# LOSS COVERAGE IN INSURANCE MARKETS: WHY ADVERSE SELECTION IS NOT ALWAYS A BAD THING

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IAA COLLOQUIUM IN OSLO

# Acknowledgement

## Bursary from

- IAA-International Actuarial Association
- The Colloquium



- Background
  - How does insurance work?
  - Risk classification Scheme

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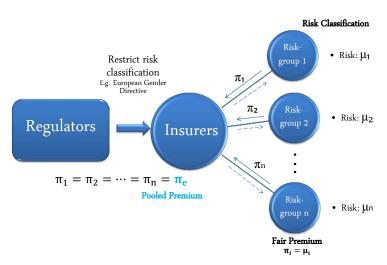


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# Background

How insurance works and risk classification scheme



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•  $0, \pi_1, \pi_2, \pi_3, \pi_e, ..., \pi_7, \pi_8, ..., \pi_n, 1.$ 

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# Typical definition

Purchasing decision is positively correlated with losses

-Chiappori and Salanie (2000) "Positive Correlation Test"

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	- · · · · · · · · · · · · · · · · · · ·	
Life Insurance	Cawley and Philipson (1999)	Χ
Auto Insurance	Chiappori and Salanie (2000)	X
	Cohen (2005)	0
Annuity	Finkelstein and Poterba (2004)	0
Health Insurance	Cardon and Hendel (2001)	X

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Adverse Selection (AS) = 
$$\frac{\text{expected claim per policy}}{\text{expected loss per risk}} = \frac{E[QL]}{E[Q]E[L]}$$
, (1)

where Q: quantity of insurance; L: risk experience.

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Adverse Selection Ratio: 
$$S = \frac{AS \text{ at pooled premium } \pi_e}{AS \text{ at risk-differentiated premiums}}$$
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>  $1 \Rightarrow \text{Adverse Selection}$ .

# Example

- A population of 1000
- Two risk groups
  - 200 high risks with risk 0.04
  - 800 low risks with risk 0.01
- No moral hazard

Full risk classification



#### Full risk classification

	Low risks	High risks	Aggregate
Risk	0.01	0.04	0.016
Total population	800	200	1000
Expected population losses	8	8	16
Break-even premiums (differentiated)	0.01	0.04	0.016
Numbers insured	400	100	500
Adverse Selection Ratio (S)			1

#### Full risk classification

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No adverse selection.



Restriction on risk classification-Case 1



#### Restriction on risk classification-Case 1

	Low risks	High risks	Aggregate
Risk	0.01	0.04	0.016
Total population	800	200	1000
Expected population losses	8	8	16
Break-even premiums (pooled)	0.02	0.02	0.02
Numbers insured	300(400)	150(100)	450(500)
Adverse Selection Ratio (S)			1.25>1

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	Low risks	High risks	Aggregate
Risk	0.01	0.04	0.016
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Numbers insured	300(400)	150(100)	450(500)
Adverse Selection Ratio (S)			1.25>1

Moderate adverse selection

Restriction on risk classification-Case 2



#### Restriction on risk classification-Case 2

	Low risks	High risks	Aggregate
Risk	0.01	0.04	0.016
Total population	800	200	1000
Expected population losses	8	8	16
Break-even premiums (pooled)	0.02154	0.02154	0.02154
Numbers insured	200(400)	125(100)	325(500)
Adverse Selection Ratio (S)			1.3462>1

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	Low risks	High risks	Aggregate
Risk	0.01	0.04	0.016
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Heavier adverse selection

Adverse selection suggests pooling is always bad. But is it?

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# Loss Coverage

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Loss Coverage (LC) = 
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#### Definition

Loss Coverage (LC) = 
$$\frac{\text{insured expected losses}}{\text{population expected losses}}$$
Loss Coverage Ratio:  $C = \frac{\text{LC at a pooled premium } \pi_e}{\text{LC at at risk-differentiated premium } \pi_i}$  (4) > 1, Favorable!

No restriction on risk classification



#### No restriction on risk classification

	Low risks	High risks	Aggregate
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Total population	800	200	1000
Expected population losses	8	8	16
Break-even premiums (differentiated)	0.01	0.04	0.016
Numbers insured	400	100	500
Insured losses	4	4	8
Loss coverage ratio (C)			1

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Numbers insured	400	100	500
Insured losses	4	4	8
Loss coverage ratio (C)			1

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Numbers insured	300(400)	150(100)	450(500)
Insured losses	3	6	9
Loss coverage ratio (C)			1.125>1

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(pooled)	0.02	0.02	0.02
Numbers insured	300(400)	150(100)	450(500)
Insured losses	3	6	9
Loss coverage ratio (C)			1.125>1

Moderate adverse selection (S = 1.25) but favorable loss coverage.

Restriction on risk classification-Case 2



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Heavier adverse selection (S = 1.3462) and worse loss coverage. Loss coverage might be a better measure!

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### **Definition**

 $d(\mu,\pi)$ : the proportional demand for insurance for risk  $\mu$  at premium  $\pi$ .

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### **Definition**

Demand elasticity:  $\epsilon(\mu,\pi) = -\frac{\partial d(\mu,\pi)}{d(\mu,\pi)}/\frac{\partial \pi}{\pi}$  i.e. sensitivity of demand to premium changes.

### Iso-elastic demand function

$$\epsilon(\mu, \pi) = \lambda$$
, i.e. constant (5)

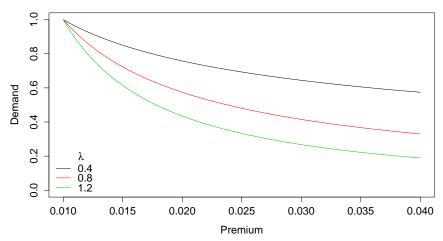
#### Iso-elastic demand function

$$\epsilon(\mu, \pi) = \lambda$$
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$$d(\mu, \pi) = \tau \left\lceil \frac{\pi}{\mu} \right\rceil^{-\lambda}.$$
 (6)

### Iso-elastic demand function

 $\tau = 1, \mu = 0.01, \lambda = 0.4, 0.8$  and 1.2



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$$d(\mu_i, \pi_e) = \tau_i \left[\frac{\pi_e}{\mu_i}\right]^{-\lambda_i}, i = 1, 2$$

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If 
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,

$$\pi_{e} = \frac{\alpha_{1}\mu_{1}^{\lambda+1} + \alpha_{2}\mu_{2}^{\lambda+1}}{\alpha_{1}\mu_{1}^{\lambda} + \alpha_{2}\mu_{2}^{\lambda}},\tag{8}$$

where

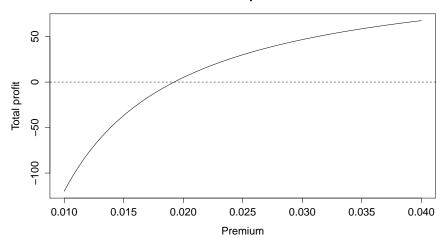
$$\alpha_i = \frac{\tau_i \mathbf{p}_i}{\tau_1 \mathbf{p}_1 + \tau_2 \mathbf{p}_2}, i = 1, 2 \tag{9}$$

(Fair-premium demand-share)

# Unique equilibrium premium

$$p_1 = 9000, \tau_1 = 1, \mu_1 = 0.01; p_2 = 1000, \tau_2 = 1, \mu_2 = 0.04, \lambda_1 = \lambda_2 = 1$$

#### Profit plot



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### Results on adverse selection

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#### Adverse Selection Ratio

$$S = \frac{\pi_{\theta}}{\alpha_1 \mu_1 + \alpha_2 \mu_2}.\tag{10}$$

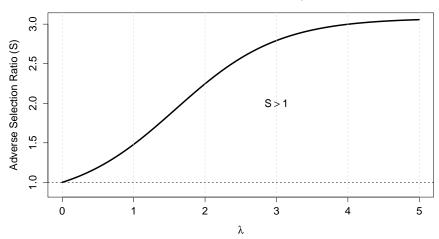
$$\alpha_i = \frac{\tau_i \rho_i}{\tau_1 \rho_1 + \tau_2 \rho_2}, i = 1, 2$$

(Fair-premium demand-share)

## Results: Adverse Selection Ratio (S)

$$p_1 = 9000, \tau_1 = 1, \mu_1 = 0.01; p_2 = 1000, \tau_2 = 1, \mu_2 = 0.04$$

#### Adverse selection ratio plot



## Results on loss coverage

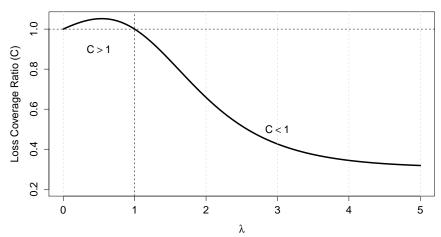
### Loss Coverage Ratio

$$C = \frac{1}{\pi_e^{\lambda}} \frac{\alpha_1 \mu_1^{\lambda+1} + \alpha_2 \mu_2^{\lambda+1}}{\alpha_1 \mu_1 + \alpha_2 \mu_2}.$$
 (11)

# Results: Loss Coverage Ratio (C)

$$p_1 = 9000, \tau_1 = 1, \mu_1 = 0.01; p_2 = 1000, \tau_2 = 1, \mu_2 = 0.04$$

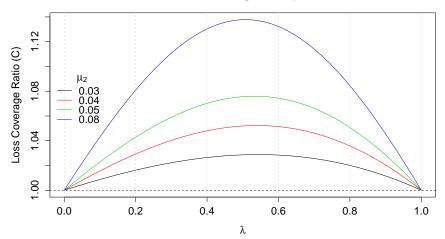
#### Loss coverage ratio plot



# Results: Loss Coverage Ratio (C)

 $p_1 = 9000, \tau_1 = 1, \mu_1 = 0.01; p_2 = 1000, \tau_2 = 1, \mu_2 = 0.03, 0.04, 0.05, 0.08$ 

#### Loss coverage ratio plot



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- When there is restriction on risk classification, a pooled premium  $\pi_e$  is charged across all risk-groups.
- There will always be adverse selection ⇒ Adverse selection may not be a good measure.
- Loss coverage is an alternative metric.
- Adverse selection is not always a bad thing!
   A moderate level of adverse selection can increase loss coverage.

#### Further Research

- Other/more general demand e.g.  $d(\mu, \pi) = \tau e^{1-(\frac{\pi}{\mu})^{\lambda}}$ .
- Loose restriction on demand elasticities.
- Partial restriction on risk classification.

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### Questions?

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Thank you!

