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Identification of Gas-Liquid Flow Regimes Using a Non-intrusive Doppler Ultrasonic Sensor and Virtual Flow Regime Maps

Somtochukwu Godfrey Nnabuife\textsuperscript{a}, Karl Ezra S. Pilario\textsuperscript{a,b}, Liyun Lao\textsuperscript{a,*}, Yi Cao\textsuperscript{c}, Mahmood Shafiee\textsuperscript{a}

\textsuperscript{a}Department of Energy and Power, Cranfield University, Cranfield, United Kingdom
\textsuperscript{b}Department of Chemical Engineering, University of the Philippines Diliman, Republic of the Philippines
\textsuperscript{c}College of Chemical and Biological Engineering, Zhejiang University, People's Republic of China

*Corresponding author, email address: l.lao@cranfield.ac.uk

Abstract

The accurate prediction of flow regimes is vital for the analysis of behaviour and operation of gas/liquid two-phase systems in industrial processes. This paper investigates the feasibility of a non-radioactive and non-intrusive method for the objective identification of two-phase gas/liquid flow regimes using a Doppler ultrasonic sensor and machine learning approaches. The experimental data is acquired from a 16.2-m long S-shaped riser, connected to a 40-m horizontal pipe with an internal diameter of 50.4 mm. The tests cover the bubbly, slug, churn and annular flow regimes. The power spectral density (PSD) method is applied to the flow modulated ultrasound signals in order to extract frequency-domain features of the two-phase flow. Principal Component Analysis (PCA) is then used to reduce the dimensionality of the data so as to enable visualisation in the form of a virtual flow regime map. Finally, a support vector machine (SVM) is deployed to develop an objective classifier in the reduced space. The classifier attained 85.7% accuracy on training samples and 84.6% accuracy on test samples. Our approach has shown the success of the ultrasound sensor, PCA-SVM, and virtual flow regime maps for objective two-phase flow regime classification on pipeline-riser systems, which is beneficial to operators in industrial practice. The use of a non-radioactive and non-intrusive sensor also makes it more favorable than other existing techniques.

Keywords: Doppler ultrasound, Support vector machine (SVM), Probability density function (PDF), Principal component analysis (PCA), S-shaped riser

1 Introduction

Two-phase gas-liquid flow is encountered frequently in the industrial operations such as nuclear power plant steam generators, boilers, chemical reactors and petroleum transportation (Julia and Hibiki, 2011). The different types of interfacial structures between different phases of fluids, known as multiphase flow regimes, can be geometrically complex and varying. The flow can be steady or unsteady, turbulent or laminar, gas/liquid segregated or mixed. Gas can flow within the liquid as bubbles or liquid can flow within the gas as droplets (Falcone et al., 2002).

The governing flow regime is influenced by many parameters such as gas/liquid superficial velocities, gas/liquid densities, gas/liquid surface tension, gas/liquid viscosities, pipe diameter
and pipe inclination (Thorn et al., 2012). Traditionally, flow regime maps are used to illustrate the dependency of the flow regime on two quantities, which are usually the superficial gas and liquid flow rates (Falcone et al., 2009). Yet, characterising and measuring two-phase flow is still challenging due to its inherent complex nature. Thus, the problem of flow regime identification remains to be relevant up to the present.

Flow regime identification methods can either be subjective techniques (direct observation) or objective techniques (scientific or indirect determination) (Rouhani and Sohal, 1983). The subjective or direct techniques involve the operator in visually interpreting an image of the flow to classify it into a flow regime. Objective or indirect determination is a two-part process. The operator must firstly utilise a suitable experimental methodology to measure flow parameters features correctly and then analyse the flow features objectively to categorise the flow regime (Juliá et al., 2008).

Currently, gas/liquid two-phase flow regime identification is mainly carried out by subjective means such as direct visual observation and via cameras (Peddu et al., 2017). Hence, the accurate classification of flow regimes is yet to be standardised, and it mostly depends upon the interpretation of individual visual views, which would lead to inconsistency in the flow regime identification due to human subjectivity. The main drawback of visual observations is that the pictures are often challenging to interpret and confusing, in particular when handling high flow velocities even with the use of high-speed cameras. Moreover, flow channels are often opaque so that flow identification by visual means is impossible (Barnea et al., 1980). Although there are numerous flow regime identification approaches already studied for two-phase gas/liquid flow, industrial acceptance remains challenging. Subjective techniques cannot facilitate industrial automation where many important decisions depend on the governing flow regime.

Significant efforts have already been made to develop flow regime identification using objective methodologies. Several research studies have used a phase distribution measurement approach.
One of the methods in this regard is the use of invasive-point sensors such as pitot tubes, fibre-optic or electrical probes and hot-wire anemometer (Barnea, 1987). The major setback to these methods is that the sensors disturb the flow fields during the measurement of void or pressure fluctuations (Dyakowski, 1996). Hence, non-invasive means must be deployed to differentiate the boundaries between divers flow regimes.

Objective flow regime identification using a clamped-on, non-invasive sensor is of great interest in many industries. Non-invasive methods are highly attractive as they eliminate the need for immersion of instrumentation in the flow. Jones and Delhaye (1976) investigated and summarised different measuring methods applied to a two-phase flow of which very few are employed directly for the characterisation of the flow regime. For instance, Barnea et al. (1980) used an enhanced electrical conductance probe in a two-phase near horizontal, horizontal and vertical flows for flow regime identification.

Among the non-invasive sensors, radiation attenuation methods are more widely used in many industrial applications due to their reliability. To mention a few, Jones and Zuber (1975) studied an X-ray void measurement system for vertical two-phase flow in a rectangular channel; Salgado et al. (2010) achieved flow regime identification using gamma-ray pulse height distributions (PHDS) and artificial neural networks (ANNs); Blaney and Yeung (2008) analysed probability distributions using the self-organising feature map and gamma densitometer data for multiphase flow regime identification; Sunde et al. (2005) proposed an enhanced method, which compares at every flow condition the visualisation of the intensity of gamma rays measurements. Generally, radiation attenuation methods based on gamma rays, X-rays and neutrons are already established online measurement systems. When compared with each other, gamma densitometer has enormous merits, such as high penetration and cost-effectiveness (Chaouki et al., 1997). However, the major drawback to these methods is their radioactive nature, which is hazardous. The need to increase the gamma source strength with an increase in density or the pipe wall thickness requires radiation protection increase, hence minimises its portability.
Chakraborty et al. (2009) presented a novel ultrasonic method for two-phase flow void fraction measurement using an ultrasonic sensor and two signal processing techniques established on the time series analysis approach: the logical signal space partitioning and the symbolic filtering. Although the theory on symbolic dynamic filtering was established, identification using pulse-echo mode is not a full classification method of flow regimes, but flow patterns instead (Jha et al., 2012). It was noted that more research needs to be carried out on experimental and computational work before applying the method in the industry. Another drawback to this method is that the set-up is invasive even though the ultrasonic method itself is non-intrusive. As an extension of the work by Chakraborty et al., (2009), Jha et al. (2012) presented the concept of implementing ultrasonic pulse echoes in a clamped-on set-up in connection with the symbolic dynamic filtering for deployment in the industries.

Regardless of the prospect of using ultrasonic pulse-echo for flow regime identification, the method is based on computational models. The computational models apply a set of non-linear equations for flow regime identification, which are frequently simplified. In practice, the simplified equations are difficult to implement since the knowledge of various flow parameters are required, such as pipe thickness and pipe diameter. The accuracy of these equations are also compromised when flow parameters deteriorate with time (Meribout et al., 2010). In addition, the ultrasound pulse-echo method is limited by the maximum velocity that it can measure due to the Nyquist criterion (Evans and McDicken, 2000).

Doppler ultrasonic sensors can also achieve non-invasive flow velocity measurement. This technique is ubiquitous in the medical field. The method employs a shift in frequency due to the flow velocities as a means for flow regime prediction (Übeyli and Güler, 2005). The applicability of continuous wave ultrasonic Doppler (CWUD) in two-phase flow velocity measurement was investigated by Kouam et al. (2003). They suggested the use of frequency resolution methods to resolve the issue of the presence of coloured noise in velocity measurement, which otherwise poses a severe problem to the classical frequency estimators.
In this paper, a non-intrusive and non-radioactive method for the objective identification of two-phase gas/liquid flow regime is proposed using CWUD signals and machine learning (ML) approaches. Many ML solutions to objective flow regime identification have already been proposed, such as (Xie et al., 2004; Hanus et al., 2017; Wang and Zhang, 2009; Trafalis et al., 2005). In this work, to better facilitate the applicability to industrial practice, principal components analysis (PCA) is used particularly for visualising the information from intrinsic flow regime features in 2-dimensional space. To this aim, a mapping is created so that in 2-dimensions, the mapped samples can be found clustered according to their respective flow regimes. SVM is then applied to the samples in the 2-dimensional space to create boundaries between the clusters. This leads to a virtual flow regime map that serves as visual aid to human operators for objective flow regime identification. In summary, the main contributions of this paper are as follows: (i) we explore the feasibility of visualizing frequency-domain features from ultrasonic Doppler signals in a 2D virtual flow regime map; and (ii) we make the first known effort towards the applicability of continuous wave Doppler ultrasound and the SVM to objectively identify flow regime in an S-shaped riser. By using safer and more advanced techniques for two-phase flow measurement and instrumentation, industries can achieve enhanced production, better process performance, and hence, larger economic advantages.

This paper is organised as follows: Section 2 presents the sensor principle and the algorithm for CWUD. In Section 3, the experimental method used in this study is described. Signal analysis using ML approaches are discussed in Section 4. In Section 5, the results and discussion of the analysed data are presented, and finally, conclusions and future work are given in Section 6.
2 Measurement Sensor and Algorithm

The Doppler shift (or Doppler Effect) is the frequency variation of an acoustic wave when movement exists between the acoustic receiver and the source, where the change in frequency is proportional to the acoustic source velocity (Weinstein, 1982). Thus, the velocity of the acoustic source is obtained by calculating the frequency shift between the acoustic receiver and the source (see Fig. 1(b)). In the ultrasonic Doppler flowmeter, shown in Fig. 1(a), a fixed-frequency acoustic beam is released continuously from the transducer into the flow. The beam is then reflected by the moving scatterers in the fluid, which could be bubbles in the flow (Chivers and Hill, 1975). Another ultrasonic transducer receives the scattered acoustic beam so that the velocity of the fluid estimated with the frequency shift based on Doppler Effect. Mathematically, the principle behind this sensor is discussed as follows.

![Figure 1: Ultrasound Doppler principle (Meire and Farrant, 1995)](image)

First, assume that the signal transmitted is

\[ x_t(t) = \varepsilon_t \cos(\omega_t t) \] (1)

and that the corresponding received signal from one of the scatterers is

\[ x_r(t) = \varepsilon_r \cos(\omega_t + \omega_d) t + \theta_1 \] (2)
where \( \omega_t = 2\pi f_t \) is the angular frequency of the transmitted signal, \( \omega_d = 2\pi f_d \) is the amount of shift in the angular frequency, and \( \theta_1 \) is the phase shift based on the scatterer distance between the receiver and the transducer (Evans et al., 1989).

Multiplying the two signals electronically will give:

\[
x_t(t) x_r(t) = \varepsilon_t \varepsilon_r \cos(\omega_t t) \cos(\{\omega_t + \omega_d\} t + \theta_1)
\]

(3)

\[
x_t(t) x_r(t) = \frac{\varepsilon_t \varepsilon_r}{2} \left[ \cos(\omega_d t + \theta_1) + \cos(2\omega_t + \omega_d) t + \theta_1 \right].
\]

(4)

The resulting signal is then low-pass filtered to remove the \( 2f_t \) source frequency, leaving only the desired Doppler signal (Evans et al., 1989):

\[
x_d(t) = \frac{\varepsilon_t \varepsilon_r}{2} \cos(\omega_d t + \theta_1).
\]

(5)

Additional signal processing may be needed since the received signal has reflected an ultrasound of amplitude greater than the signal backscattered from the moving scatterers. Finally, the relationship between the Doppler shift \( f_d \) and the velocity of the scatterer can be described as follows (Sanderson and Yeung, 2002):

\[
f_d = 2f_t \frac{v}{c} \cos \theta
\]

(6)

where \( f_d \) is the Doppler frequency shift, \( f_t \) is the transmitted ultrasound frequency, \( v \) is the flow velocity average, and \( \theta \) is the angle between the flow velocity and the ultrasound beam.

The Continuous-wave ultrasonic Doppler (CWUD) used in this work is a non-invasive flowmeter. The CWUD is suitable for the measurement of ultrasonic reflective fluid of flows. It calculates the shifts in frequency, processes the ultrasonic signals, and evaluates the velocity of the flow. The CWUD calculates the change in frequency of the signals reflected from the discontinuities or scatters like bubbles in the flowing fluid. To achieve a suitable bonding between the external conduit surface and the sensor, a glycerine gel was applied to avoid air cavities trapping between
the sensor and the conduit surface. The CWUD has two separate crystals transducers embedded in one probe which transmit and receive ultrasonic signals continuously at 500 KHz.

The CWUD has two piezoelectric crystal elements embedded in one transducer. The electronic circuit of the metre electrifies the transducer in a continuous mode; one of the transducers emits an ultrasonic signal and the other receiving transducer, provides the output signals (Kremkau, 1975). The received output signals are then filtered and amplified by the flowmeter electronics. The Doppler frequency shift signals are the processed output signal, and it was obtained using a data acquisition card (NI-PCI-6040E) and a LabVIEW program. Other specifications of the CWUD flow meter used in the experiment are given in Table 1.

Table 1: Continuous Wave ultrasonic Doppler flow meter specifications

<table>
<thead>
<tr>
<th>Model</th>
<th>DFM-2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Maker</td>
<td>United Automation Ltd., Southport, U.K.</td>
</tr>
<tr>
<td>Velocity range</td>
<td>0 to 19.99 feet per second velocity by LCD (Liquid Crystal Display).</td>
</tr>
<tr>
<td>Repeatability</td>
<td>1 % of reading.</td>
</tr>
<tr>
<td>Indicator</td>
<td>Sufficient signal strength only when green LED (Light Emitting Diode) is on</td>
</tr>
<tr>
<td>Temperature</td>
<td>Instrument 0 to 50°C. Standard sensor -30 to 70°C. HT Sensors are available up to 120°C</td>
</tr>
</tbody>
</table>

The detailed experimental specifications are given in the following section.

3 Test Rig and Experimental Procedure

3.1 Two-phase flow test rig set-up

The experiment was carried out on a 2-inch S-shaped riser of the three-phase flow loop at Cranfield University oil and gas centre. The 2-inch flow loop is made up of a 40-m horizontal pipeline, 5.5-m vertical lower section, 1.5-m down-comer, 5.7-m vertical upper section and 3.5-m topside section. This test rig is operated using the DeltaV (Fieldbus based supervisory, control and data acquisition) software provided by Emerson Process Management. The schematic diagram of the test rig is shown in Figure 2. The air used was supplied from the bank of two
compressors connected in parallel. When both compressors are run in parallel, a maximum air flow rate of 1410 m$^3$/hr FAD at 7 bar can be supplied. The air from the two compressors is accumulated in a 8-m$^3$ capacity receiver to reduce the pressure fluctuation from the compressor. Air from the receiver passes through a bank of three filters (coarse, medium, fine) and then through a cooler where debris and condensates present in the air are stripped from the air before it goes into the flow meters. The water flow rate was supplied from a 12.5-m$^3$ capacity water tank. The water was supplied into the flow loop by two multistage Grundfos CR90-5 pumps. The water pump has a duty of 100 m$^3$/hr at 10 bar. The speed control is achieved using frequency variables inverters. The water pumps are operated remotely using DeltaV, a fieldbus based supervisory, control and data acquisition software (SCADA). The water flow rate was metered by a 1-inch Rosemount 8742 magnetic flow meter (up to 7.36 l/s) and 3-inch Foxboro CFT50 Coriolis meter (up to 30 kg/s).

After the experiment, air and water were separated in an 11.12-m$^3$ horizontal three-phase gravity separator. After the separation in the three-phase separator and cleaning, air is exhausted into the atmosphere while water from the three-phase separator enters its 1.6-m$^3$ coalescer, where the water is further cleaned before returning to the storage tank.

The 2-inch S-shaped flow loop test facility used in this experiment have a 54.8-mm internal diameter, 40-m length and 1.5-m downcomer. The 2-inch S-shaped flow loop test section has a transparent pipe for flow regime observation. The air flow-rate was adjusted by controlling the valves through the DeltaV to achieve the desired flow regime.
A clamp-on non-intrusive CWUD transducer with an excitation voltage of ±10V, operating at a carrier frequency of 500 kHz was attached at the top-side of the S-shaped riser in Fig. 2. The ultrasound beam incident angle was 58° with respect to flow direction on the S-shaped riser. It is essential to place the ultrasonic sensor on the pipe at least 10 diameters away from the tees, valves and bends to prohibit measurement errors from cavitation, swirls and turbulent eddies. A gel coupling agent was applied between the pipe wall and the Doppler transducer to make the ultrasound energy transmission easier. The electronics of CWUD flow meter was adapted to record the voltage signals of the Doppler frequency shift for further analysis (see Fig. 3).

Ultimately, the process variable being measured by the ultrasound Doppler is average flow velocity. Based on the pipe scale and flow velocity range, it was estimated that the value of the flow velocity fluctuates at a frequency no more than 2 kHz. Hence, in the LabVIEW data acquisition system, a sampling frequency of 10 kHz is appropriate with respect to the Nyquist criterion, since this is 5 times the estimated upper limit frequency of the flow velocity fluctuations.
3.2 Flow regime classification methodology

3.2.1 Feature Extraction from ultrasonic Doppler signals

Feature extraction is the most crucial step in any flow regime identification method. This step aims to find any information from the measurement data that can be used to best distinguish among flow regimes. For high-frequency data, such as the ultrasonic Doppler signals, features can be extracted either from the time domain or frequency domain. In this work, the widely used frequency-domain power spectral density (PSD) features are adopted (de Kerret et al., 2017).

Given a stationary discrete-time signal $x(n)$, the power spectral density function $P_X(f)$ of this signal is defined as the Fourier transform of the autocorrelation sequence $R_X(k)$ (Xie et al., 2004):

$$P_X(f) = \sum_{k=-\infty}^{\infty} R_X(k) \exp \left( -2\pi i k \frac{f}{f_s} \right)$$  \hspace{1cm} (7)

where $f_s$ is the sampling frequency. Since the signal is only measured on a finite interval $[0, \ldots, N-1]$, Welch’s method is adopted for obtaining the PSD, which is given as

$$\hat{P}_X(f) = \sum_{k=-N+1}^{N-1} \hat{R}_X(k) \exp \left( -2\pi i k \frac{f}{f_s} \right)$$  \hspace{1cm} (8)
where the autocorrelation is (Xie et al., 2004):

\[
\hat{R}_x(k) = \frac{1}{N} \sum_{n=0}^{N-1-k} x(n + k)x(n).
\]

(9)

Using Welch’s method in the same way as did Abbagoni and Yeung (2016), the PSD features were analysed from each sample of ultrasonic Doppler signals at various gas-liquid flow rates as shown in Fig. 4. A total of 130 data samples of different superficial gas and liquid velocities were recorded. Different flow regime labels were assigned to each data sample by visual observation at the same ambient temperature conditions. Each data sample acquired consists of Doppler frequency shift signals recorded for a period of 900s. The data set was sub-divided into 70% for training (91 samples) and 30% for testing (39 samples). With a sampling frequency of 10 kHz, a Hanning window of length 1024 and a 75% overlap were used in the Welch method.

![Gas and liquid flow rates of all samples from the experiment](image)

Figure 4: Gas and liquid flow rates of all samples from the experiment

Typical power spectral estimates from each flow regime are presented in Fig. 5. Notice that the relevant frequency spectrum ranges from 0-1200 Hz. In this range, the PSD spectrum is distinct in each flow regime. To obtain the actual features that can distinguish between the flow regimes, bands of length 120 Hz were taken from the power spectrum and the mean PSD was computed on each band, as did Abbagoni and Yeung, (2016). Also, the maximum peak of the PSD, the mean
weighted frequency $\bar{f}$ of the spectral power and the variance of the spectral power equation $\sigma_f^2$ were computed for each sample. The last two are computed as

$$\bar{f} = \frac{\sum_i f_i P_x(f_i)}{\sum_i P_x(f_i)}$$  \hspace{1cm} (10)$$

$$\sigma_f^2 = \frac{\sum_i (f_i - \bar{f})^2 P_x(f_i)}{\sum_i P_x(f_i)}.$$  \hspace{1cm} (11)$$

In total, 13 features are obtained from the power spectrum of ultrasound signals, namely: the mean PSD for each of the 10 frequency bands, the maximum peak of the PSD, $\bar{f}$, and $\sigma_f^2$. This approach is commonly used for distinguishing each flow regime using features in the frequency-domain (Abbagoni and Yeung, 2016; Drahoš and Čermák, 1989). Our work takes the further step of taking these features and visualising them in 2-dimensional space, before flow regime classification by an efficient pattern recognition technique.

Figure 5: Typical power spectra of each flow regime
3.2.2 Dimensionality Reduction for Visualization

In unsupervised machine learning, dimensionality reduction is a family of methods used to express the same information from a high-dimensional data set using only a few dimensions. In the previous subsection, the information as expressed in 13 features (dimensions) was taken from ultrasound Doppler signals for flow regime identification. Here, the same information is to be retained using only 2 dimensions by performing a dimensionality reduction method. Since this step is unsupervised, the information about the flow regime labels of the samples is not used yet. Nonetheless, the benefit of reducing to 2 dimensions is the ability to visualise the information in a 2-dimensional space. This leads to the realisation of a virtual flow regime map completely from ultrasound Doppler data.

In our work, principal components analysis (PCA) is used for linear dimensionality reduction, which is by far the most popular (Van Der Maaten et al., 2009). In PCA, the information is retained in a set of latent variables that are linear combinations of the original set of features. The PCA algorithm is outlined as follows.

Given an $M$-dimensional data set of $N$ samples, $\mathbf{x}_i \in \mathbb{R}^M$, $i = 1, 2, \ldots N$, PCA proceeds by first normalising the data to zero mean and unit variance, giving us $\mathbf{\bar{X}} \in \mathbb{R}^{M \times N}$. The sample covariance matrix of this data set is computed as

$$\Sigma_{xx} = \frac{1}{N - 1} \mathbf{\bar{X}}^T \mathbf{\bar{X}} \in \mathbb{R}^{N \times N}.$$  \hspace{1cm} (12)

The eigenvalue decomposition of the covariance matrix can be written as

$$\Sigma_{xx} = \mathbf{V} \Lambda \mathbf{V}^T$$  \hspace{1cm} (13)

where $\mathbf{V} \in \mathbb{R}^{N \times N}$ is the matrix of eigenvectors on each column and $\Lambda \in \mathbb{R}^{N \times N}$ is the diagonal matrix of decreasing eigenvalues. The columns of matrix $\mathbf{V}$ represent the principal directions that successively explain the maximum variance in the data, while the eigenvalues in $\Lambda$ are scaling factors equivalent to the data variance values themselves. The projection matrix is given by:
\[ P = VA^{-1/2} \in \mathbb{R}^{N \times N}. \]  

(14)

By using only the first 2 columns of \( P \), denoted as matrix \( P_2 \), the dimensionality of the data is reduced to 2 while preserving as much information possible. The projections are then applied to the covariance matrix so as to obtain latent variables \( L \) as

\[ L = P_2^T \Sigma_{xx} \in \mathbb{R}^{2 \times N}. \]  

(15)

After Eq. (15), each training sample is now represented by every column of \( L \), which has 2 features that can be plotted in a 2-dimensional space. A machine learning technique for classification can then be used to create decision boundaries objectively between the samples in 2-dimensional space.

3.2.3 Support Vector Machine for Classification

This paper proposes the use of a support vector machine (SVM) for objectively classifying flow regimes in an S-shape riser using 2-dimensional features from the ultrasonic Doppler data.

Cortes and Vapnik, (1995) originally proposed the SVM for binary classification. Given \( N \) data samples of features \( x_i \in \mathbb{R}^M \) each belonging to either of 2 classes, labelled \( y_i \in \{+1,-1\} \), the aim of binary classification is to learn a mapping function that can be used to predict the unknown class of a new sample. SVM solves this by searching for a linear separating hyperplane in the \( M \)-dimensional feature space that maximizes the margin of separation between samples from each opposing class. This separating hyperplane can then serve as a decision boundary between classes. To achieve nonlinear separations, kernels can be used to first transform the original feature space using nonlinear projections, prior to seeking the separating hyperplane (Cristianini and Shawe-Taylor, 2014). The idea of “maximum margin of separation” is the logic offered by the SVM approach that replaces the human subjective approach in flow regime classification. Hence, using SVM, an objective flow regime classifier can be developed.
More specifically, the dual formulation of kernel binary SVM classification is posed as the following convex quadratic programming problem (Cristianini and Shawe-Taylor, 2014):

\[
\begin{align*}
\max & \quad \sum_{i=1}^{N} \alpha_i - \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} y_i y_j \alpha_i \alpha_j K(x_i, x_j) \\
\text{subject to} & \quad \sum_{i=1}^{N} y_i \alpha_i = 0, \\
& \quad 0 \leq \alpha_i \leq C, \quad i = 1, \ldots, N
\end{align*}
\] (16)

where \(x_i \in \mathbb{R}^M, i = 1, 2, \ldots, N\) is the \(N\) training samples with \(M\) features, \(\alpha_i\) are Lagrange multipliers, \(K(\cdot, \cdot)\) is a kernel function, \(y_i \in \{+1, -1\}\) are the known labels for each sample, i.e. positive or negative, and \(C\) is a regularization parameter. To project the data into the kernel feature space, the widely used radial basis kernel function is adopted, given by:

\[
K(x, x') = \exp \left( -\frac{\|x - x'\|^2}{k_w} \right)
\] (17)

where \(k_w\) is the kernel width. The advantage of SVM over other pattern recognition models is that the solution to Eq. (16) is unique and can be calculated efficiently. On the other hand, ANNs require an iterative gradient descent solution, which may converge to local minima. Our application area has no issue with large data sets as well since the number of training samples is only in the order of \(10^2\) and the number of features is in the order of 10. This setting is ideal for an SVM solution. Once the problem in Eq. (16) is solved, the optimal values \(\alpha_i^*\) are obtained, wherein the \(i\)th training samples \(x_i\) that correspond to \(\alpha_i^* > 0\) are deemed as support vectors. Support vectors participate in creating the boundaries between two classes, defined by the decision function:

\[
f(x) = \sum_{i \in SV} y_i \alpha_i^* K(x_i, x) + b^*
\] (18)

where \(SV\) is the set of support vectors and \(b^*\) is a bias term calculated so that \(y_i f(x_i) = 1\) for any \(i\) with \(0 < \alpha_i^* < C\) (Cristianini and Shawe-Taylor, 2014). For any test sample \(x\), the function
$y = \text{sign}(f(x))$ outputs either +1 or -1 to signify if the sample belongs to the positive or the negative class. Accordingly, the exact boundary between the two classes consists of the points $x$ where the SVM decision becomes indifferent, i.e. $\text{sign}(f(x)) = 0$.

In the case of the experiment, samples belong to either of the 4 classes: (1) Bubbly Flow, (2) Slug Flow, (3) Churn Flow, and (4) Annular Flow. Thus, multi-class SVM needs to be implemented. Various strategies for multi-class classification have been proposed, such as one-against-one and one-against-rest to name a few. Here, an efficient one-against-one strategy proposed by Platt et al., (2000) called DAGSVM, is adopted. It has been reported that DAGSVM retains the accuracy offered by other approaches, but is faster to train and evaluate (Platt et al., 2000). Previously, DAGSVM has been adopted in the objective identification of two-phase flow regimes using electrical capacitance data (Wang and Zhang, 2009).

In this work, DAGSVM is employed by training 6 binary classifiers, one for each possible pair of distinct flow regime classes, e.g. 1-vs-2, 1-vs-3, 1-vs-4, 2-vs-3, and so on. Training a binary classifier involves solving for a decision boundary between two classes in the form of Eq. (18). The classifiers are then arranged in a decision directed acyclic graph (DDAG) as shown in Fig. 6. The DDAG structure is key to the efficiency of DAGSVM, which makes it advantageous over other multi-class classification strategies.

![Figure 6: DDAG for Multi-class SVM classification](image)
In the DDAG, any new incoming sample goes through the decision in each node, always starting from the 1-vs-4 node. Each node represents a binary decision as to which class the sample is definitely excluded from, e.g. the 1-vs-4 node classifies the sample as either “Not 1” or “Not 4”. The branch corresponding to the decision of the current SVM classifier is then traversed. As the downward traversal progresses, the sample is continuously being classified at every visited node by eliminating the excluded class, until only a single class is retained. At this point, the bottom of the DDAG is reached and the sample has been definitely associated to a single flow regime. The implementation of DAGSVM used in this work is available online in (Pilario, 2018).

By taking the 2-dimensional data from ultrasound Doppler signals after dimensionality reduction, together with the flow regime labels of each sample, the DAGSVM is used to create exact boundaries between the flow regimes. This completes the virtual flow regime map for use in objective flow regime classification. The summary of the methodology is given in Fig. 7.

![Diagram](image)

**Figure 7:** Proposed methodology for objective flow regime identification

### 4 Results and Discussions

Flow regime data samples were acquired experimentally from the S-shape riser system described in Section 3.1, and preliminary results are already shown in Fig. 5. In this section, we proceed with the proposed approach for data analysis and discussion of the results.
4.1 PCA Visualization

Figure 8 shows the resulting 2D visualisation of the ultrasound Doppler data for each training sample after applying PCA. The benefit of PCA visualization can be demonstrated by establishing the relationship between Fig. 8 and Fig. 4. These figures are similar in that they both represent a map where every point location is associated to a distinct gas-liquid flow rate value pair.

In Fig. 8, Annular Flow samples (high gas flow rate and low liquid flow rate) are found at the lower left corner of the map, while Bubbly Flow samples (low gas flow rate and high liquid flow rate) are found at the right and upper right corners of the PCA map. On the other hand, the Slug Flow and Churn Flow samples are found in a specific order in the middle region. The direction of increasing gas flow rate can be elucidated from right to left in the PCA map, while the direction of increasing liquid flow rate results from bottom to top. These directions correspond to the axes of the flow regime map in Fig. 4. Because of this relationship, it can be said that PCA was able to discover the gas-liquid flow rate information of every sample using only the PSD features obtained from the ultrasound Doppler experiment. Thus, PCA can arrange the Doppler data meaningfully in 2D space, further enabling the construction of a virtual flow regime map.

However, it can be noticed that there is no clear gap or boundary between the samples from different flow regimes in the PCA map. By conferring with Fig. 4, it was found that these samples lie mostly on the transition regions. Hence, a soft margin SVM can be used to establish the boundary between the various flow regimes, by setting the value of $C$ to be less than $\infty$. By further varying the SVM parameters, $k_w$ and $C$, one can control the complexity of the boundaries between flow regimes. This investigation is carried out in Section 4.2.
Another benefit of PCA visualization of data is the detection of outliers. The consistency of the human expert in labelling flow regimes may be impeded by certain factors, leading to the presence of outlier data samples. One obvious case is the sample at 10 Sm$^3$/hr air flow rate and 3.5 kg/s water flow rate, which was observed to exhibit churn flow (see Fig. 4), yet is found between bubbly and slug flow regime samples. In the PCA visualization of ultrasound Doppler data (see Fig. 8), this specific data point lies at the position near (4.0, -1.0) in the 2D map, also between bubbly and slug flow samples. Hence, this data point is considered to be an outlier. Other outliers confirmed in the same way in our training dataset include those at air-water flow rates of (200 Sm$^3$/h, 4.5 kg/s) and (10 Sm$^3$/h, 2.5 kg/s). Ultimately, the degree to which these outliers are tolerated by the subsequent SVM classification is dictated by setting appropriate parameters of $k_w$ and $C$.

4.2 SVM classification

In Figure 9, a sample of flow regime map for $k_w = 7$ and $C = 100$ where the samples of both the training and test data are superimposed. In this map, the background colours denote the results from the SVM classification, e.g. SVM identified the Slug Flow regime for every point location in the L-shaped region between Bubbly and Churn Flow regime. Superimposed in this map are
the training data samples (circles) and test data samples (triangles). By noting the mismatch between the sample colours and background colours, the training and test data classification accuracies are found to be 85.7% and 84.6% respectively. Without counting the confirmed outliers in the training samples, the accuracy in the training data is 88.6%. These results depict the capability of the SVM approach for objective classification of two-phase flow regime based on Doppler ultrasound data.

Figure 9: Virtual flow regime map using SVM at $k_w = 7$ and $C = 100$. The background colours denote the SVM identification results. A mismatched sample colour and background colour indicates misclassification. Legend: Circles – training samples; triangles – test samples

For completeness, a case of empty pipe was included in the test samples. Interestingly, this sample was identified as churn flow by the SVM. Although this result does not make sense, the fact that the PCA mapping placed the empty-pipe ultrasound Doppler signal data at the bottom of the map validates that the direction of increasing liquid flow rate occurs upward in the PCA visualization.

4.3 SVM Performance at Different Parameters

The list of misclassified samples in Fig. 9 is presented in Table 1. Some disparities in using the proposed identification method were observed. In particular, the objective classifier identifies some Slug Flow samples as Churn Flows samples. This misclassification is related to the parameter choice issues in the SVM objective classifier. Various settings for $k_w$ and $C$ gives
varying classification performance. The SVM accuracy over a grid of parameter values, such as $k_w \in \{1,3,...,9\}$ and $C \in \{1,10,...,10^4\}$, is presented in Fig. 10.

### Table 2: List of Misclassified Samples in Fig. 9

<table>
<thead>
<tr>
<th>Misclassified Training Samples (13 out of 91)</th>
<th>Vsg (Sm$^3$/h)</th>
<th>Vsl (kg/s)</th>
<th>SVM Classification</th>
<th>Actual Classification</th>
<th>Outlier?</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>2.5</td>
<td>Slug Flow</td>
<td>Bubbly Flow</td>
<td>Y</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>3.5</td>
<td>Bubbly Flow</td>
<td>Churn Flow</td>
<td>Y</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>2</td>
<td>Churn Flow</td>
<td>Slug Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>4</td>
<td>Slug Flow</td>
<td>Bubbly Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>30</td>
<td>4</td>
<td>Bubbly Flow</td>
<td>Slug Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>2</td>
<td>Churn Flow</td>
<td>Slug Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>3</td>
<td>Churn Flow</td>
<td>Slug Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>4.5</td>
<td>Bubbly Flow</td>
<td>Slug Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>120</td>
<td>1</td>
<td>Annular Flow</td>
<td>Churn Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>120</td>
<td>4</td>
<td>Slug Flow</td>
<td>Churn Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>200</td>
<td>4.5</td>
<td>Slug Flow</td>
<td>Bubbly Flow</td>
<td>Y</td>
<td></td>
</tr>
<tr>
<td>300</td>
<td>0.1</td>
<td>Churn Flow</td>
<td>Annular Flow</td>
<td>N</td>
<td></td>
</tr>
<tr>
<td>300</td>
<td>1.5</td>
<td>Churn Flow</td>
<td>Annular Flow</td>
<td>N</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Misclassified Test Samples (6 out of 39)</th>
<th>Vsg (Sm$^3$/h)</th>
<th>Vsl (kg/s)</th>
<th>SVM Classification</th>
<th>Actual Classification</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>0.5</td>
<td>Churn Flow</td>
<td>Slag Flow</td>
<td></td>
</tr>
<tr>
<td>20</td>
<td>0.5</td>
<td>Churn Flow</td>
<td>Slag Flow</td>
<td></td>
</tr>
<tr>
<td>30</td>
<td>2</td>
<td>Churn Flow</td>
<td>Slag Flow</td>
<td></td>
</tr>
<tr>
<td>50</td>
<td>0.1</td>
<td>Churn Flow</td>
<td>Slag Flow</td>
<td></td>
</tr>
<tr>
<td>300</td>
<td>0.5</td>
<td>Churn Flow</td>
<td>Annular Flow</td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>Churn Flow</td>
<td>Empty Pipe</td>
<td></td>
</tr>
</tbody>
</table>

Indeed, accurate classification of training data can be acquired by adjusting $k_w$ and $C$ towards the direction of overfitting (lower $k_w$ and higher $C$). However, overfitting shows poor generalisation to unseen test data. Concisely, overfitting makes the classification biased towards the training samples. On the other hand, at high $k_w$ and low $C$, under-fitting occurs. In the case of underfitting, the boundaries tend towards linearity at the expense of higher misclassification rates. In general, the only way to increase the level of confidence with the resulting flow regime map is to validate it against numerous unseen test data samples as possible. With only the available data, the choice of $k_w = 7$ and $C = 100$ already gives useful results for objective flow regime classification, while striking a balance between overfitting and underfitting.
With the virtual flow regime map at hand, further analysis on the flow regime transitions and uncertainties can be performed. More importantly, online objective flow regime identification can be developed from the proposed approach in this work. Using a continuous feed of ultrasound Doppler-based flow velocity information, PCA-SVM can automatically visualize the frequency-domain features and classify the flow regime at every sampling instant. Hence, the proposed approach has a broad potential for industrial applications.

5 Conclusion and future works

In this paper, the necessity of objective, non-invasive and non-intrusive measurement methods for flow regime identification in industrial practice is highlighted. Specifically, this work proposed the use of non-invasive clamp-on continuous wave ultrasound Doppler (CWUD) and machine learning approaches for objective two-phase gas/liquid flow regime identification. From the ultrasonic signals, Power Spectral Density (PSD) features were extracted and subjected to principal components analysis (PCA) for projecting the data in 2-dimensional space. A multi-class support vector machine (SVM) classifier is trained to establish exact boundaries between the flow regimes in the reduced data space. In the end, the objective classifier accuracy for both the training and testing data samples were 85.7% and 84.6% respectively. More importantly, the generation of virtual flow regime maps enabled useful data visualizations of the Doppler signals, which can aid in detecting outliers and explain the decisions made by the SVM classifier. These results justify the suitability of our approach for flow regime identification in industrial practice.
To improve this work, the proposed approach must be tested against many other test rigs and configurations to see if the generated virtual flow regime maps are indeed capable of visualizing flow regime patterns from the CWUD data. In addition, the feature extraction and dimensionality reduction steps are deemed most important in the entire procedure. Many other techniques for these steps must be tested to see if a clear separation can be produced between various samples from different flow regimes.

Further research can also be made in applying the proposed approach for examining two-phase water-oil flow, mostly to address the necessity of clamp-on non-invasive ultrasonic flow monitoring for oil well testing.

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References


