parameter-free predictions of observable properties of the system. The requirement that T_c is the same as in experiments leads to $U_{d_{z^2}, d_{xy}} = 0.65$ eV, which is comparable to the values of Hund's coupling found for Ni atoms [49]. This result should motivate high-pressure measurements and dynamical mean-field theory studies to further explore the role of electronic correlations involving Hund's coupling. We stress that the present attractive interaction is described by a phenomenological parameter and therefore our calculation cannot directly address the question of its origin.

Having fixed our single parameter, we can now make parameter-free predictions. We first compute the specific heat of LaNiGa_2 as a function of temperature by evaluating the temperature dependence of the quasiparticle DOS self-consistently [46,51]. It is shown in Fig. 3(a) as compared to the corresponding experimental data from Ref. [11]. The agreement is excellent, suggesting that the observed two-gap behavior of this curve is consistent with our equal-spin, interorbital pairing model.

The solution of the self-consistency equations reveals a charge imbalance between $\uparrow\uparrow$ (67%) and $\downarrow\downarrow$ (33%) triplet components on the Ni atom. The migration of Cooper pairs from the minority $\downarrow\downarrow$ state to the majority $\uparrow\uparrow$ state is expected to generate a finite magnetization. Since our pairing interaction $U_{d_{z^2}, d_{xy}}$ is spin independent (hence preserves TRS), we have found a spontaneous TRS breaking in the INT state, which is a perfect analog of a ferromagnetic transition in a normal-state DFT calculation. The pairing-induced spontaneous magnetization (μ_s) is shown in Fig. 3(b). The magnetic moment is expected to vary linearly very close to

T_c [10]; however, this behavior is hard to resolve here due to demanding numerical accuracy near T_c . We can estimate the size of the internal magnetic field at zero temperature using μ_s^0 , the value of μ_s at $T = 0$, as $B_{\text{int}} \approx \frac{\mu_0 \mu_s^0}{4\pi abc} \approx 0.3$ G which is of similar order as seen in the zero-field μSR measurements [10].

Finally, we compute the spin-resolved quasiparticle DOS of LaNiGa_2 as shown in Fig. 3(c). Its similarity with Fig. 1(b) is striking, confirming that our DFT-KKR calculation for this material describes the same physics. The two distinct superconducting gaps are clearly visible, and the spin-resolved curves show that they correspond to different spin species. The double-peak structure of the DOS is our main prediction. We note that the splitting between the two peaks is of the order of 0.2 meV—within the resolution of current scanning tunneling microscopy [52], photoemission [53], and tunneling experiments [54]. The crucial feature is that, unlike the case of a multiband superconductor [55], the two peaks correspond to *distinct spin channels*. Verifying this experimentally would thus require spin resolution [56].

Interestingly, in Ref. [11] the specific heat measurement was fitted by a phenomenological two-band model leading to the gap values $\Delta_1 = 1.08k_B T_c$ and $\Delta_2 = 2.06k_B T_c$, while we find that the difference between the gaps is only around 20%. Clearly, the difference between the two procedures comes from the fact that our first-principles-based calculation included all of the five bands crossing the level. However, our main point is that the DOS is spin polarized around the Fermi level, and the superconducting gaps correspond to different spin channels, not different bands.

We note that it is important to consider the effect of magnetic and nonmagnetic impurities on the INT state. Although this is outside the scope of the present Rapid Communication, due to the two full gaps we expect the INT state to be protected from nonmagnetic impurity scattering and a version of the Anderson's theorem [57] to hold.

We showed that an unconventional superconductor in the INT state has at least two gaps, one for each spin flavor, irrespective of the number of Fermi surfaces. Instead of the

traditional route of ignoring the microscopic complexity of Fermi surfaces, we consider the fully relativistic electronic band structure of LaNiGa₂. We perform fully self-consistent computations of its observables by taking a phenomenological pairing model on the Ni atom in the INT state. The pairing model has a single adjustable parameter fixed by the experimental value of T_c of the material. There is an excellent agreement between the computed and measured specific heat of the system. We showed that due to the migration of Cooper pairs a subdominant order parameter, magnetization, arises spontaneously, breaking TRS consistent with the zero-field μ SR experiment. The salient feature of our calculations is a double-peak structure in the quasiparticle DOS arising from the two spin channels. We have predicted quantitatively the splitting between the two peaks and showed that it is well within the reach of present experimental technology and resolution. We have thus achieved a desired milestone: a

quantitative theory of exotic pairing in an unconventional superconductor, namely, LaNiGa₂, predicting a smoking-gun signature of its unconventional pairing state.

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