

Title: Combustion behavior profiling of single pulverized coal particles in a drop tube furnace through high-speed imaging and image analysis

Authors: Xiaojing Bai^{1, 2},
Gang Lu^{2*},
Tom Bennet³,
Archi Sarroza³,
Carol Eastwick³,
Hao Liu^{3*},
Yong Yan²

Address: ¹ School of Control and Computer Engineering, North China Electric Power University,
Beijing, 102206, China

² School of Engineering and Digital Arts, University of Kent, Canterbury,
Kent CT2 7NT, UK

³ Faculty of Engineering, University of Nottingham, University Park,
Nottingham, NG7 2RD, UK

E-mails: xb9@kent.ac.uk, g.lu@kent.ac.uk, tombennet@gmail.com, liu.hao@nottingham.ac.uk,
carol.eastwick@nottingham.ac.uk, y.yan@kent.ac.uk

* Corresponding authors, Tel: 00441227823706 (G. Lu), 00441158467674 (H. Liu),
Fax: 00441227456084 (G. Lu), 00441159513159 (H. Liu)

ABSTRACT

1
2 Experimental investigations into the combustion behaviors of single pulverized coal particles are
3 carried out based on high-speed imaging and image processing techniques. A high-speed video
4 camera is employed to acquire the images of coal particles during their residence time in a visual
5 drop tube furnace. Computer algorithms are developed to determine the characteristic parameters
6 of the particles from the images extracted from the videos obtained. The parameters are used to
7 quantify the combustion behaviors of the burning particle in terms of its size, shape, surface
8 roughness, rotation frequency and luminosity. Two sets of samples of the same coal with
9 different particle sizes are studied using the techniques developed. Experimental results show that
10 the coal with different particle sizes exhibits distinctly different combustion behaviors. In
11 particular, for the large coal particle (150-212 μm), the combustion of volatiles and char takes
12 place sequentially with clear fragmentation at the early stage of the char combustion. For the
13 small coal particle (106-150 μm), however, the combustion of volatiles and char occurs
14 simultaneously with no clear fragmentation. The size of the two burning particles shows a
15 decreasing trend with periodic variation attributed to the rapid rotations of the particles. The
16 small particle rotates at a frequency of around 30 Hz, in comparison to 20 Hz for the large
17 particle due to a greater combustion rate. The luminous intensity of the large particle shows two
18 peaks, which is attributed to the sequential combustion of volatiles and char. The luminous
19 intensity of the small particle illustrates a monotonously decreasing trend, suggesting again a
20 simultaneous devolatilization/volatile and char combustion.

21
22 **Keywords**– pulverized coal particles; drop tube furnace; high-speed imaging; image processing;
23 combustion behaviors

24

I. INTRODUCTION

25

26

27 Although renewable energy has been attracting much attention in recent years due to
28 environmental concerns, conventional fuels such as pulverized coal will remain to be a major
29 energy resource for years to come worldwide due to their wide availability and competitively low
30 cost, particularly with the development of new combustion technologies such as co-firing coal and
31 biomass and oxy-coal combustion [1]. Whilst the effects of chemical composition and other fuel
32 properties of coal on combustion have been widely studied, the physical characteristics of a
33 pulverized solid fuel, such as particle size, shape, and etc. have also been found to have a
34 significant impact on the ignition and combustion behaviors of fuel particles, and consequently the
35 flame stability, combustion efficiency and pollutant emissions [2]. The combustion process of
36 solid fuel particles comprises typically three stages, i.e., heating, volatilization/devolatilization,
37 and char oxidization [3]. Depending upon not only the fuel properties, but also the heating rate,
38 particle size, combustion environments (temperature and stoichiometry etc.) and the volatile
39 matter evolution, the homogeneous ignition and heterogeneous ignition of fuel particles may occur
40 sequentially or simultaneously [4]. This makes it more difficult to characterize the combustion
41 behaviors of fuel particles. Therefore, the measurement and characterization of individual fuel
42 particles are required to explore the insight into the combustion mechanism of fuel particles, and
43 consequently advance the knowledge to optimize combustion processes and validate
44 computational modeling results.

45

46 There is a range of experimental and modeling work that has been carried out to investigate the
47 combustion behaviors of coal and biomass fuel particles of different ranks and sizes under
48 different combustion conditions in drop tube furnaces (DTFs) using non-visualized and visualized
49 technical approaches [5-11]. For instance, Wang et al. [12] investigated the combustion behaviors
50 and ash characteristics of coal and biomass particles through analyzing the particles sampled from

51 different heights of the DTF using X-ray fluorescence spectroscopy and a particle size analyzer.
52 Costa et al. [13] evaluated the gas temperature, particle burnout and particle fragmentation of raw
53 and torrefied pine shells and olive stones in a DTF using various instruments (e.g., a low pressure
54 three-stage cascade impactor, a particle size analyzer and a scanning electron microscope). Pereira
55 et al. [14] studied the kinetics of poplar short rotation coppice in a DTF through thermogravimetric
56 analysis. The above investigations are based on non-visualized technical approaches. With the
57 advent of high-speed digital imaging and image processing techniques, the visualization and
58 characteristics of burning particles have become feasible. Simões et al. [11] investigated the
59 ignition mode and delay time of biomass fuels through the analysis of particle images from a high-
60 speed camera. The impact of gas temperature and oxygen concentration on the ignition mode and
61 ignition delay time was assessed. Shaddix et al. [15] analyzed the ignition and devolatilization
62 characteristics of both high-volatile bituminous and subbituminous coal particles through single-
63 particle imaging in both N₂ and CO₂ diluent gasses. Kim et al. [16] investigated the ignition
64 behaviors of coal particles under high heating-rate conditions using a flat flame burner and particle
65 images. Levendis et al. [4, 17] and Riaza et al. [1] employed three-color pyrometry and high-speed
66 high-resolution cinematography to study the combustion behaviors of single coal particles in both
67 air and simulated oxy-fuel environments. Kosher et al. [18] also studied the combustion
68 characteristics of individual coal particles in an oxygen-enriched environment using high-speed
69 OH-PLIF (Planar Laser-induced Fluorescence).

70

71 Although certain progress on the characterization of burning particles using visualized approaches
72 has been made, a few studies have been undertaken on the quantitative profiling of single fuel
73 particles. Podczec [19] proposed a shape factor, which used the deviations of the 2-D (two-
74 dimensional) particle outlines from the images of a circle, triangle and square, for the particle
75 analysis . Gao et al. [20] conducted the on-line measurement of particle size and shape and their

76 distributions through image processing, where the images of particle were acquired from a color
77 CCD camera coupled with multi-wavelength laser sources. Carter et al. [21] and Qian et al. [22]
78 combined digital imaging and electrostatic sensors to obtain the size distribution and volumetric
79 concentration of particles in pneumatic conveying pipes. It is clear that, whilst the combustion
80 behaviors of fuel particles influence the overall performance of a combustion process, limited
81 studies have been carried out to investigate the combustion behaviors of burning particles through
82 the measurement of physical characteristics such as size, shape, surface roughness, rotational
83 frequency and luminosity.

84

85 This paper presents experimental investigations into the combustion behaviors of individual coal
86 particles with the aim to providing a quantitative description of particle dynamics during
87 combustion through high-speed imaging and digital image processing. The videos of two sets of
88 individual coal particles were recorded using a high-speed camera during the combustion process
89 in a visual drop tube furnace (V-DTF). Algorithms are developed to acquire and process the
90 particle images in terms of physical quantities, including size, shape, surface roughness, rotation
91 and luminosity. These quantities are then used to describe the characteristics of the burning
92 particles during their residence time in the furnace.

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II. MATERIALS AND METHODS

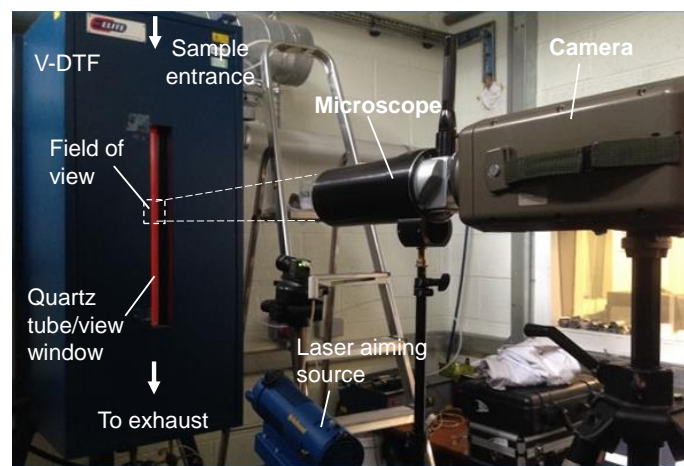
95

96 *A. V-DTF and high-speed camera*

97 DTFs have been widely used for combustion research as they can provide critical data for the in-
98 depth understanding of ignition and combustion behaviors of fuel particles in power plant boilers
99 [23]. The tiny size, short residence time of the particles and the variations of the size and shape
100 make it very difficult to visualize and characterize the burning particles. With the aid of high-
101 speed imaging, it is possible to visualize burning particles in a DTF. Fig. 1 is the overview of the

102 experimental setup in this study. The V-DTF used in this study is an electrically heated drop tube
103 furnace equipped with a 1400 mm long quartz tube with an inner diameter of 50 mm, capable of
104 maintaining gas temperatures up to 1050°C within the 1000 mm-long heated zone [24, 25]. The
105 quartz work tube is insulated by a spun ceramic fiber blanket to minimize the heat loss during
106 experimentation. The fuel particles are injected into the quartz tube from the water-cooled feed
107 probe mounted at the top of the quartz tube. The particles are heated, ignited and combusted in the
108 furnace with the residual ash being vacuumed away or collected with the collection probe mounted
109 at the bottom end of the quartz tube. There is a long and narrow viewing window at the front side
110 of the furnace which allows a camera system to access and view the combustion process of the
111 fuel particles inside the quartz tube.

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113

114

Fig. 1. Overview of the experimental setup.

115

116 A high-speed camera (Phantom v12.1), capable of recording a video at a frame rate up to
117 1,000,000 fps (frames per second), acquires videos of burning coal particles. A long-distance
118 microscope (Questar QM-1, which has a 56 cm to 152 cm working distance, a 30 to 1 variability
119 in the field of view and a resolution better than 3 microns at 56 cm) is coupled with the camera to
120 ensure that coal particles can be captured during their residence time in the furnace. The resulting
121 field of view is around 8 mm × 8 mm.

122

123 *B. Coal properties and test conditions*

124

125 Two sets of coal sample with different particle sizes (Particles A and B) were prepared from the
126 same batch of Colombian bituminous coal (El Cerrejon, which was sourced directly from a UK
127 power plant). Each sample was separately dried, sieved with particle size ranging from 150-212
128 μm for Particle A, and 106-150 μm for Particle B. The proximate and ultimate analyses of the
129 samples are summarized in Table 1. In the test, a small amount (in milligrams) of the sieved coal
130 particles were dropped manually through the feed probe into the quartz tube which was pre-
131 heated to 800°C and supplied with air at a rate of 5 l/min. The high-speed camera tracked and
132 took the videos of the particles at a frame rate of 6200 fps during their residence time in the
133 quartz tube.

134

135 Table 1. Proximate and ultimate analyses* of El Cerrejon

136 (* BS ISO 17246:2010 and BS ISO 17247:2013)

Proximate analysis (% , as received)		Ultimate analysis (% , dry basis)	
Moisture	2.3	Carbon	72.2
Volatile matter	36.6	Hydrogen	4.8
Fixed carbon	51.4	Oxygen	9.1
Ash	9.7	Nitrogen	1.5
		Sulphur	2.4
High heating value: MJ/kg (dry basis)		29.6	

137

138

139

140 *C. Contour detection and extraction*

141 Once the videos were recorded, individual images of a particle were read frame by frame in a
142 computer. Image progressing algorithms were then developed to process the images. Detecting the
143 particle contour is the initial step in the image processing. The Otsu's method [26] was used to
144 automatically segment the images. The Otsu's method calculates the optimum threshold separating
145 the histogram of an image into two pixel groups (i.e., foreground and background groups) and
146 ensures that the intra-class variance is minimal or equivalent. Once the threshold is determined,
147 the binary format of the image is generated, which allows the particle contour retrieval is to be
148 performed. The 8-connectivity, which traces neighbors to every pixel that touches one of their
149 edges [20], is then used to extract the contour of the particle's binary image. These pixels are
150 connected horizontally, vertically, and diagonally. The 8-connectivity can be described as,

151
$$\max(|x' - x''|, |y' - y''|) = 1, \quad (1)$$

152 where (x', y') and (x'', y'') are a pair of pixels in the image. Once the particle contour is
153 determined, a set of characteristic parameters, which describe the particle size, shape, surface
154 roughness, rotation and luminosity, are computed.

155

156 *D. Characteristic parameters*

157

158 *a) Size and shape*

159 Two parameters, i.e., *Area* and *Aspect ratio*, are defined to describe the size and shape of the
160 particle.

161

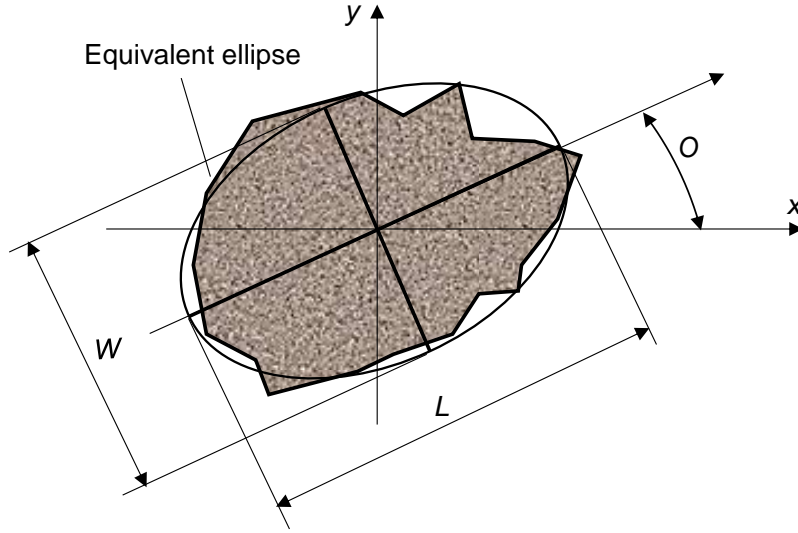
162 *Area (A)*- The Area is the quantity representing the particle size. *A* is determined by counting
163 the pixel number within the particle contour, *R*, i.e.,

164
$$A = \sum_{(i,j) \in R} 1. \quad (2)$$

165 *Aspect ratio (R_a)*- The Aspect ratio is the ratio of the major axis to the minor axis of the
 166 equivalent ellipse of a particle [27], and is calculated as,

167
$$R_a = \frac{L}{W}, \quad (3)$$

168 where L and W are the lengths of the major and minor axes, respectively, as shown in Fig. 2. For a
 169 circle, R_a is 1. The larger the R_a , the more elongated the particle.



170
 171 Fig. 2. A particle and its equivalent ellipse.

172
 173 *b). Surface roughness*

174 Two parameters, *Boundary distance* and *Boundary variance index*, are computed for quantifying
 175 the surface roughness of the particle.

176
 177 *Boundary distance [$r(k)$]*- The Boundary distance is the distance between a point (x_k, y_k) on
 178 the boundary and the center (x_c, y_c) of the particle, i.e.,

179
$$r(k) = \sqrt{(x_k - x_c)^2 + (y_k - y_c)^2}, \quad (4)$$

180 where, $k=0, 1, 2, \dots, N-1$, N is the number of the boundary points, and, in this study, $N=128$.

181

182 By using (4), the boundary of the particle is transformed into a one-dimensional ‘signal’ in the
 183 spatial domain and thus the discrete Fourier transform (DFT) is performed over $r(k)$ [28], i.e.,

$$184 \quad F(n) = \frac{1}{N} \sum_{k=0}^{N-1} r(k) e^{-j2\pi nk/N}, \quad (5)$$

185 where, $n=0, 1, 2, \dots, N-1$. Once the DFT form of the boundary distance is obtained, the variance of
 186 the boundary is determined.

187

188 *Boundary variance index-* The Boundary variance index, $DF=[DF_1, DF_2, \dots, DF_{N/2}]$, is the
 189 ratio of the absolute values of $F(n)$ ($n=1, 2, \dots, N/2$) to the absolute value of the *DC (Direct*
 190 *Current)* component $|F(0)|$, i.e.,

$$191 \quad DF_n = \frac{|F(n)|}{|F(0)|}, \quad (6)$$

192 where $|F(0)|$ is the average of the boundary distance [29]. The variance of the DF represents the
 193 variance of the boundary in different scales. The rougher the boundary, the greater the DF .

194

195 c). Rotation

196 Previous studies revealed that coal particles rotate rapidly during combustion due to volatile
 197 releases and/or the intensive exothermic combustion reactions [30]. The rotation of a particle can
 198 be quantified through the computation of the change in particle orientation during its residence
 199 time in the furnace. High-speed imaging has made it possible to derive parameters relating to the
 200 motion of the particles such as orientation and rotational frequency. The orientation, O , is counted
 201 as the angle between the major axis and the x-axis of the equivalent ellipse of the particle, i.e. [31],

$$202 \quad O = \arctan \left(\frac{\left| \sum_{i \in R} x_i^2 - \sum_{i \in R} y_i^2 \right| + \sqrt{\left(\sum_{i \in R} x_i^2 - \sum_{i \in R} y_i^2 \right)^2 + 4 \left(\sum_i x_i y_i \right)^2}}{2 \sum_i x_i y_i} \right), \quad (7)$$

203 where (x_i, y_i) are the coordinates of pixel i within the equivalent ellipse. Rotation index of the
 204 particle, R_{ind} , is then defined as,

$$205 \quad R_{ind} = \pm \sin(O) . \quad (8)$$

206 R_{ind} ranges from -1 to 1, where $R_{ind}=1$ stands for 90° and $R_{ind}=-1$ stands for 270° . Note that the
 207 sign is dependent upon the orientation of the particle computed from the former image frame and
 208 the initial sign is defined as positive.

209

210 *d). Luminosity*

211 The luminous intensity of a burning coal particle is highly related to its surface temperature [21].
 212 In general, a higher luminous intensity entails a higher surface temperature [7]. The normalized
 213 luminous intensity, G , is the averaged grey-level intensity of the particle image normalized to the
 214 maximum grey-level of the image (255 in this study), i.e.,

$$215 \quad G = \frac{\sum_{(i,j) \in R} I_{i,j}}{255A} \times 100\% , \quad (9)$$

216 where I_{ij} is the gray-level of the image at pixel (i, j) and A is the area defined in (2).

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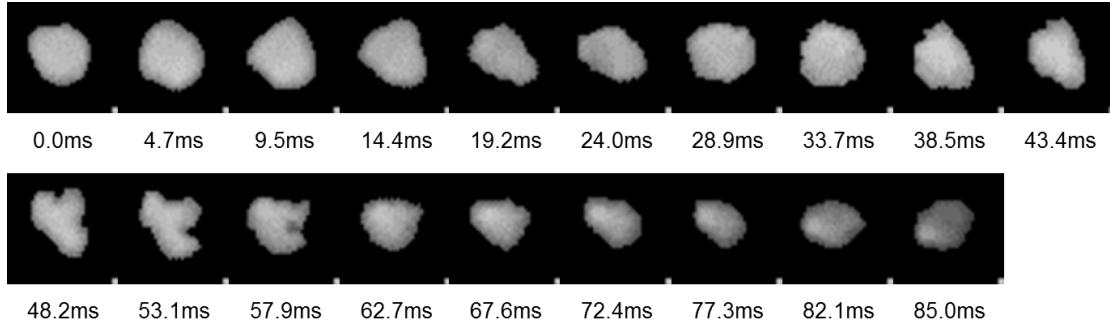
III. EXPERIMENTAL RESULTS

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221 Fig. 3 shows the example images of the coal particles captured by the camera system. The sample
 222 images provide visualized information associated with the combustion behaviors of the two
 223 particles. It should be noted that, by the time when the particle was captured by the camera, it had
 224 been in the quartz tube for some time, and thus each image frame does not represent the absolute
 225 residence time of the particle in the quartz tube, but the relative residence time between frames,
 226 e.g., two successive frames represent a relative residence time of 0.2 ms. The combustion of
 227 volatiles and char including fragmentation of the particles were clearly observed from the images.

228 As expected, the combustion behaviors of the particles varied significantly in their residence time.
229 The quantification of such variations was performed in terms of the characteristic parameters
230 defined in Section II.

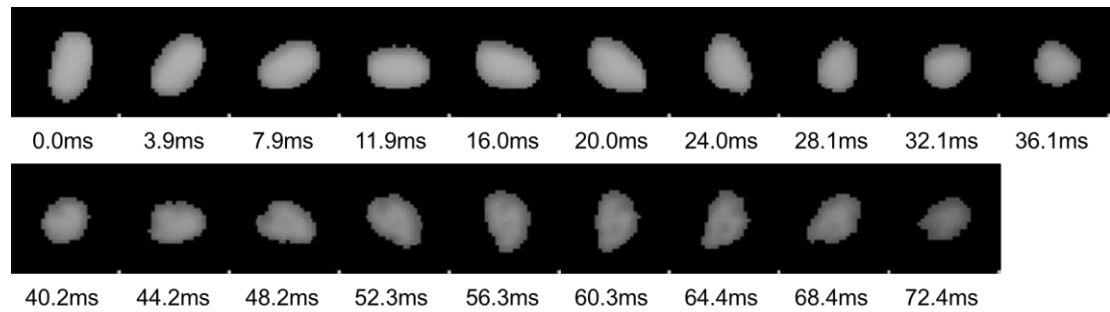
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(a) Particle A (150-212 μm).



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(b) Particle B (106-150 μm).

236 Fig. 3. Example images of coal particles by frames and relative time.

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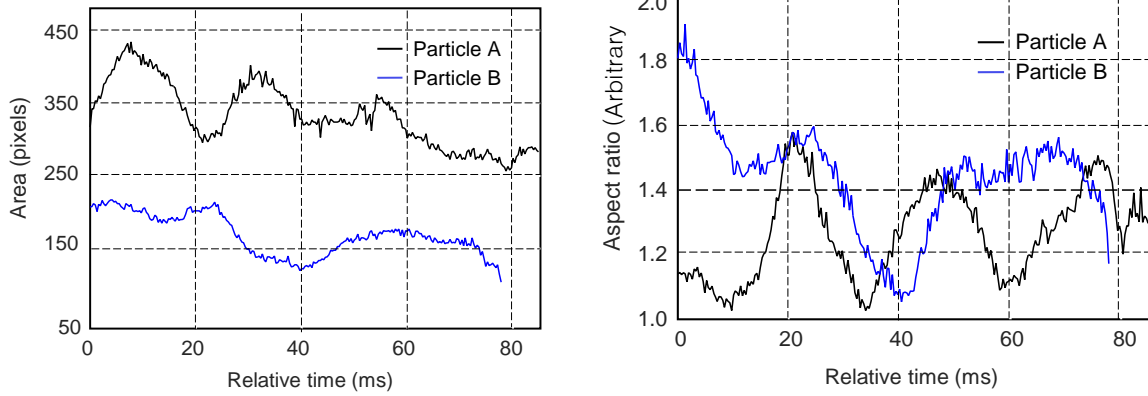
238 A. Size and shape characteristics

239 Fig. 4(a) shows the area variation of the coal particles during their residence time in the quartz
240 tube. A decreasing trend is evident for both Particles A and B due to the mass loss of the particles
241 during combustion. The periodic variation of the particle area is believed to be due to the rotation
242 of the particle in the line-of-sight direction of the camera system. It is also observed that the
243 combustion behaviors of the two particles differ due to their different sizes. For instance, for
244 Particle A, the devolatilization/volatile combustion dominated before about 20 ms. It is evident
245 that the boundaries of the particle were clear and smooth [refer to Fig. 3(a), and also the later

246 section about the surface roughness]. It is observed in the video [refer to Fig. 3(a)] that the
247 fragmentation of the particle started from about 20 ms, and the significant char combustion began
248 around 40 ms. These are also evident in Figs.4(a) and 4(b) where the area and shape of the
249 particle show great fluctuations in the period from 20–40 ms. The single-phase char combustion
250 began around 60 ms [refer to Fig. 3(a)], toward to the completion of combustion. For Particle B,
251 as it is relatively small in size (106-150 μm), the combustion of volatiles and char appeared to
252 take place simultaneously at the initial stage of combustion, and fragmentation was not visualized.
253 This is supported by the fact that the particle area decreased gradually during the initial stage of
254 combustion process (0–24 ms), which is believed to be the result of the simultaneous combustion
255 of volatiles and char. The single-phase char combustion appeared to begin around 24 ms [refer to
256 Fig. 3(b)].

257

258 Fig. 4(b) suggests that the aspect ratio of Particle A ranges between 1.0 and 1.6 but the averaged
259 value tends to be greater in its residence time, suggesting that the shape of the particle changed
260 from ‘round’ to ‘longitudinal’ during combustion. A periodic variation is also clearly seen with a
261 period of around 25 ms (163 frames), which is similar to the period of the area variation [Fig.
262 4(a)], which is again believed to be due to the particle rotation in the line-of-sight direction. On
263 the other hand, the aspect ratio of Particle B varies from 1.0 to 1.8, suggesting that Particle B is
264 slightly ‘longer’ than Particle A. A decreasing trend is also found, indicating that the shape of
265 particle changed from ‘longitudinal’ to ‘round’ during its residence time.



(a) Area.

(b) Aspect ratio.

Fig. 4. Variation of the area and aspect ratio of the coal particles.

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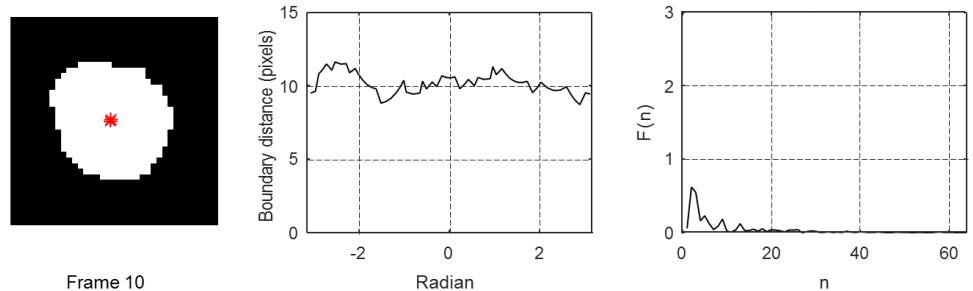
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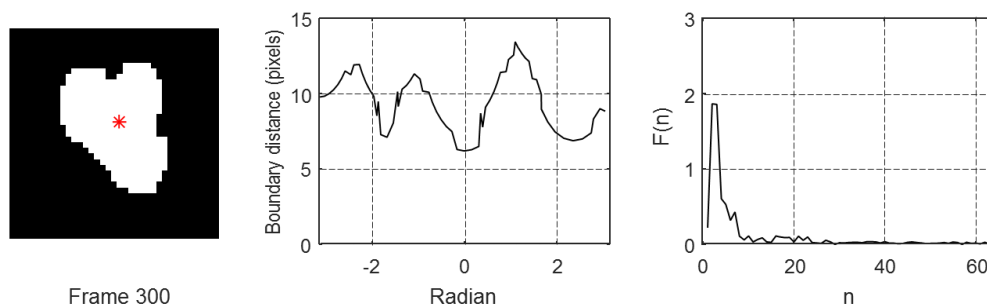
With regard to the surface roughness of the particles, Fig. 5 shows two typical examples of the binary images of Particle A, i.e., Frame 10 (at 1.5 ms) and Frame 300 (at 48.4 ms), and the corresponding boundary distance $r(k)$, and the DFT of $r(k)$. As can be seen, the profile of the boundary distances differs significantly from one frame to another. Compared to the frequency of Frame 300, there are fewer low-frequency components of Frame 10 due to the fact that the boundary of Frame 10 is smoother than that of Frame 300 [Fig. 5(a)]. As the difference in surface roughness is mainly shown in the low frequency band, only the first four components, DF_1 - DF_4 , are further analyzed.

Fig. 6 presents DF_1 - DF_4 of the boundary variance index for Particle A. It reveals that DF_1 , which represents the lowest frequency variance among the four components, is lower than the other three components. DF_2 shows a periodical trend which is considered to be related to the rotation of the particle. It was observed in the video that there were some fragments broken up from the main particle during the later stage of devolatilization/volatile combustion and the initial stage of char combustion, i.e., between 20 ms and 60 ms. The results illuminate that the fragmentation and char combustion of the coal particle affect the boundary variance in different scales, especially at higher frequency components, i.e., DF_3 and DF_4 .

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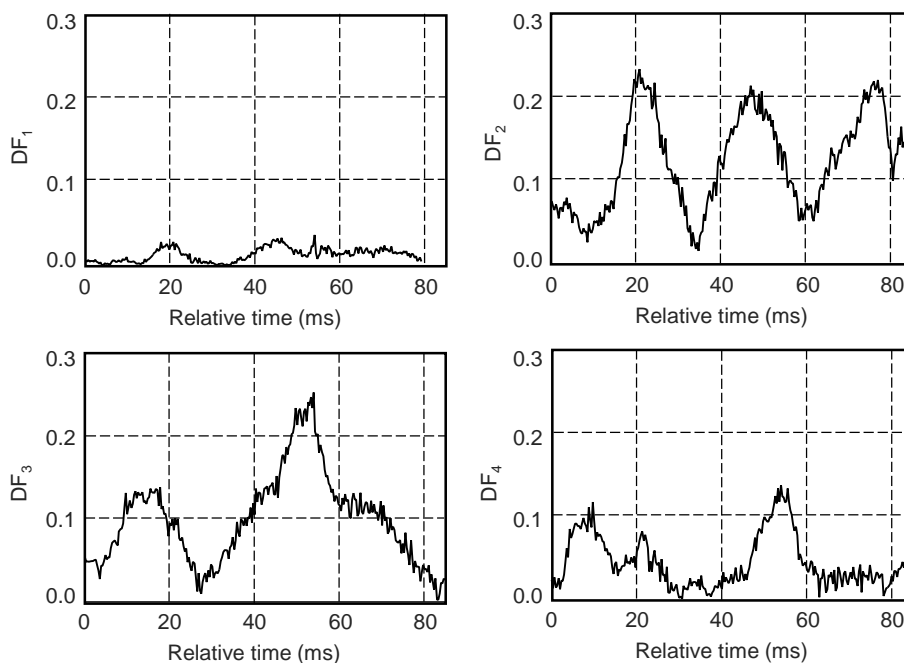
(a) Binary image. (b) Boundary distance. (c) DFT of the boundary distance.

290

Fig. 5. Binary image, boundary distance and DFT of Particle A for Frames 10 (at 1.5 ms) and 300

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(at 48.4 ms).



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293

Fig. 6. Boundary variance index of boundary distance of Particle A.

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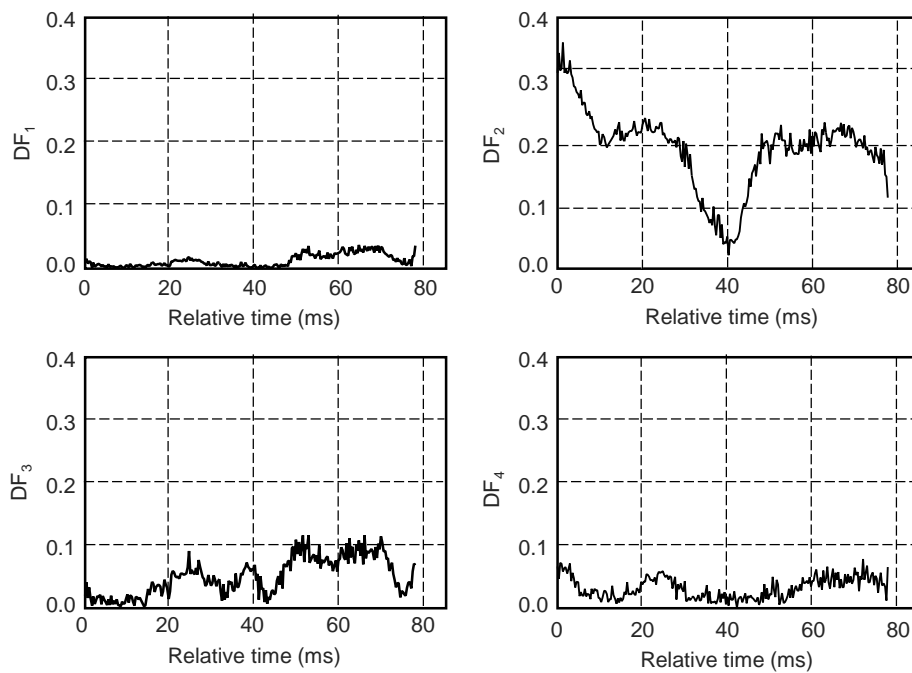
Fig. 7 illustrates DF_1 - DF_4 of the boundary variance index for Particle B. Similar to Particle A, DF_1

295

is lower than the other three. DF_2 has the lowest value at around 40 ms, indicating a smoother

296 surface of Particle B at that period of time. In addition, DF_1-DF_3 vary irregularly but have much
 297 lower amplitudes in comparison to that of Particle A, suggesting that Particle B has a smoother
 298 surface than Particle A. This may be attributed to the fact that Particle B has no obvious
 299 fragmentation during combustion as a result of its smaller size in comparison to Particle A. The
 300 results have also suggested that the particle fragmentation and char combustion are a main
 301 contributor to the surface roughness of the particles.

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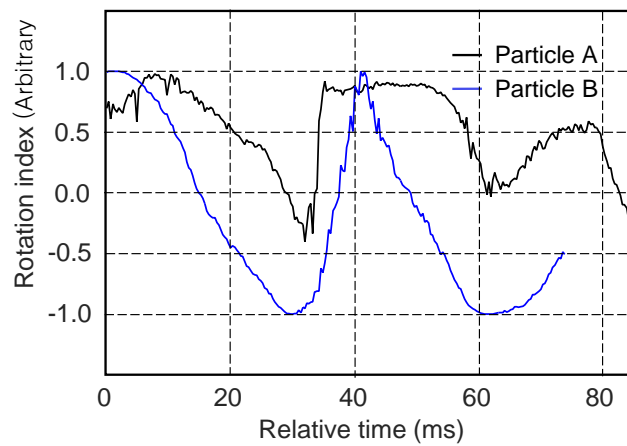
304 Fig. 7. Boundary variance index of boundary distance of Particle B.

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306 *B. Rotational characteristics*

307 The rotation variance of the particle is owing to the momentum changes caused by the
 308 heterogeneous combustion. Fig. 8 shows that the rotation index of Particle A has a similar
 309 periodic variation as observed in Fig. 4. Again, the periodic variation is believed to be attributed
 310 to the rotation of the particle in the line-of-sight direction of the camera system. It is also noted
 311 that the rotation index of Particle A varies in a range between -0.25 and 1 (i.e., 90° and 200°),
 312 which does not mean that the particle does not rotate but may be attributed to the case that the

313 rotation direction of the particle is close to the line-of-sight. It can be found in Fig. 4 that the
314 period of the area variation of Particle A is around 50 ms (computed between the two peaks),
315 suggesting a rotational frequency of 20 Hz. In contrast, the period of the area variation of Particle
316 B is 33 ms, which means the rotational frequency of Particle B is around 30 Hz. The higher
317 rotational frequency of Particle B may be attributed to the smaller size (hence a greater influence
318 of the gaseous flow in the DTF), greater combustion rate and no fragmentation (which would
319 reduce the motion of the particle) in comparison to Particle A.

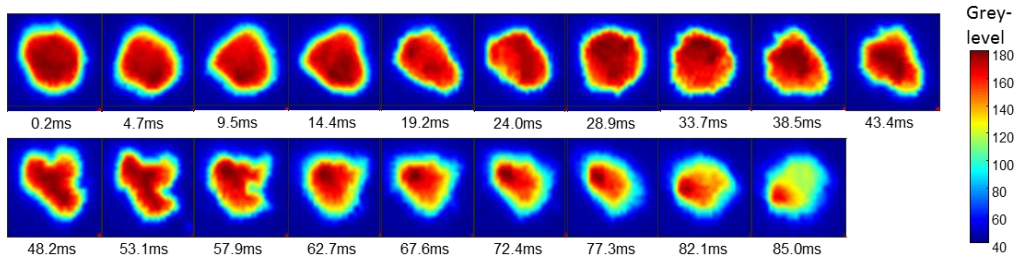


320
321 Fig. 8. Rotation index of the coal particles.

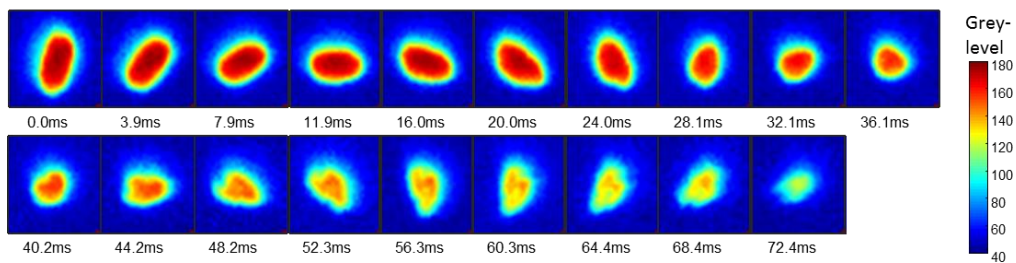
322
323 *C. Luminous characteristics*

324 As mentioned earlier, the luminous intensity of the burning particles in the images is closely
325 related to the surface temperature of the particles. It is believed that, in general, the higher the
326 luminous intensity, the higher the surface temperature and thus more intensive combustion
327 reactions. Fig. 9 exhibits the pseudo color images of the luminous intensity of the burning
328 particles. It is found that the luminosity of both particles is relatively homogeneous during the
329 early stage of the combustion, which is because of the volatile combustion in that period of time.
330 When the volatile combustion is about to finish, however, the luminosity becomes heterogeneous
331 due to the inhomogeneous char combustion as a result of ash layer formed in the remaining char
332 particle. The variations of the luminous intensity of the particles can be more clearly seen in Fig.

333 10. The normalized luminous intensity of Particle A shows a periodical trend from 0 ms to about
 334 40 ms, and then a decreasing trend, indicating that its luminous intensity decreases towards the
 335 later stage (at around 20ms) of the devolatilization/volatile combustion and increase with the
 336 initial stage of char combustion (the significant char combustion of the core particle started
 337 around 40 ms). A decreasing rate of 0.58%/ms is found from 42 ms to 83 ms, suggesting the
 338 significant consumption of carbon in the remaining char particle. In contrast, a monotonous
 339 decreasing trend is observed from the normalized luminous intensity of Particle B (Fig. 10). This
 340 indicates that the combustion of volatiles and char took place at the same time from the beginning
 341 (when the particle's burning can be picked up by the camera) and hence a heterogeneous
 342 combustion all the way. It is also noted that the luminous intensity decreased dramatically after
 343 75 ms, indicating the completion of the combustion.

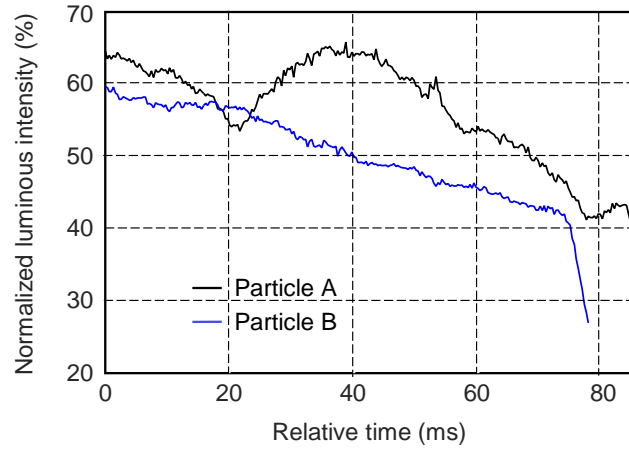


(a) Particle A.



(b) Particle B.

Fig. 9. Pseudo color images of the luminous intensity of the particles.



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350

351 Fig. 10. Normalized luminous intensity of the coal particles.

352

353 It should be mentioned that the experimental results presented above have suffered from
 354 uncertainties in some extent. The uncertainty of the measurement can be attributed to the image
 355 resolution, especially considering the tiny size of coal particles. The boundary of the particle in
 356 the images can be irregular and sometimes blur, this would result in a low signal-to-noise ratio,
 357 and thus an uncertainty in the calculation of the physical parameters. In the presented study, the
 358 particle sizes range from 106 μm to 212 μm , which gave us reasonable image sizes, and thus the
 359 uncertainty caused would not introduce a significant error in the calculation. In addition, the
 360 particles are of 3-D arbitrary shape, but the computed parameters are based on their 2-D images.
 361 This also introduces an uncertainty, which is unavoidable and difficult to assess. From a statistic
 362 analysis point of view, however, such an uncertainty would not make a significant impact on the
 363 results.

364

365 IV. CONCLUSIONS

366

367 In this study, the combustion behaviors of two sets of coal particles with different sizes have been
 368 investigated using high-speed imaging and image processing techniques. Characteristic
 369 parameters including area, aspect ratio, boundary distance, boundary variance index, rotation

370 index and normalized luminous intensity have been defined and computed to quantify the
371 combustion behaviors of the particles. It has been found that the coal with different particle sizes
372 and shapes exhibits distinctly different combustion behaviors. For the large coal particle, the
373 combustion of volatiles and char takes place sequentially, whilst, for the small particle, the
374 combustion of volatiles and char occurs at the same time. The results have also shown that the
375 size of the particles has a decreasing trend due to the combustion of volatiles and char with
376 periodic variations which is attributed to the rotation of the particles. The fragmentation and char
377 combustion have caused significant changes in the surface roughness of the particles. In addition,
378 the luminosity of the large particle shows two peaks when the combustion of volatiles and char
379 happen sequentially, whilst the luminosity of the small particle decreases monotonously when the
380 combustion of volatile and char occurs simultaneously. It can be concluded that the combination
381 of high-speed imaging and image processing has provided a feasible and effective means for
382 characterizing the combustion behaviors of burning coal particles. Further applications of the
383 developed techniques will be extended to the study of combustion behaviors of pulverized
384 biomass and biomass/coal blends under various combustion conditions.

385

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