Using Insurance to Manage Reliability in the Distributed Electricity Sector: Insights from an Agent-Based Model

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Abstract

High penetration of distributed technologies would call for a different way to manage electricity reliability for semi-independent households. One option could be to allow customers to withdraw power from the grid when their home system fails. This behavior, however, could constitute an existential threat for utilities: if consumers use the network less, and continue to pay according to their usage, the utility might be unable to recover its costs. This paper investigates whether the creation of a reliability insurance market would help to deal with these concerns. We propose a business model where utilities offer insurance to semi-independent, yet risk averse households, against the prospect of a blackout, when a pay as you go system is no longer available. With the use of an Agent Based Model, we test if contracts from this market can converge into a theoretical optimal contract where bounded perception of risks and losses impact the price of insurance and potential revenues of utilities. We find that such a market could exist as consumers efficiently transfer all or a portion of their risk to the utility, based on their willingness to pay and risk profiles, which allows them to avoid blackouts at the margin.

Keywords: Distributed energy resources, new business models, utilities of the future, agent based model, utility death spiral
1 Introduction

High penetration of new distributed energy resource (DER) technologies would call for a different way to manage reliability in the power sector. In central electricity systems, planners invest in capacity higher than the peak load to have reserve margins that can deliver almost perfect coverage, as they can spread this cost among all customers. This approach was more feasible when technology options were limited, and the underlying assumption was that blackouts have an infinite negative value. In a distributed dominated power system, however, it seems unnecessarily expensive and unfair, as all customers pay an equal amount regardless of their preferences for risk. To deal with security of supply in this context, this paper tests the creation of a risk market that enables reliability preferences to be internalized through the use of insurance.

New distributed energy technologies - by this we refer to the combination of domestic photovoltaic (PV) panels plus batteries plus information devices - allow households to generate, trade, reduce, and shift their electricity consumption, bypassing the traditional utilities. The most extreme case of distributed energy resource (DER) adoption would be self-sufficiency, i.e., the consumer produces all the power their home needs and also stores enough for later use. However, the issue of security of supply for self-sufficient households would remain. There is an inherent risk in all intermittent technologies that they would temporarily fail due to adverse weather or technical problems.

Being self-sufficient would allow households to disconnect from the grid and avoid all external charges (Green and Staffell 2017). However, most of those households will still need to use the networks to draw power from the grid if their system fails. A pay as you go scheme would not reflect the opportunity cost of idle infrastructure and could lead to a utility death spiral if the way this back up is priced stays the same (Felder and Rasika 2014; Muaafa et al. 2017). Traditionally, network costs are bundled into the price of electricity. This pricing may be inadequate if self-sufficient households defect from the grid on mass, and in the presence of technologies where customers can best reflect their preferences for guaranteed services.

Insurance exists to reduce or eliminate the cost to an individual who faces an adverse event, like the loss of power. There are many different types of insurance policies available, and virtually any individual or business can find an insurance company willing to insure them for a price. We propose the utility can offer power of last resort to energy self-sufficient households in case they...
suffer a blackout. Specifically, the value proposition is that utilities’ idle capacity resulting from the fast deployment of DERs in the domestic sector can be repackaged and repriced as insurance. This service is currently embedded in electricity provision and is taken for granted. By selling insurance, utilities would guarantee a stable revenue stream by charging a constant fee, instead of charging very high prices in periods of abrupt demand surges followed by low fees for periods of negligible demand. This proposal may also appeal to customers as an insurance-based model can reflect their attitudes towards the risk of blackout and can, therefore, be an efficient and equitable way to pay for network access.

We investigate the extent to which contracts for insurance can converge into a theoretical optimal contract. This contract is defined on the basis of a household-specific energy budget, a risk aversion attitude, an expected loss and with the supplier possessing full and complete information about the households. The static version of the model is then generalized into a dynamic framework where households are allowed to renew or switch contracts over time, and firms do not possess full information about households and hence cannot offer an optimal contract. Instead, they offer a menu of contracts from which households choose the one they prefer and can afford. Firms are allowed to adapt their offerings periodically based on profitability considerations.

The dynamic outcomes of this generalized setup are examined through an agent-based model, particularly how the perception of risks and losses impact the price of insurance and potential revenues of utilities. It also examines the stability of such an insurance market and household-level outcomes. We also explore how this market would react to policy initiatives that affect its underlying parameters. This paper addresses a latent problem. While most of the literature on disrupting DERs looks at the gradual penetration of new technologies, we take a different stance and assume that this penetration has already occurred. So, instead of analyzing the incumbent utilities’ reaction to the erosion of their market shares, we start from the end and figure out the steps back.

We show that this insurance market helps to internalize risk and reduce blackouts significantly. However, there may be households who are not able to cover their full energy needs due to either budgetary considerations or the extreme nature of their risk profiles. Our simulations show that of those households who would otherwise experience a complete loss of power in the case of a disruption to their DER, on average between 1 to 15 percent can
fully cover their excess energy needs through insurance. Between 50 to 70 percent of those households who would otherwise experience a complete loss of power are budget constrained and would still be able to partially cover their excess energy needs.

Through this paper’s proposed approach, the security of electricity provision would move away from an engineering approach, based on system-wide costs, towards an economic approach, where an insurance mechanism along with an array of alternative contracts can balance system-wide supply and demand. This paper formalizes in an Agent Based Model the conceptual reliability insurance business model put forward in Fuentes et al. (2019) for a distributed electricity sector. Prior to that the only proposal for an insurance market for electricity has been from the head of the United Kingdom’s energy regulator, the Office of Gas and Electricity Markets, or OFGEM, in an article published in 2016 in The Telegraph titled “Households could be charged annual ‘insurance premium’ for access to electricity grid” (Gosden, 2016). Billimoria and Poudineh (2018) have also put forward the idea of an insurance to deal with reliability issues as an alternative to a centralized capacity market mechanism that responds to shortfalls in an energy only market. This market design is a hybrid solution that alignes incentives for centralized decision making while allowing revealed consumer preferences to guide new capacity deployment. Other business models that unbundle electricity services have started to emerge. For example, the Rocky Mountain Institute proposed a business model for lighting — measured in lumens — where the provider delivers a specified service (Calhoun et al., 2017). Other institutes such as Energy Systems Catapult have applied broadly similar thinking to propose the creation of a domestic heating and cooling service (Watkins, 2017).

The paper is organized as follows. Section 2 discusses the insurance business model and presents its theoretical foundations. Section 3 presents the set up of an agent based model that formalizes the business model of section 2. We discuss the results of our simulations in section 4. Section 5 discusses our results and presents the paper’s conclusions.
Figure 1. A customer with a DER pays a variable cost for reliability when a customer without DERs pays a fixed cost. The difference between them is their perceived savings.

2 Model
2.1 Background
Designing new markets for which limited experience exists is a challenging task. A multitude of unforeseen interactions may occur between consumers and retailers. Designing a new market for the electricity sector is an even greater challenge. The sector is characterized by difficult real world factors such as asymmetric information, imperfect competition, strategic interactions, collective learning, multiple equilibria and path-dependent investments (Weidlich and Veit, 2008). Some of these problems are too idiosyncratic for traditional economic modeling techniques. Agent based models (ABMs) are well suited to modeling complex systems characterized by irrational behavior, heterogeneity and agents that learn from mistakes. The ABM approach follows a flexible, bottom-up methodology where the behaviours of actors or agents can be modeled explicitly, without having to resort to any aggregation or specification of a representative agent. Hence household- and provider-specific behavior can be flexibly and robustly built into the model, with few restrictive assumptions.

ABMs have been used in the electricity sector in at least three areas (Ringler et al., 2016). The first is in the study of wholesale markets, concentrated on large generation companies that behave with bounded rationality and have complete information. In this section, we include the seminal work of Bower and Bunn (Bower and Bunn 2000, 2001; Bower et al., 2001), and other larger open source models, such as the Aalborg University’s Electricity Market Complex Adaptive System
(EMCAS), the research group at Iowa State University’s (Koesrindartoto et al., 2005), and the OPIMATE Model (Maenhoudt and Deconinck, 2010; Schröder, 2012). These models help to investigate market restructuring, the market integration of renewable sources, and the impacts of congested transmission.

ABMs have also been used to understand electricity consumer behavior. The focus of these investigations has been on modeling electricity consumption and generation at very low levels of aggregation. They have also investigated indirect effects, such as the diffusion of new technologies, and the interaction between ‘prosumers’ and markets (Hamalainen et al., 2000; Müller et al., 2007; Zhang and Nuttall, 2011; Kowalska-Pyzalska et al., 2014).

More recently, work has been done on decentralized structures and market integration. This literature has focused on the changing paradigms in electricity systems using ABMs, specifically concerning smart grids and new markets. Research of this type attempts to answer questions related to the integration of demand responses and distributed generation in local or centralized markets (Gnansounou et al., 2007; Muuafa et al., 2017; Stephenson et al., 2010; Gottwald et al., 2011). The model presented in this paper bridges the gap between the work on consumer behavior and decentralized structures.

The following assumptions for our model provide the context for our analysis (see Fuentes, Blazquez and Adjali [2018] for the justification of these shortcuts):

- Households wish to have power provision 100 percent of the time, at the lowest cost to them, while maximizing their level of electricity independence.
- Overnight, all households install large amounts of PV and batteries, which allows them to be power independent.
- Utilities are entitled to cut households off from their network if they no longer use their service on a regular basis.
- There is an inherent risk associated with all intermittent forms of generation.
- Households cannot buy power from other households. This simplification allows us to isolate pure risk management strategies and ignore potential externalities arising through inter-household networks.
• Households have pre-allocated budgets for purchasing additional energy or insurance in the event a shortfall occurs from their domestic source.
• For further simplification, we do not analyze commercial and industrial users.

The theoretical foundations of our analysis is provided in two stages. A static version of the microfoundations first presented which define the market equilibrium under simplified rational actor assumptions in a one period framework. The assumptions of rationality, from both the perspectives of households and firms are then relaxed in a more generalized dynamic model with bounded rationality and reinforcement learning, to provide a more complete and relatively more realistic description of the insurance market. While the single period static model is solved analytically, the more complex dynamic model is explored using agent based simulations. We are now ready to provide the descriptions of the static and dynamic versions of the market models considered here.

2.2 Static Model
2.2.1 The household
We first examine a representative household’s choice of insurance coverage from an energy supplier. We consider a simple one-period model of a representative electricity market, with \( N \) households and a single supplier \( S \). Each household \( n \in N \) has installed energy generation capacity which provides a fixed \( \bar{C}_n \) units of energy at any given period. A representative household’s energy demand \( C_n \) is assumed to be stochastic, such that \( C_n \leq \bar{C}_n \) with probability \( 1 - \pi \) and \( C_n > \bar{C}_n \) with probability \( \pi \).

Each household is characterized by a ‘dis-utility’ function \( U(L_n) \) where \( L_n \) is the energy loss or shortfall faced by a household \( n \), defined as:

\[
L_n = \begin{cases} 
0, & \text{if } C_n \leq \bar{C}_n \\
C_n - \bar{C}_n, & \text{otherwise}
\end{cases}
\]  

Households are considered to be risk-averse. We define the (dis-)utility of loss \( L_n \) for household \( n \) as a monotonically decreasing strictly concave function:

\[
U(L_n; \alpha_n) = \bar{U} - e^{\alpha_n L_n}
\]

where, \( \bar{U} > 1 \) and \( \alpha_n > 0 \).
Note that the first and second derivatives of the utility function specified above are $U'(L_n) = -\alpha e^{\alpha L_n} < 0$ and $U''(L_n) = -\alpha^2 e^{\alpha L_n} < 0$, respectively. The above specification implies that the household specific coefficient of absolute risk aversion (CARA) in our model is given by:

$$\frac{U''(L_n)}{U'(L_n)} = \alpha_n$$  \hspace{1cm} (3)

Each household produces energy at full capacity at every period, but its energy demand may exceed installed capacity with probability $\pi$ as specified above. If the demand exceeds installed capacity, the household has the option of purchasing energy from the supplier at a contracted two-part tariff $(p, F)$, where $p$ is the per unit price of energy bought, and $F$ is the lump-sum ‘standing charge.’ Each household is endowed with a specific budget $B_n$ dedicated for additional energy needs (including insurance coverage), and hence faces a budget constraint:

$$p(L_n - L_n^*) \leq B - F$$  \hspace{1cm} (4)

where $(L_n - L_n^*)$ is the ‘coverage’ provided by the supplier to household $n$ in case of a shortfall in its domestic production. Consequently, $L_n^*$ is the level of shortfall or loss in energy that the household is willing to face, given its budget constraint and utility specification. In other words, $L_n^*$ is the household specific loss not covered by the insurance contract with the supplier. This specification allows the household to draw as much energy as it wants from the supplier, provided it pays the requisite price$^1$.

Unlike the standard microeconomic choice specification of ‘energy’ versus ‘all other goods,’ we adopt a more straightforward approach where the household has already decided to allocate a budget. This makes the model more tractable without any loss of generality, as the central question is on how insurance contracts should be structured rather than on deriving a household’s energy demand. Also, it is increasingly being recognized that energy demand exists not for its own sake, but as it acts as a medium to consume other goods and services (heating/cooling, lighting and so forth)$^2$. Thus, modeling energy (derived) demand needs to explicitly consider the trade-off between the consumption of goods and services using this energy against all others. However, using such a specification needlessly complicates the model, given that the demand for insurance

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$^1$ We relax this assumption with a coverage limit in the dynamic model, in the next section. The presence or absence of this additional constraint has no influence on main results in the static framework.

is itself a second order derived demand based on the demand for energy. Thus henceforth, household-specific budgets for insurance or additional energy needs are assumed to be exogenously fixed at $B$.

Given that households are symmetric, we drop the subscript $n$ from the analysis which follows.

For the sake of simplicity, assume that households are aware of the exact level of loss that they can incur in case installed capacity falls short of demand and there is no insurance coverage. This implies, *ex ante*, households have full knowledge of the level of loss that they might incur (say, $\bar{L} > 0$) and the probability of such an outcome ($\pi$), but not whether the outcome will actually take place. Note that this is qualitatively similar to the general situation where any positive level of loss can be incurred with a known continuous probability over the support $(-\bar{C}, \bar{L})$.

We are now ready to state the main results of this section pertaining to the equilibrium decisions of a representative household and the supplier.

**Lemma 1** A rational household characterized by risk aversion $\alpha$ and potential loss $\bar{L}$ will be willing to accept an insurance contract offering a cover of $\kappa$ only if

$$\kappa \geq \bar{L} - \frac{1}{\alpha} \log \left[ (1 - \pi) + \pi e^{\alpha \bar{L}} \right]$$

Proof: Let $L^c$ be the ‘certainty equivalent’ amount of loss for the household. Hence by definition,

$$U(L^c) = (1 - \pi)U(0) + \pi U(\bar{L})$$

or,

$$\bar{U} - e^{\alpha L^c} = (1 - \pi)(\bar{U} - 1) + \pi(\bar{U} - e^{\alpha \bar{L}})$$

Solving the above for $L^c$, we get

$$L^c = \frac{1}{\alpha} \log \left[ (1 - \pi) + \pi e^{\alpha \bar{L}} \right],$$

which is the level of ‘certain’ loss that makes a risk-averse household indifferent to either accepting or rejecting the random loss (see Figure 1).

If an insurance contract provides a cover $\kappa$, the household will either face a loss of 0 (with probability $1 - \pi$) or a loss of $\bar{L} - \kappa$ (with probability $\pi$). If $\bar{L} - \kappa > L^c$, then for a monotonic utility function $U(\bar{L} - \kappa) < U(L^c)$. In other words, the expected utility from the contract is less
than the expected utility of a household that does not accept the contract and takes on the full risk. Hence, for a rational household to accept an insurance contract, $\bar{L} - \kappa \leq L^c = \frac{1}{\alpha} \log\left(1 - \pi + \pi e^{\alpha T}\right)$. The proof follows.

Thus Lemma 1 introduces a lower bound on the loss that a household will be willing to accept in the case where the household has insurance cover. The next proposition defines the equilibrium level of cover that the household purchases.

**Proposition 1** Facing an insurance cost of $(p, F)$, where $B > F$, a rational utility maximizing household will opt for an equilibrium level of coverage $\kappa^*$, such that,

$$\kappa^* = \begin{cases} \frac{B - F}{p}, & \text{if } \bar{L} - \kappa^* \leq L^c \\ 0, & \text{otherwise} \end{cases}$$

Proof: The single period optimization problem faced by the household is the following:

$$\max_L (1 - \pi)U(0) + \pi U(L) \text{ s.t. } L \leq L^c \text{ and } p(\bar{L} - L) \leq B - F$$

Since $U(0) = \bar{U} - 1$, which is a constant, the problem reduces to maximizing $\pi U(L)$ wrt $L$ subject to the incentive and budget constraints, respectively. Now as $U'(L) < 0$ for all $L \geq 0$, and as the budget $B$ is specific to energy consumption only, we must have $(\bar{L} - \kappa^*(p, F)) = \frac{B - F}{p}$, as long as the incentive constraint $L^*(p, F) \leq L^c$ holds (Lemma 1). Replacing $\kappa^* = \bar{L} - L^*(p, F)$ above, proof of the first part follows. Now suppose the incentive constraint does not hold, that is, $\bar{L} - \kappa^* > L^c$. In this situation, the household would be better off facing the risk without any insurance cover (Lemma 1), implying $\kappa^* = 0$. The proof follows.

Proposition 1 implies that the household uses up the entire allocated budget to purchase the optimum level of cover. However, as a corollary to Proposition 1, this implies that the price of insurance $(p, F)$ should not be too high, causing $\kappa^*$ to be so low that $\bar{L} - \kappa^* > L^c$, in which case the household would prefer not to buy the insurance contract.

2.2.2 The supplier

The results above explore the choices made by households with respect to the level of coverage they buy from the supplier. The households themselves are characterized by the energy budget
(B), risk aversion (α), the probability of facing a loss (π), and the shortfall in energy supply they can potentially face (L). In this section, we identify what the ‘ideal’ contract is for a household, from the perspective of the supplier.

Suppose that the supplier faces a constant marginal cost c and a fixed cost Φ of including a household within the grid and supplying it with energy. The following proposition characterises the optimum pricing strategy for the supplier for a specific household where the supplier possesses full and complete information about the household.

**Proposition 2** Suppose that the supplier possesses full and complete information about a household’s energy budget (B), risk aversion (α), the probability of facing a loss (π), and the potential shortfall in supply (L). In equilibrium, the supplier can maximize its profit from this household by offering it a contract \((p^*, F^*)\), where

\[
p^* = \frac{B - F^*}{L - L^c},
\]

\[
F^* = \begin{cases} 
\Phi, & \text{if } \Phi < B \\
0, & \text{otherwise}
\end{cases}
\]

\[
L^c = \frac{1}{\alpha} \log \left[ (1 - \pi) + \pi e^\alpha L \right].
\]

as long as, \(p^* > c\). A rational utility maximizing household will accept such a contract as it satisfies both the budget and incentive constraints.

Proof: For any given contract \((p, F)\) being offered by the supplier, the expected demand from a household for the supplier’s energy is:

\[
\frac{\pi (B - F)}{p}
\]

If the contract is accepted, the expected profit \(\Pi_s\) for the supplier from this household, given marginal cost \(c\) and fixed cost \(\Phi\), is:

\[
\Pi_s = (p - c) \pi \frac{(B - F)}{p} - \Phi + F
\]

The supplier’s optimization problem is to \(\max_{p,F} \Pi_s\). Now,
\[
\frac{\partial \Pi_u}{\partial p} = \frac{c\pi (B - F)}{p^2} > 0
\]

Hence, the supplier should raise its per unit price \( p \) as long as either the budget or the incentive constraint of the household becomes binding.

In equilibrium,

\[
L^*(p, F) \leq L^c \quad \text{(from Lemma 1)},
\]

and \((\bar{L} - L^*(p, F)) = \frac{B - F}{p}\) \( \text{(from Proposition 1)},\) where, \( L^c = \frac{1}{\alpha} \log[(1 - \pi) + \pi e^{\alpha L}] \).

Substituting \( L^* = \bar{L} - \frac{B - F}{p} \) from the second expression into the first, we have

\[
p \leq \frac{B - F}{\bar{L} - L^c}
\]

As \( \frac{\partial \Pi_u}{\partial p} > 0 \), the profit maximizing price given any \( F \) is,

\[
p^* = \frac{B - F}{\bar{L} - L^c}
\]

Given that \( \frac{\partial \Pi_u}{\partial F} = -\frac{p - c}{p} < 0 \) if \( p > c \), \( F \) can then be benchmarked to the fixed cost \( \phi \) of supplying energy to the household with budget \( B \). If the household has a sufficient budget to cover the fixed costs, set \( F^* = \phi \), otherwise set \( F^* = 0 \). In both cases, the equilibrium profit \( \Pi^* = B - \phi - c(\bar{L} - L^c) \), and hence the supplier is indifferent between a positive or a zero lump sum component.

This completes the proof.

Figure 2 illustrates the optimum price setting principle. The optimum unit price is higher for households that do not pay the lump sum (\( F^* = 0 \)), and lower for households that pay a positive lump sum (\( F^* = \phi \)).

Note that the above analysis assumes that the supplier has full knowledge of a household’s characteristics such as its budget, levels of risk aversion and the probability of loss. In the more realistic case where it does not and is only aware of the probability distribution of each of these.
characteristics in the market, the above result on optimum pricing strategy may be modified to reflect the expected values of these characteristics in the market. In such a case, the supplier cannot fully discriminate between households but may offer a single contract which only eligible households (for whom the constraints are satisfied) will choose. Alternatively, it can offer a menu of contracts, each with a different level of per unit price and lump sum, and households will select the contract which maximizes their utility. In both cases, it is possible that some households do not purchase any contract, thus choosing to stay ‘dark’ when there is a shortfall in their self-generated energy supply.

2.3 Dynamic Model
We assume that time extends from 0 to $T$, where $T$ is sufficiently large so that the supplier and the households are not able to factor it explicitly into their optimization. We also assume that households have complete information about the past and no information about the future. Their energy demand for period $t$ is uniquely determined in $t$ and is unconditional on any previous period’s usage (no seasonality or autocorrelation). The supplier also only provides energy coverage for a single period. All assumptions regarding household behaviour hold true in this model for any specific period $t \in T$. To start, we only consider rational households and suppliers with no learning or adaptation capabilities.

Given that the period-specific conditions for a household remain the same as in the static framework, and the insurance coverage provided by the utility is essentially for a single period (and cannot spill over into the future), the household’s rational equilibrium demand $\kappa^*(t)$ in period $t$ is identical to that characterised in Proposition 1.

$$\kappa^*_t = \begin{cases} \frac{B - F_t}{p_t}, & \text{if } L - \kappa^*_t \leq L^c \\ 0, & \text{otherwise} \end{cases}$$

The supplier’s problem is to maximize the discounted sum of period profits $\Pi_t(p_t, F_t)$ over $t \in T$, where $T \to \infty$. Given that there are no inter-temporal constraints or spill-overs in the model, the inter-temporal maximization is equivalent to the period maximization problem, implying that the supplier maximizes per period profit in the dynamic model as well. Hence, in this version of the dynamic model, the equilibrium $p^*_t$ and $F^*_t$ are identical to the static equilibrium values expressed in Proposition 2.
2.3.1 Adaptation and learning

We now introduce an alternative dynamic specification, where both the supplier and the households are allowed to learn from past behavior and outcomes and adapt their behaviour over time. This is specifically done in order to reduce the rationality burden on both, as is required by the economic model specified earlier. This allows households to make ‘mistakes’ in their choice of insurance contract (in terms of coverage purchased) and the ability of the utility to change the tariff charged in each contract offered based on demand. This makes the modeling less restrictive and provides us with a more flexible implementation of the agent-based model.

In this specification, neither the supplier nor the households are assumed to be rational, but alternative characterizations of behavior are benchmarked against the rational equilibrium outcome. We make the following adjustments to the model to incorporate learning behavior.

First, we introduce a coverage limit in the contract, which acts as an additional constraint for households in the model. This implies that an energy insurance contract is now of the form \((p, F, L)\), where \(p\) and \(F\) represent the per unit and lump sum prices respectively, as before. The additional \(L\) represents the maximum coverage allowed within the contract at the given prices.

Second, we allow for the possibility of multiple insurance contracts being made available by the supplier to the households. In this scenario, the supplier provides a menu of alternative \(K\) contracts \([\{(p^1_t, F^1, L^1), ..., (p^K_t, F^K, L^K)\}]\) from which a household has to select one.

Third, we introduce an adaptation rate parameter \(\tau\), which represents how quickly households and the supplier are allowed to change their demand and supply behaviours, respectively. At time \(t = 0\), the supplier offers the contracts \([(p^1_0, F^1, L^1), ..., (p^K_0, F^K, L^K)\}], from which each household selects one. We assume that the supplier updates the contracts every \(\tau\) periods, and the households, once they have chosen a contract, are contractually bound to it for \(\tau\) periods as well. After every \(\tau\) periods, the supplier has the option to modify its offerings and the households have the option to update their choices. These sets of contracts and choices once again remain fixed for the next \(\tau\) periods. Thus the parameter \(\tau\) indicates the rate at which actors in the market are able to update
their decisions, with a smaller value indicating a faster update\(^3\). We now define the updated rules of this framework that households and the supplier follow.

The households choose from the menu probabilistically. Hence, household \(n\) is characterised by a probability distribution \((\rho^1(t), \ldots, \rho^K(t))_n\) in period \(t\), such that in every \(\tau\) periods it selects contract \(k \in \{1, \ldots, K\}\) with probability \(\rho^k_t\). While a household chooses a contract once every \(\tau\) periods, the probability distribution is updated in every period \(t\). Hence, at the time of choosing the next contract, the household faces a potentially new probability distribution over the choices representing the cumulative effect of the last \(\tau\) periods. The dynamic update of a household’s probability distribution over the available menu of contracts at period \(t\) is assumed to follow a simple reinforcement learning algorithm based on which of the three constraints had been binding in period \(t - 1\). These are summarized as follows:

\((\text{Rule 1H})\) If the budget constraint was binding in period \(t\), in period \(t + 1\) reduce the probability weights on contracts with relatively higher per unit prices and increase the probability weights on contracts with relatively lower per unit prices.

\((\text{Rule 2H})\) If the incentive constraint was binding in period \(t\), in period \(t + 1\) reduce the probability weights on contracts with relatively lower coverage limits and increase probability weights on contracts with relatively higher coverage limits.

\((\text{Rule 3H})\) If the coverage limit constraint was binding in period \(t\), in period \(t + 1\) reduce the probability weights on contracts with relatively lower coverage limits and increase probability weights on contracts with the highest coverage limits.

Note that while Rules 2 and 3 are qualitatively similar, applicable under the general condition of insufficient coverage in the previously chosen contracts, Rule 3 encourages a faster movement than Rule 2 towards contracts with the highest coverage limits. Exactly how Rules 1-3 are operationalized depends on the number of contracts \(K\), and will be discussed in the next subsection.

The supplier is allowed to adjust the \textit{unit prices offered} in the contracts every \(\tau\) periods, reflecting changing demand conditions. Let \(D^*_k(t)\) be the total number of households subscribing to contract

\(^3\) As an example, one can consider each period to be a month and if \(\tau = 12\), each contract lasts for 12 months. Households choose a new contract annually. Note that the annual nature of contracts is just an example, and the model update can happen faster or slower as desired.
\(k\) in period \(t\), and let \(0 < \theta < 1\) be a threshold parameter defined exogenously. The update rule for any contract \(k \in \{1, ..., K\}\) can then be stated as:

(Rule 1S) Every \(\tau\) periods, change unit price of contract \(k\) from \(p^k\) to \(p^k(1 + \Delta p^k)\), where \(\Delta p^k\) is defined as:

\[
\Delta p^k = \begin{cases} 
\frac{D_k^*(t) - D_k^*(t-\tau)}{D_k^*(t-\tau)} & \text{if, } \left| \frac{D_k^*(t) - D_k^*(t-\tau)}{D_k^*(t-\tau)} \right| > \theta, \\
0, & \text{otherwise}
\end{cases}
\]

The above rule makes price adjustments in the dynamic model demand driven, where existing per unit price is increased (or decreased) in the same proportion as the change in cumulative demand over \(\tau\) periods, provided the change is large enough, as determined by the parameter \(\theta\). Note that a higher \(\theta\) implies a less frequent price update than a lower \(\theta\), but each update is by a greater amount. On the other hand, a smaller \(\theta\) implies more frequent updates than a higher \(\theta\) but by a smaller proportion. This rule internalises the update amount and makes it completely demand driven.

3 The agent-based framework

We simulate the dynamic model using an agent based model, with independent agents representing households and the single supplier. This model would help us answer the extent to which second-best contracts can be designed to be closer to optimal designs with two-part tariffs where customers can self-select themselves. The model will solve for final unit prices under different contract settings, cumulative revenues for the supplier, and the extent to which this product allow reliability to be internalized by calculating the percentage of houses that decided not left uninsured.

Each household agent has the following parameters: \(\alpha, \bar{L}, B, \pi\), randomly drawn from uniform distributions: \(\alpha \in (0, \bar{\alpha}), \bar{L} \in (0, \bar{L}), B \in (0, \bar{B}), \pi \in (0, \bar{\pi})\). The upper limits of the supports are parameters in the simulations, details of which are provided in Table 1. The supplier provides three alternative contracts for households to select from, i.e., \(K = 3\). The households choose a contract and the menu of contracts is updated every 12 steps within the simulation (\(\tau = 12\)). A household at \(t = 0\) starts with an even probability distribution (0.33, 0.33, 0.33) across all contracts in the menu.
By default, we set contract 1 to be a ‘spot’ contract with no pre-specified energy limit, i.e., potentially $L^1 \to \infty$. Contracts 2 and 3 set upper limits on how much energy a household can draw. We impose the following constraints on the contracts: $L^1 > L^2 > L^3$ and $p^1 > p^2 > p^3$. Thus the spot contract is the risk-less contract but with the highest per unit price, while contract 3 is the riskiest contract but with the lowest per unit price. Contract 2 is an intermediate one, providing a balance between risk and cost.

As described above, the choice probabilities are updated by the household at the end of period $t$ based on which of the three constraints are binding on the household in the same period. For any given household, let the actual contract chosen in period $t$ be denoted by $k^*(t)$. Let $\delta$ be an adjustment parameter, which is the amount households adjust their choice probabilities every period. In such a case, Rules 1H, 2H, 3H are operationalized in the following manner:

**Rule 1H - Budget constraint binds in period $t - 1$**

- a. If $k^*(t - 1) = 1 \to \begin{cases} 
\rho^1(t) = \rho^1(t - 1) - \delta, \\
\rho^2(t) = \rho^2(t - 1) + \frac{\delta}{2}, \\
\rho^3(t) = \rho^3(t - 1) + \frac{\delta}{2}
\end{cases}$

- b. If $k^*(t - 1) = 2 \to \begin{cases} 
\rho^1(t) = \rho^1(t - 1) - \frac{\delta}{2}, \\
\rho^2(t) = \rho^2(t - 1) - \frac{\delta}{2}, \\
\rho^3(t) = \rho^3(t - 1) + \delta
\end{cases}$

- c. If $k^*(t - 1) = 3 \to \begin{cases} 
\rho^1(t) = \rho^1(t - 1) - \frac{\delta}{2}, \\
\rho^2(t) = \rho^2(t - 1) - \frac{\delta}{2}, \\
\rho^3(t) = \rho^3(t - 1) + \delta
\end{cases}$

**Rule 2H – Incentive constraint binds in period $t - 1$**

- a. If $k^*(t - 1) = 1 \to \begin{cases} 
\rho^1(t) = \rho^1(t - 1) + \delta, \\
\rho^2(t) = \rho^2(t - 1) - \frac{\delta}{2}, \\
\rho^3(t) = \rho^3(t - 1) - \frac{\delta}{2}
\end{cases}$

- b. If $k^*(t - 1) = 2 \to \begin{cases} 
\rho^1(t) = \rho^1(t - 1) + \frac{\delta}{2}, \\
\rho^2(t) = \rho^2(t - 1) + \frac{\delta}{2}, \\
\rho^3(t) = \rho^3(t - 1) - \delta
\end{cases}$
c. If \( k^*(t-1) = 3 \) → \[
\begin{align*}
\rho^1(t) &= \rho^1(t-1) + \delta \\
\rho^2(t) &= \rho^2(t-1) + \frac{\delta}{2} \\
\rho^3(t) &= \rho^3(t-1) - \frac{\delta}{2}
\end{align*}
\]

**Rule 3H – Coverage limit constraint binds in period \( t - 1 \)**

a. If \( k^*(t-1) = 1 \) → \[
\begin{align*}
\rho^1(t) &= \rho^1(t-1) + \delta, \\
\rho^2(t) &= \rho^2(t-1) - \frac{\delta}{2} \\
\rho^3(t) &= \rho^3(t-1) - \frac{\delta}{2}
\end{align*}
\]
b. If \( k^*(t-1) = 2 \) → \[
\begin{align*}
\rho^1(t) &= \rho^1(t-1) + \delta, \\
\rho^2(t) &= \rho^2(t-1) - \frac{\delta}{2} \\
\rho^3(t) &= \rho^3(t-1) - \frac{\delta}{2}
\end{align*}
\]
c. If \( k^*(t-1) = 3 \) → \[
\begin{align*}
\rho^1(t) &= \rho^1(t-1) + \frac{\delta}{2} \\
\rho^2(t) &= \rho^2(t-1) + \frac{\delta}{2} \\
\rho^3(t) &= \rho^3(t-1) - \delta
\end{align*}
\]

Both Rules 2H and 3H are similar in that they both add weight on contracts with higher coverage. The only distinction between them is in the rate at which they shift the households’ choice towards the spot contract: Rule 3H shifts the probability weights in favor of the spot contract at a higher rate than 2H, while Rule 1H shifts the weights in favor of cheaper contracts. The adjustment parameter \( \delta \) is fixed exogenously at 0.05. Once the updates have taken place, the probabilities are rebased to ensure that they are bounded within the \([0, 1]\) interval.

### 3.1 The Experimental Setup

The agent-based simulations are implemented in Netlogo 6, incorporating the behavioural rules for the agents described above. Each agent represents a household, with household-specific parameters presented in Table 1. The observer context plays the role of the single supplier in the market. Each run of the simulation represents one instance of a single experiment, where an experiment is defined as a unique combination of input parameter values. Each experiment is replicated 10 times, in order to account for randomness in the model, where each replication is labelled as a “run”. Each run is composed of 300 time steps. After repeated manual screening of runs under various parameter combinations, it was observed that the model attained a high degree of stability well within 300 time steps.
Table 1 also distinguishes between the input, control and output parameters within the simulation, along with the context they belong to – household, supplier or environmental. The input parameters are those whose values change from experiment to experiment and while the values of the control parameters are held fixed across all experiments. The choice of input versus control factors were made following a series of sensitivity analyses on all exogenous parameters, to determine which of these were relevant for the research questions to be addressed in this paper. Once this distinction was made, we adopted a $2^k$ factorial design for the experiments – where the agent based model outcomes were tested on combinations of two distinct values of the input parameters and their interactions. Table 1 also presents the values of the input and control parameters used.

Table 1: List of parameters and operational values in the simulations

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Context</th>
<th>Meaning</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\bar{\alpha}$</td>
<td>Household</td>
<td>Upper limit of household-specific coefficient of absolute risk aversion</td>
<td>$[0.1, 0.9]$</td>
</tr>
<tr>
<td>$\bar{L}$</td>
<td>Household</td>
<td>Upper limit of potential loss per household</td>
<td>$[100, 500]$</td>
</tr>
<tr>
<td>$B$</td>
<td>Household</td>
<td>Upper limit of household-specific budget</td>
<td>$[50, 500]$</td>
</tr>
<tr>
<td>$\bar{\pi}$</td>
<td>Household</td>
<td>Upper limit of household-specific probability of loss</td>
<td>$[0.2, 0.8]$</td>
</tr>
<tr>
<td>$p^1_0$</td>
<td>Supplier</td>
<td>Initial unit price for contract 1 (at $t = 0$)</td>
<td>$[100, 150]$</td>
</tr>
<tr>
<td>$L^1$</td>
<td>Supplier</td>
<td>Limit on energy that can be drawn under contract 1, as a proportion of upper limit of potential loss ($L^1 \cdot \bar{L}$)</td>
<td>$[1]$</td>
</tr>
<tr>
<td>$p^2_0$</td>
<td>Supplier</td>
<td>Initial unit price for contract 2 (at $t = 0$)</td>
<td>$[25, 75]$</td>
</tr>
<tr>
<td>$L^2$</td>
<td>Supplier</td>
<td>Limit on energy that can be drawn under contract 2, as a proportion of upper limit of potential loss ($L^2 \cdot \bar{L}$)</td>
<td>$[0.5, 0.9]$</td>
</tr>
<tr>
<td>$p^3_0$</td>
<td>Supplier</td>
<td>Initial unit price for contract 3 (at $t = 0$)</td>
<td>$[1, 10]$</td>
</tr>
<tr>
<td>$L^3$</td>
<td>Supplier</td>
<td>Limit on energy that can be drawn under contract 3, as a proportion of upper limit of potential loss ($L^3 \cdot \bar{L}$)</td>
<td>$[0.1, 0.45]$</td>
</tr>
<tr>
<td>$\theta$</td>
<td>Supplier</td>
<td>Threshold in cumulative demand change for price adjustment</td>
<td>$[0.05, 0.5]$</td>
</tr>
<tr>
<td><strong>Control</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\bar{U}$</td>
<td>Household</td>
<td>Utility under certain zero loss</td>
<td>$[2500]$</td>
</tr>
<tr>
<td>$N$</td>
<td>Environment</td>
<td>Number of households</td>
<td>$[2500]$</td>
</tr>
<tr>
<td>$F^1_1$</td>
<td>Supplier</td>
<td>Lump sum payment under contract 1</td>
<td>$[0]$</td>
</tr>
<tr>
<td>$F^2$</td>
<td>Supplier</td>
<td>Lump sum payment under contract 2</td>
<td>$[50]$</td>
</tr>
<tr>
<td>$F^3_3$</td>
<td>Supplier</td>
<td>Lump sum payment under contract 3</td>
<td>$[50]$</td>
</tr>
<tr>
<td><strong>Output</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p^1_{300}$</td>
<td>Supplier</td>
<td>Final unit price under contract 1</td>
<td></td>
</tr>
<tr>
<td>$p^2_{300}$</td>
<td>Supplier</td>
<td>Final unit price under contract 2</td>
<td></td>
</tr>
<tr>
<td>$p^3_{300}$</td>
<td>Supplier</td>
<td>Final unit price under contract 3</td>
<td></td>
</tr>
<tr>
<td>Revenue</td>
<td>Supplier</td>
<td>Cumulative revenue for $\tau$ previous periods</td>
<td></td>
</tr>
<tr>
<td>$h^F$</td>
<td>Environment</td>
<td>Houses (% of those facing a loss) with full coverage, averaged across 300 runs</td>
<td></td>
</tr>
<tr>
<td>$h^H$</td>
<td>Environment</td>
<td>Houses (% of those facing a loss) with partial coverage due to binding budget constraint</td>
<td></td>
</tr>
<tr>
<td>$h^L$</td>
<td>Environment</td>
<td>Houses (% of those facing a loss) with partial coverage due to binding contract coverage limit constraint</td>
<td></td>
</tr>
<tr>
<td>$h^I$</td>
<td>Environment</td>
<td>Houses (% of those facing a loss) with partial coverage due to binding incentive constraint</td>
<td></td>
</tr>
<tr>
<td>$h^{BL}$</td>
<td>Environment</td>
<td>Houses (% of those facing a loss) with partial coverage due to binding budget constraint and contract limit constraint</td>
<td></td>
</tr>
<tr>
<td>avg $\rho^1$, sd $\rho^1$</td>
<td>Household</td>
<td>Mean and SD of the distribution of $\rho^1(300)$ across households</td>
<td></td>
</tr>
<tr>
<td>avg $\rho^2$, sd $\rho^2$</td>
<td>Household</td>
<td>Mean and SD of the distribution of $\rho^2(300)$ across households</td>
<td></td>
</tr>
<tr>
<td>avg $\rho^3$, sd $\rho^3$</td>
<td>Household</td>
<td>Mean and SD of the distribution of $\rho^3(300)$ across households</td>
<td></td>
</tr>
</tbody>
</table>

## 4 Results

The model solves for final prices for each one of the three type of contracts, the revenue for utilities, and the extent to which households internalize and transfer risks to the utility. We measure these by estimating the percentage of houses that obtain full or partial coverage. For those who only obtain partial coverage, we investigate the source of that decision, i.e., whether the decision was constrained by their budget, by contract limits and/or binding incentives.

To give a comprehensive picture, we present the convergence and stability properties of the model based on the central values, variances and trends in output variables, measured over the entire 300 steps in each run. We then explain the observed variation in the outputs at the macro level, using multivariate regressions, and present the estimated impact of input variables. We measure the values of output variables at the end of each run in each experiment, or in other words the ‘final’ value of the output at the 300th step. Finally, we examine sub-samples of households and correlate their behavior with their intrinsic properties to explore the behavior at the agent level. This is done using a final and intermediate measure of outputs in each run.

### 4.1 Convergence

We find that the model has strong convergence properties in the output variables under all input settings explored within the simulations. This is true for prices, the proportion of houses facing
one or more (or no) constraints, and in the distribution of choice probabilities. This indicates that, conditional on the learning and adaptation algorithms of the supplier and households, the market moves towards a dynamically stable outcome within the stipulated 300 steps.

Figure 2. Convergence patterns in the unit prices of the three contracts

Figures 2-4 show outputs of a sample of runs from the sensitivity analysis, where the control variables are varied across two levels – low and high. What we observe is that the output variables either achieve a stable value quickly (such as in the prices in Figure 1), or the variations exhibit a predictable pattern within a very narrow band (such as in choice probabilities and household proportions in Figures 2 and 3, respectively). These patterns are consistent in the actual experiments, where input variables are varied and controls are held fixed.

This implies that the dynamic model implemented here exhibits strong convergence properties, even without the strict rationality assumptions of the static case. A simple reinforcement learning mechanism can provide stable outcomes in the market.
Figure 3. Convergence patterns in the average choice probabilities across the three contracts

Figure 4. Convergence patterns in the proportions of households facing alternative constraints
4.2 Input-output relationships
Here we present the partial impact of input variables on output variables using a set of linear regressions, in which the coefficients of the input variables indicate the *partial* impact of the input on the output. Tables 2-4 show the magnitude of the impact, whether the impact is positive or negative and statistical significance of independently varying each input on the output, as measured in the experiments. The values presented in bold indicate a relatively large magnitude of impact (which is statistically significant) when compared with the size of other coefficients in the same regression equation.

4.2.1 Impact on contract prices and revenue
We observe that as the potential loss for households increase, they generally switch from cheaper but riskier to more expensive but safer contracts. The unit prices of the less risky contracts (1 and 2) seem to depend positively on the upper limit of expected losses faced by the households, as seen by the coefficients of $\bar{\pi}$. However, the price of contract 3, the riskiest contract, has a negative and significant coefficient. Thus, higher levels of expected loss faced by households pushes up the demand for the safer contracts with relatively wider coverage, with households willing to pay the higher unit price.

Table 2. Effect sizes on output variables – final prices and revenue

<table>
<thead>
<tr>
<th>Output</th>
<th>$p_{300}^1$</th>
<th>$p_{300}^2$</th>
<th>$p_{300}^3$</th>
<th>revenue</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>-44.18***</td>
<td>-12.91***</td>
<td>2.05***</td>
<td>3.27E04***</td>
</tr>
<tr>
<td>$\bar{\pi}$</td>
<td>28.36***</td>
<td>4.20***</td>
<td>-0.80***</td>
<td>7.48E04***</td>
</tr>
<tr>
<td>$\bar{L}$</td>
<td>0.00</td>
<td>0.00</td>
<td>-0.001***</td>
<td>23.39***</td>
</tr>
<tr>
<td>$\bar{\alpha}$</td>
<td>-0.06</td>
<td>-0.22</td>
<td>-0.02</td>
<td>-45.64</td>
</tr>
<tr>
<td>$\bar{B}$</td>
<td>-0.02***</td>
<td>-0.01***</td>
<td>0.00</td>
<td>247.70***</td>
</tr>
<tr>
<td>$p_{300}^1$</td>
<td>1.37***</td>
<td>0.00</td>
<td>0.00</td>
<td>3.58</td>
</tr>
<tr>
<td>$L^2$</td>
<td>83.23***</td>
<td>12.26***</td>
<td>-2.45***</td>
<td>2.27E04***</td>
</tr>
<tr>
<td>$p_{300}^2$</td>
<td>-0.003</td>
<td>1.10***</td>
<td>0.00</td>
<td>9.98</td>
</tr>
<tr>
<td>$L^3$</td>
<td>59.64***</td>
<td>22.60***</td>
<td>-2.31***</td>
<td>7.46E04***</td>
</tr>
<tr>
<td>$p_{300}^3$</td>
<td>0.38***</td>
<td>0.08***</td>
<td>0.93***</td>
<td>1.55E03***</td>
</tr>
<tr>
<td>$\theta$</td>
<td>-160.00***</td>
<td>-11.60***</td>
<td>2.70***</td>
<td>3.22E03*</td>
</tr>
</tbody>
</table>
We observe that the demand for the riskiest contract not only falls, as expected, when its nearest rival becomes less risky, but it also falls when it becomes less risky. Less frequent but larger price changes are associated with increased demand for less risky alternatives and lower demand for the riskier contract. Overall, it seems that the demand for the less risky contracts is more sensitive to changes in the above input parameters than the riskier ones. This is apparent in the gradual decrease in the size of the coefficients from a high positive value (contract 1) to a small negative value (contract 3).

The utility’s revenue is also most strongly impacted by the same parameters as above, plus the initial price of contract 3, \( p_0^3 \). Of all the initial prices, only the initial price of contract 3, the riskiest contract, has a notable impact its final price, affecting it positively and, in turn, positively impacting the utility’s revenue. This is another way in which the riskiest contract is distinct from the other two.

4.2.2 Constrained households
One would expect that increasing coverage would reduce the proportion of households constrained by coverage limits, and possibly increase the proportion obtaining full coverage. However, as shown in Table 3, this is not always the case (negative coefficient of \( L^2 \) for \( h^F \), and a positive coefficient of \( L^2 \) for \( h^L \)). We also see that varying \( L^2 \) and \( L^3 \) also seems to affect the proportion of households subject to the budget constraint, which is a surprising result. No households under the settings used in our experiments faced a binding incentive constraint (where the actual loss was greater than the certainty equivalent).

Table 3. Effect sizes output variables – household coverage and constraints

<table>
<thead>
<tr>
<th>Input</th>
<th>( h^F )</th>
<th>( h^B )</th>
<th>( h^L )</th>
<th>( h^{BL} )</th>
<th>( h^I )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>6.79***</td>
<td>44.65***</td>
<td>6.79***</td>
<td>48.07***</td>
<td>NA</td>
</tr>
<tr>
<td>( \bar{\pi} )</td>
<td>-0.4***</td>
<td>0.18</td>
<td>-0.49***</td>
<td>0.63***</td>
<td>NA</td>
</tr>
<tr>
<td>( \bar{L} )</td>
<td>-0.01***</td>
<td>0.01***</td>
<td>-0.01***</td>
<td>0.01***</td>
<td>NA</td>
</tr>
<tr>
<td>( \bar{\alpha} )</td>
<td>-0.01</td>
<td>-0.02</td>
<td>-0.01</td>
<td>0.05</td>
<td>NA</td>
</tr>
<tr>
<td>( \bar{B} )</td>
<td>0.02***</td>
<td>-0.02***</td>
<td>0.02***</td>
<td>-0.03***</td>
<td>NA</td>
</tr>
<tr>
<td>( p_0^1 )</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>NA</td>
</tr>
<tr>
<td>( L^2 )</td>
<td>5.49***</td>
<td>9.47***</td>
<td>5.48***</td>
<td>-15.54***</td>
<td>NA</td>
</tr>
<tr>
<td></td>
<td>$p_0^2$</td>
<td>0.00</td>
<td>0.01***</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>---</td>
<td>----------</td>
<td>------</td>
<td>---------</td>
<td>------</td>
<td>------</td>
</tr>
<tr>
<td>$L^3$</td>
<td>-17.72***</td>
<td>34.53***</td>
<td>-17.72***</td>
<td>-27.31***</td>
<td>NA</td>
</tr>
<tr>
<td>$p_0^3$</td>
<td>-0.6***</td>
<td>0.32***</td>
<td>-0.67***</td>
<td>0.67***</td>
<td>NA</td>
</tr>
<tr>
<td>$\theta$</td>
<td>-1.23***</td>
<td>0.85***</td>
<td>-1.23***</td>
<td>1.14***</td>
<td>NA</td>
</tr>
</tbody>
</table>

4.3 Choice probabilities
As losses become more likely, the probability of choosing contract 2 increases. This seems to suggest that the increased chance of households facing a loss leads to an increased preference for the middle contract, which is both relatively less risky than contract 3 and less expensive than contract 1. There is still a spread around the choice probabilities across households.

The results presented in Table 4 suggest that the upper limit of the household-specific loss ($\bar{\pi}$) and the coverage limits ($L^2$ and $L^3$) are the only input parameters which have a notable impact. Thus there is an increased preference for the ‘safer’ option.

Table 4. Effect sizes output variables – choice probability means and standard deviations

<table>
<thead>
<tr>
<th>Output</th>
<th>$avg \rho^1$</th>
<th>$sd \rho^1$</th>
<th>$avg \rho^2$</th>
<th>$sd \rho^2$</th>
<th>$avg \rho^3$</th>
<th>$sd \rho^3$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>0.49***</td>
<td>0.44***</td>
<td>0.20***</td>
<td>0.18***</td>
<td>0.31***</td>
<td>0.37***</td>
</tr>
<tr>
<td>$\bar{\pi}$</td>
<td>-0.06***</td>
<td>-0.07***</td>
<td>0.11***</td>
<td>0.04***</td>
<td>-0.04***</td>
<td>-0.03***</td>
</tr>
<tr>
<td>$\bar{L}$</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>$\bar{\alpha}$</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>$B$</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>$p_0^0$</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>$L^2$</td>
<td>-0.18***</td>
<td>-0.12***</td>
<td>0.00</td>
<td>0.00</td>
<td>0.17***</td>
<td>-0.02***</td>
</tr>
<tr>
<td>$p_0^1$</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>$L^3$</td>
<td>-0.24***</td>
<td>-0.03***</td>
<td>-0.20***</td>
<td>-0.02***</td>
<td>0.44***</td>
<td>0.09***</td>
</tr>
<tr>
<td>$p_0^2$</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
</tr>
<tr>
<td>$\theta$</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>0.01***</td>
<td>0.00</td>
</tr>
</tbody>
</table>
4.3.1 Interactions of inputs
Figures 4-7 show how output variables are affected by each input for the entire range of values of the other input variables. We then concentrate on the joint impact of the four primary inputs - $\bar{\pi}$, $L^2$, $L^3$ and the threshold parameter $\theta$. 4

4.3.2 Price variation per contract
Figures 5a, b and c explore the variation in the final unit prices in the three contracts across different input parameter settings. As can be seen, $\theta$ is a strong moderator of the relationships between the rest of the inputs and prices. We find there are consistent relationships between the unit prices and $\bar{\pi}$, $L^2$, $L^3$ at low values of $\theta$. However, these relationships disappear almost completely for higher values of $\theta$. Therefore, in situations where the utility makes infrequent but large changes in prices, outputs no longer depend on the other parameters. This is an important result in terms of market design and has important regulatory implications.

We noted other significant interaction effects between the input and output variables, such as the positive $\bar{\pi} \times L^2$ effect on $\rho^1$ (Figure 6a), implying that the fall in $\rho^1$ due to increased $\bar{\pi}$ is steeper under high values of $L^2$.

5 Conclusion and policy implications
This paper tests the viability of creating an energy insurance market for energy self-sufficient households with contracts according to their preferences for risk, allowing utilities to continue generating revenue from households who no longer rely on electricity bought from the grid. The utility serves the purpose of an insurance provider that supplies a menu of contracts, and the households select the appropriate product based on expected loss, risk profile and budget.

We find it is more efficient for households to transfer the ‘last mile’ of risk to the utility rather than bear the disutility of a blackout. We find that an insurance market can act as an indirect

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4 Figures 5 to 7 graphically present the impact of the four inputs on every output variable. In each figure, each box and whiskers plot shows the four quartiles and the median of the output variable in question across all the 10 runs in any given experiment. Each figure is divided into eight regions, with two boxplots in each region. These two boxplots represent experiments with low (0.2) and high (0.8) values of $\bar{\pi}$ respectively for given values of the other three inputs. The left four regions represent experiments with the lower value of $\theta=0.05$, whereas the four regions on the right half of the figures represent the higher value of $\theta=0.5$. Each half is further sub-divided into two quarters – where each quarter is representative of low $L^3$ (0.1) and high $L^3$ (0.45) respectively. Finally, each quarter is further sub-divided into two sections, where each section represents experiments with the low value of $L^2$ (0.5) and the high value of $L^2$ (0.9). As mentioned above, there are eight such sections, with two boxplots in each. The ordering of experiments in each figure is consistent across Figures 5-7, to make them comparable.
regulatory mechanism to manage reliability in a distributed power market. The static model illustrates the possible nature of new insurance products, the profile of households who purchase them, and the pricing policies set by the utility who have perfect information about the households and operate in one period only. The dynamic model, implemented as an ABM, extends the static model to incorporate imperfect information on the part of the utility, as well as the bounded rational nature of households (who may choose to over or under insure), and the role of dynamic learning mechanisms in driving the long-term trajectory of the market. We find that under the general relaxed assumptions of the dynamic model, a stable market can exist, where prices converge to a long-run equilibrium, and the distribution of choices made by households becomes stationary (within limits). We find that it is the coverage limits which seem to most influence the choice of contracts at the household level and the final market prices. This would imply that there could be a sizeable market for this service, concurring with the finding that the revenue of the utility-insurer depends mostly on the coverage limits of the contracts and households’ potential energy needs. Thus, the utility has a degree of control over its revenues by choosing the coverage limits or, in other words, the riskiness of the contracts available, as well as the nature of the price adjustments it carries out in the market. At the same time, the long-term choices made by households may be influenced by the riskiness associated with the contracts as well as the possible losses they may face.

From a regulatory point of view, this proposal is in line with the general trend in regulatory governance that moves towards more flexible, incentive-based and indirect regulation (Parmet, 2013). Self-regulation and decentralized mechanisms would be a natural fit in the distributed power generation based sector. We showed that the insurance market proposed in this paper would help to internalize the risk to a great extent, reducing blackouts significantly. However, there may be households unable to cover their full energy needs due to budgetary considerations or the extreme nature of their risk profiles. This paper shows a feasible way forward for both utilities and regulators in the event of widespread distributed power systems.
Figure 5a. Variation in unit price of Contract 1

Figure 5b. Variation in unit price of Contract 2
Figure 5c. Variation in unit price of Contract 3

Figure 6a. Variation in average probability of choice of contract 1
Figure 6b. Variation in average probability of choice of contract 2

Figure 6c. Variation in average probability of choice of contract 3
Figure 7a. Variation in percentage of households fully covered

Variation in $\bar{h}^F$ across high and low values of $\bar{\alpha}, L^1, L^2, \theta$

Figure 7b. Variation in percentage of households with binding budget constraints and coverage limits

Variation in $\bar{h}^{BL}$ across high and low values of $\bar{\alpha}, L^1, L^2, \theta$
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