Restructuring Software: A Case Study

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SUMMARY

We use knot count and path count metrics to identify which routines in the Level 1 BLAS might benefit from code restructuring. We then consider how both logical restructuring and the improvements in the facilities available from successive versions of Fortran have allowed us to improve both the complexity of the code as measured by knot count, path count and cyclomatic complexity, and the user interface of one of the identified routines which compute the Euclidean norm of a vector. With these reductions in complexity we hope that we have contributed to improvements in the maintainability and clarity of the code. Software complexity metrics and the control graph are used to quantify and provide a visual guide to the quality of the software, and the performance of a Fortran code restructuring tool is reported. Finally we give some indication of the cost of the extra numerical robustness offered by the BLAS routine over the use of new Fortran 90 intrinsic functions.

KEY WORDS Software complexity metrics Fortran Euclidean norm Software tools

INTRODUCTION

Three of the most important qualities of software, as far as the end user is concerned, are robustness, reliability and efficiency. Those interested in fixing bugs and upgrading software are also keen that the code be easy to understand, test, and maintain. Details of these, and other important software factors may be found in Fenton and Watts.

The ability to produce clear, readable code depends both on the implementation language and the programmer. The programming language needs to have the control and data structures available to allow the coder to generate a clean and simple, yet efficient, implementation of the algorithm. In general, the fewer facilities a language provides the more difficult it is for a programmer to generate such code.

Fortran has evolved from the very simple ‘high level’ language of the 1950’s, through Fortran 66, the first programming language to be standardised, and Fortran 77, a relatively minor modernisation, to the much larger and more complex Fortran 90.

The Level 1 Basic Linear Algebra Subroutines (BLAS), originally published in Fortran 66, implemented a number of common vector operations and were designed to be used as building blocks for linear algebra software. Routines were provided to deal with the different numerical data types available in Standard Fortran 66 (default precision for real and complex and double precision real). The routines were designed to be both numerically robust and efficient (many used loop unrolling to obtain better performance), although for maximal efficiency it was expected that specially tuned versions would be made available for particular hardware platforms.

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First we describe briefly three software metrics and look at how they were used to help identify which of the Level 1 BLAS were likely to be difficult to understand, test and maintain. We then consider how restructuring the code affected the metrics to ascertain whether the chosen measures offer any help in quantifying the improvements made to the code. We also report on how well two Fortran code restructurers fared on the original and rewritten Fortran 66 routines. A Fortran 77 version of one of the routines is presented. We then consider how the new facilities offered by Fortran 90 may be used to improve both the code and the user interface. Finally we look at the impact which the universal use of IEEE floating-point arithmetic may have on the underlying method and the cost of numerical robustness.

SOFTWARE COMPLEXITY MEASURES

In attempting to assist in the production of high quality software, various methods have been proposed to limit the complexity of individual code modules and many methods of measuring code complexity have been advocated (see Zuse for an extensive bibliography). In order to help in quantifying the effects of any changes we make to the software, we will consider the use of three of these metrics

1. knot count which provides some indication of coding clarity,
2. path count (a variant on the metric proposed by Nejmeh) which gives an estimate of the effort required for testing,
3. cyclomatic complexity which also attempts to estimate the testing effort required.

In addition we will look at a pictorial representation of the code in the form of a control graph. The program control graph is a directed graph consisting of basic blocks of code (nodes) connected by directed arcs (edges) corresponding to the flow of control between these nodes. A basic block of code is a sequence of executable statements containing no decisions or transfers of control. Cyclomatic complexity is related to the control graph and is defined to be the cyclomatic number

\[ V(G) = \text{edges} - \text{nodes} + 2 \]

This may be shown to be equivalent to the number of predicates used in the code plus one. It is generally accepted that compound predicates contribute more to program complexity than simple predicates and Myers suggests the use of a complexity interval whose lower bound is \( V(G) \) and whose upper bound is one more than the total number of conditions.

Work by Shepperd and Shepperd & Ince has highlighted a number of theoretical problems with the use of cyclomatic complexity as a software metric; we consider these further in the Conclusion.

The knot count of Woodward et al gives a good indication of program clarity. It is dependent both on the implementation language and the order of statements in the code. A knot is said to occur in a piece of code whenever the paths associated with two transfers of control intersect (see Figure 1 for two examples). The greater the number of knots in a program unit the less intelligible the code is likely to be.

The static path counts given below are similar to Nejmeh’s NPATH statistic and provide an upper bound for the number of possible static paths through the code. Note that some paths so defined may not be executable. The path count complexity of a function is defined as the product of the path complexities of the individual constructions. Thus, for example, the path complexity of a simple if-then-else statement is 2 while three consecutive if-then-else statements would have an associated value of \( 2^3 = 8 \). Three nested if statements would have
a path count of 4. This metric provides a useful measure of the effort required to test the code stringently as well as giving an indication of code maintainability. A reduction in the path count caused by restructuring code would imply the elimination of paths through the code which were originally either impossible to execute or irrelevant to the computation. This would be likely to reduce the time spent in the testing phase of the software development.

All the values of the software metrics stated in this paper have been generated using QAFortran\textsuperscript{15}.

THE LEVEL 1 BLAS

The original BLAS publication\textsuperscript{6} did not define double precision complex routines. In addition a number of subprograms, for example, multiple precision versions and several mixed precision routines, no longer appear on the BLAS reference card\textsuperscript{16} which is now widely considered to be the official definition of the BLAS.

Table I gives the number of lines of executable code in each of the 46 routines listed on the card along with the values of the three metrics defined above. Where routines exist for more than one data type the values given are for the subprogram generating the largest values.

The *NRM2 and *ROTMG families of routines stand out as having very high knot and path counts. Given the low numbers of executable statements, these values indicate that the routines are likely to be difficult to understand, due to the high knot count, and difficult to test thoroughly, due to the large number of possible paths through the code.

To study the effects of code restructuring on these metrics we have chosen a routine from the shorter of the two families, SNRM2. In fact the metric values for SNRM2 are somewhat less than the values given in Table I for the routine which acts on complex input data. The restructuring detailed below is equally applicable to the complex data routine but is easier to follow, as is the description of the underlying algorithm, when applied to the real data case.
Table I. Metric Values for BLAS 1 Routines

<table>
<thead>
<tr>
<th>Routine</th>
<th>LOC</th>
<th>McCabe</th>
<th>Knots</th>
<th>Paths</th>
</tr>
</thead>
<tbody>
<tr>
<td>*ROTG</td>
<td>22</td>
<td>5:6</td>
<td>2</td>
<td>16</td>
</tr>
<tr>
<td>*ROTMG</td>
<td>121</td>
<td>18:18</td>
<td>92</td>
<td>98304</td>
</tr>
<tr>
<td>*ROT</td>
<td>22</td>
<td>7:8</td>
<td>1</td>
<td>8</td>
</tr>
<tr>
<td>*ROTM</td>
<td>84</td>
<td>13:15</td>
<td>17</td>
<td>144</td>
</tr>
<tr>
<td>*SWAP</td>
<td>37</td>
<td>10:11</td>
<td>2</td>
<td>16</td>
</tr>
<tr>
<td>*SCAL</td>
<td>22</td>
<td>8:9</td>
<td>2</td>
<td>8</td>
</tr>
<tr>
<td>*CPY</td>
<td>31</td>
<td>10:11</td>
<td>2</td>
<td>16</td>
</tr>
<tr>
<td>*AXPY</td>
<td>29</td>
<td>11:12</td>
<td>2</td>
<td>16</td>
</tr>
<tr>
<td>*DOT</td>
<td>29</td>
<td>10:11</td>
<td>4</td>
<td>32</td>
</tr>
<tr>
<td>*DOTU</td>
<td>22</td>
<td>7:8</td>
<td>1</td>
<td>8</td>
</tr>
<tr>
<td>*DOTC</td>
<td>22</td>
<td>7:8</td>
<td>1</td>
<td>8</td>
</tr>
<tr>
<td>*xDOT</td>
<td>23</td>
<td>7:8</td>
<td>3</td>
<td>16</td>
</tr>
<tr>
<td>*NRM2</td>
<td>48</td>
<td>18:19</td>
<td>64</td>
<td>10240</td>
</tr>
<tr>
<td>*ASUM</td>
<td>22</td>
<td>8:9</td>
<td>4</td>
<td>8</td>
</tr>
<tr>
<td>I*AMAX</td>
<td>22</td>
<td>8:9</td>
<td>3</td>
<td>8</td>
</tr>
</tbody>
</table>

THE EUCLIDEAN NORM ROUTINES

Given an \( n \)-vector, \( \{x_i\}_{i=1}^n \), the Euclidean norm is defined as

\[
\|x\|_2 = \left( \sum_{i=1}^{n} x_i^2 \right)^{\frac{1}{2}}
\]  

There are four BLAS routines available for this calculation; one for each of the numerical data types mentioned above. The underlying algorithm is relatively simple and may be considered as a compromise between the efficiency of a naive implementation of (1) as a simple square-and-add loop, and the provable numerical robustness of Blue’s algorithm\(^{17}\). The BLAS routines form partial sums of squares as

\[
\frac{1}{x_{\text{max}}^2} \sum_{i=1}^{r} x_i^2
\]

where

\[
x_{\text{max}} = \begin{cases} 
1 & \text{if } \text{cutlo} < z < \text{cuthi} \\
1 & \text{if } z > \text{cuthi} \text{ or } z < \text{cutlo} \\
z & \text{if } z > \text{cuthi} \text{ or } z < \text{cutlo}
\end{cases}
\]

and

\[
z = \max_{i=1..r} |x_i|
\]

Thus as each element is added into the partial sum there may be, at worst, a change of scale. The values of \( \text{cutlo} \) and \( \text{cuthi} \) are dependent on the machine arithmetic and are set in the published code to values which are hopefully applicable to all machines in order to assist with portability (see also below in the section on THE FUTURE OF THE *NRM2 ROUTINES). The original, published code for the single precision version, \( \text{s}nrm2 \), with the introductory comments stripped out and with some minor corrections, is presented in Figure 2. (This is the code currently available from \( \text{netlib}^{18} \).)
REAL FUNCTION SNRM2 ( N, SX, INCX)
INTEGER I, INCX, IX, J, N, NEXT
REAL SX(1), CUTLO, CUTHI, HITEST, SUM, XMAX, ZERO, ONE
DATA ZERO, ONE /0.0E0, 1.0E0/
DATA CUTLO, CUTHI / 4.441E-16, 1.304E19 /
1 IF(N .GT. 0 .AND. INCX.GT.0) GO TO 10
2 SNRM2 = ZERO
3 GO TO 300
4 10 ASSIGN 30 TO NEXT
5 SUM = ZERO
6 I = 1
7 IX = 1
8 20 GO TO NEXT,(30, 50, 70, 110)
9 30 IF( ABS(SX(I)) .GT. CUTLO) GO TO 85
10 ASSIGN 50 TO NEXT
11 XMAX = ZERO
12 50 IF( SX(I) .EQ. ZERO) GO TO 200
13 IF( ABS(SX(I)) .GT. CUTLO) GO TO 85
14 ASSIGN 70 TO NEXT
15 GO TO 105
16 100 CONTINUE
17 IX = J
18 ASSIGN 110 TO NEXT
19 SUM = (SUM / SX(I)) / SX(I)
20 105 XMAX = ABS(SX(I))
21 GO TO 115
22 70 IF( ABS(SX(I)) .GT. CUTLO ) GO TO 75
23 COMMON CODE FOR PHASES 2 AND 4.
24 IN PHASE 4 SUM IS LARGE. SCALE TO AVOID OVERFLOW.
25 110 IF( ABS(SX(I)) .LE. XMAX ) GO TO 115
26 SUM = SUM + SX(I)**2
27 115 SUM = SUM + (SX(I)/XMAX)**2
28 GO TO 200
29 75 SUM = (SUM * XMAX) * XMAX
30 FOR REAL OR D.P. SET HITEST = CUTHI
31 FOR COMPLEX SET HITEST = CUTHI
32 85 HITEST = CUTHI/FLOAT( N )
33 PHASE 3. SUM IS MID-RANGE. NO SCALING.
34 DO 95 J = IX, N
35 IF(ABS(SX(I)) .GE. HITEST) GO TO 100
36 SUM = SUM + SX(I)**2
37 I = I + INCX
38 95 CONTINUE
39 SNRM2 = SQRT( SUM )
40 GO TO 300
41 200 CONTINUE
42 IX = IX + 1
43 I = I + INCX
44 IF( IX .LE. N ) GO TO 20
45 END OF MAIN LOOP.
46 COMPUTE SQUARE ROOT AND ADJUST FOR SCALING.
47 SNRM2 = XMAX * SQRT(SUM)
48 300 CONTINUE
49 RETURN
50 END

Figure 2. Original Fortran 66 Code for snrm2
However harmful it may be considered\textsuperscript{19}, the use of explicit GOTO statements and labels was unavoidable in Fortran 66 due to the extremely limited control structures that were provided. For example, there was no IF-ELSE IF-ELSE block available; thus even a simple IF-THEN-ELSE construction required two labels and two GOTO statements, and generated a knot. In restructuring the code we looked primarily at reducing the knot count; we also report the number of explicit GOTO statements and target labels (i.e., those labels that appear explicitly in a GOTO statement) in the code as these contribute both to the knot count and to the ease of understanding of the code. It was hoped that the path count and cyclomatic complexity values would provide an indication of the effect of any restructuring had on the test effort required. Any reduction in these metrics could be viewed as a reduction in the work required to ensure a comprehensive path coverage was achieved.

Figure 3 shows the control graph of the source given in Figure 2 and reflects the complexity of the code. Each circle in the control graph represents a basic block. The numbers in parentheses denote the lines of code, given in the equivalent source code listing, which make up each basic block; the other number is the block number and is included for ease of reference. The most telling of the metric values is the knot count which, at 41, is extremely high for a routine containing just 44 executable statements. The cyclomatic complexity interval is (13:14) and the path count is 1024, again very high for such a short routine and far in excess of the 200 maximum for a routine quoted in Nejmeh\textsuperscript{10} for a similar metric. In addition the code contains 15 explicit gotos and 13 target labels.

Spag\textsuperscript{20}, a software tool designed to improve the structure of Fortran 66 by rearranging (and if necessary duplicating) statements and using Fortran 77 constructions, produced some improvements. The knot count was almost halved to 23, the cyclomatic complexity interval was reduced to (10:11) and the path count was reduced to 256. Nag\textunderscore struct, one of NAG’s suite of Fortran 77 software tools\textsuperscript{21}, only managed a reduction of one in the knot count although the path count was reduced by a factor of almost three.

Restructuring the original code by hand was more successful. This new Fortran 66 version had a knot count of just 17 and a path count of 256. The cyclomatic complexity interval was (11:16), showing that, although the number of predicates was reduced, the logical complexity of some of them had increased. It is interesting to note here that spag, even using Fortran 77 as its target language, did not manage to reduce the number of knots to this level.

The hand coded Fortran 77 version given in Figure 4 has a knot count of 2 whilst the path count has been reduced to 65. The cyclomatic complexity interval remains the same as for the input Fortran 66 code. There is now a single explicit GOTO and just three labels, two of which are used as do-loop terminators. The other label, both knots and the explicit GOTO are required to test for a zero input vector and the possible return of a zero value.

Figure 5 shows the control graph for the hand coded Fortran 66 version of the routine and clearly shows the improvement in structure over the original. The implicit use of IF-THEN-ELSE constructs is now obvious and it is the translation of these into explicit Fortran 77 constructs which accounts for a large proportion of the reduction in knots. Both commercial restructurers fared much better on this code, generating versions with almost as few knots (4 in each case) and paths (spag, 96 and nag\textunderscore struct, 65) as the hand crafted Fortran 77.
Although the new features of Fortran 90 do not provide more than a cosmetic improvement to the final Fortran 77 code (for example, use of the new relational operators) the ENDDO and EXIT statements do allow the removal of the remaining three labels albeit with a little contortion in the case of the break out from the loop testing for the zero vector.

However the new language does offer scope for improving the user interface. Most users
REAL FUNCTION SNRM2(N, SX, INCX)
REAL CUTLO, CUTHI, ZERO, ONE, HITEST, SUM, XMAX, SX(*)
PARAMETER (CUTLO=8.232E-11, CUTHI=1.304E19, ZERO=0.0E0,
* ONE=1.0E0)
INTEGER INCX, N, I, NN
LOGICAL TINY, HUGE
*
1 IF (N.LE.0 .OR. INCX.LT.1) THEN
2 SNRM2=ZERO
3 ELSE
4 NN = N*INCX
5 HITEST = CUTHI/FLOAT(N)
6 DO 10 I=1,NN,INCX
7 IF (SX(I) .NE. ZERO) GO TO 20
8 10 CONTINUE
* ZERO VECTOR
9 SNRM2 = ZERO
10 RETURN
11 20 TINY = ABS(SX(I)) .LE. CUTLO
12 HUGE = ABS(SX(I)) .GE. HITEST
13 XMAX = ABS(SX(I))
14 SUM = ZERO
15 IF (.NOT.TINY .AND. (.NOT.HUGE)) THEN
* MIDRANGE ... NO SCALING
16 SUM = SUM + SX(I)*SX(I)
17 ELSE
* NEED TO SCALE
18 SUM =ONE
19 ENDIF
20 DO 30 I=I+INCX,NN,INCX
* TRANSITION FROM TINY (SCALED) TO MIDRANGE (UNSCALED)
21 IF (TINY .AND. ABS(SX(I)).GT.CUTLO) THEN
22 TINY = .FALSE.
23 SUM = (SUM*XMAX)*XMAX
24 ENDIF
25 IF(.NOT.TINY .AND. (.NOT.HUGE)) THEN
* TRANSITION FROM MID-RANGE TO HUGE
26 IF(ABS(SX(I)).GE.HITEST) THEN
27 HUGE = .TRUE.
28 XMAX = ABS(SX(I))
29 SUM=ONE + (SUM/XMAX)/XMAX
30 ELSE
* NO TRANSITION (I.E. MIDRANGE)
31 SUM=SUM+SX(I)*SX(I)
32 ENDIF
33 ELSE
34 IF(ABS(SX(I)) .LE. XMAX) THEN
* NO NEED TO CHANGE SCALE
35 SUM = SUM + (SX(I)/XMAX)**2
36 ELSE
* NEED TO SCALE UPWARDS
37 SUM = ONE + SUM*(XMAX/SX(I))**2
38 XMAX = ABS(SX(I))
39 ENDIF
40 ENDIF
41 30 CONTINUE
* SCALE RESULT
42 IF(TINY .OR. HUGE) THEN
43 SNRM2 = XMAX*SQRT(SUM)
44 ELSE
45 SNRM2 = SQRT(SUM)
46 ENDIF
47 ENDIF
48 END

Figure 4. Restructured Fortran 77 Code for snrm2
of the *nrm2 routines have no need of the incx parameter, the most common requirement being to compute the norm of an entire vector. Certainly users would be happier with a call to a single routine rather than having to call different routines for different types of vector; after all Fortran 77 compilers allow this for intrinsic functions like sin and cos. Being able to write

\[ x_{\text{norm}} = \text{nrm2}(x, n) \]
where the value returned is given by (1) no matter what the type of \( x \) would be a step in the right direction. In fact Fortran 90 provides the ability to use

\[
x_{\text{norm}} = \text{nrm2}(x)
\]

where, provided the vector \( x \) is defined as an assumed-shape array, the routine can obtain the length of the vector, \( n \), internally. Additionally, the other two arguments may still be provided if required and the original Fortran 77 routines may be used inside a wrapper routine.

```fortran
function snrm2_opt(sx, n, incx) result (sp_norm)
    integer, optional, intent(in) :: n, incx
    real, intent(in) :: sx(:)
    real :: sp_norm

    integer :: local_n, local_incx
    real :: snrm2

    if (present(n)) then
        local_n = n
    else
        local_n = size(sx)
    endif

    if (present(incx)) then
        local_incx = incx
    else
        local_incx = 1
    endif

    sp_norm = snrm2(local_n, sx, local_incx)
end function snrm2_opt
```

Figure 6. Fortran 90 Wrapper Routine for \texttt{snrm2}

The three new facilities provided by Fortran 90 which are helpful here are assumed-shape (allocatable) arrays, optional arguments, and user defined generic functions. The maximum size of an array no longer needs to be determined at compile time; dynamic allocation allows the correct amount of storage to be reserved for the particular problem being solved and the size of such arrays may be ascertained when they are passed as parameters to subprograms. Thus

```fortran
real, dimension(:), allocatable :: vector
read *, size_of_problem
allocate (vector(size_of_problem))
```

defines a real array of length \( \text{size\_of\_problem} \). A wrapper routine, with \( n \) and \( \text{incx} \) as optional arguments can be used to generate default values when these parameters are not explicitly provided by the user. The version of a wrapper routine implementing this for a real vector, \texttt{snrm2\_opt}, is given in Figure 6.

The change in the order of the parameters in \texttt{snrm2\_opt} is important as the non-optional argument (the input vector) must come first. Similar wrappers may be constructed for the other vector types. It should be noted that explicit use of the double precision type statement
TIM HOPKINS

has been superseded in Fortran 90 by the use of a real declaration with an appropriate kind selector.

Finally, a generic function, \( \text{nrm2} \), may be constructed as shown in Figure 7. We note that within \( \text{nrm2} \) the \( \text{incx} \) parameter only needs to be retained for backwards compatibility, since Fortran 90 allows a stride value as part of the triplet used to define an array section. We may thus replace, for example,

\[
x_{\text{norm}} = \text{snrm2}(n, x, \text{incx})
\]

with

\[
n_{\text{nn}} = 1 + (n-1) \ast \text{incx} \\
x_{\text{norm}} = \text{nrm2}(x(1:nn:incx))
\]

The interface module needs to be USE’d in all program units and modules wishing to refer to \( \text{nrm2} \). The improvements in the interface can be obtained without translating the underlying \( *\text{nrm2} \) functions into Fortran 90. Thus Fortran 90 may be viewed as providing added value to existing code.

\[
\text{module generic_nrm2} \\
\text{ interface nrm2} \\
\quad \text{function snrm2\_opt}(sx, n, \text{incx}) \text{ result } (\text{sp\_norm}) \\
\quad \text{integer, optional, intent(in)} :: n, \text{incx} \\
\quad \text{real, intent(in)} :: sx(:, ) \\
\quad \text{real } :: \text{sp\_norm} \\
\quad \text{end function snrm2\_opt} \\
\quad \text{function dnrm2\_opt}(dx, n, \text{incx}) \text{ result } (\text{dp\_norm}) \\
\quad \text{integer, optional, intent(in)} :: n, \text{incx} \\
\quad \text{double precision, intent(in)} :: dx(:, ) \\
\quad \text{double precision } :: \text{dp\_norm} \\
\quad \text{end function dnrm2\_opt} \\
\quad \text{function cnrm2\_opt}(cx, n, \text{incx}) \text{ result } (\text{c\_norm}) \\
\quad \text{integer, intent(in)} :: n, \text{incx} \\
\quad \text{complex, intent(in)} :: cx(:, ) \\
\quad \text{real } :: \text{c\_norm} \\
\quad \text{end function cnrm2\_opt} \\
\quad \text{function znrm2\_opt}(zx, n, \text{incx}) \text{ result } (\text{z\_norm}) \\
\quad \text{integer, optional, intent(in)} :: n, \text{incx} \\
\quad \text{complex*16, intent(in)} :: zx(:, ) \\
\quad \text{double precision } :: \text{z\_norm} \\
\quad \text{end function znrm2\_opt} \\
\end{interface} \\
\text{end module generic_nrm2}
\]

\[\text{Figure 7. Fortran 90 Generic Function for Computing the Euclidean Norm of a Vector}\]

THE FUTURE OF THE *NRM2 ROUTINES

The four BLAS routines, *nrm2, scale partial sums to avoid unnecessary overflows, underflows and possible loss of accuracy. Thus, for example, the 3-vector whose elements are all
would cause an overflow if a simple square-and-add loop were used. This is unreasonable since the final result, \( \sqrt[3]{\text{maxreal}} / 2 \), is representable by the floating-point system.

There are two developments since the original routine was published which are worthy of mention. First the IEEE floating-point standard\(^{22} \) and second the vector and matrix operations available in Fortran 90.

With the increased adoption of the IEEE floating-point standard it may be assumed that the parameters cutlo and cuthi may soon be replaced by their IEEE values rather than using the given universal values. These two parameters are defined as

\[
\begin{align*}
cutlo &= \sqrt{u / \text{eps}} \\ 
cuthi &= \sqrt{v}
\end{align*}
\]

where \( u \) and \( v \) are the smallest and largest positive numbers representable and \( \text{eps} \) is the smallest number such that \( 1 + \text{eps} > 1 \). (It should be noted that these values may be obtained via the new Fortran 90 numerical inquiry functions tiny, huge, and epsilon.) Table II gives the values as published, which are claimed to be applicable over all machines, along with values specifically associated with the IEEE single and double precision definitions. The probability of scaling taking place in a double precision IEEE routine would appear to be extremely small for most practical applications.

Table II. cutlo and cuthi Values

<table>
<thead>
<tr>
<th>Published</th>
<th>IEEE Standard</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single</td>
<td>Double</td>
</tr>
<tr>
<td>cutlo</td>
<td>4.4e-16</td>
</tr>
<tr>
<td>cuthi</td>
<td>1.3e+19</td>
</tr>
</tbody>
</table>

Second, Fortran 90 provides two new intrinsic functions, dot_product and sum which could be used to generate the required norm. These are both generic in the same sense as the nrm2 function defined above. Thus

\[
\begin{align*}
\text{nrm2}(x) & \equiv \sqrt{\text{dot_product}(x,x)} \\ & \equiv \sqrt{\text{sum}(x*x)}
\end{align*}
\]

It should be noted that neither the dot_product nor the sum function offers the numerical robustness of the nrm2 routines in providing accurate results for a very wide range of numerical inputs.

The overheads involved in using snrm2, rather than a simple square-and-add loop in the case of data requiring no scaling, mainly consist of the additional tests at lines 21, 25 and 26 in Figure 4. To gauge the extra cost involved a comparison was made of the execution times of the four methods

1. snrm2,
2. a simple square-and-add code,
3. the Fortran 90 intrinsic function, dot_product,
4. the Fortran 90 intrinsic function, sum.

In each case the vector of length 1000000 was computed 50 times. Three compilers were
used, SUN f77 (version 1.4), NAG f90 (version 2.0a(264)) and EPC f90 (version 1.0.1) all running on a SUN 4/670MP under SunOS 4.3.

Table III shows the timings, in seconds, obtained using the Unix time command. Several runs of each program were made and the times averaged. The optimised timings are for the highest level of optimisation available and the non-optimised timings are for debug mode using the -g flag. (Note that all three compilers offer more stringent checking in the form of array bound, and in some cases, unassigned variable checks.)

Overall the cost of \texttt{snrm2} compared to the square-and-add code is a factor of around two to three. The effectiveness of the \texttt{dot_product} intrinsic function was not consistent, being much faster than square-and-add using the EPC compiler and about the same using the NAG compiler. The \texttt{sum} routine had little to offer. The \texttt{snrm2} code appears to be slightly more susceptible to optimisation than either the square-and-add, or \texttt{dot_product} and \texttt{sum} codes.

In order to ascertain quantitatively where the extra time was being spent in \texttt{snrm2}, \texttt{rtp} \(^{23}\), a real time profiler, was used to obtain timing information at a statement level. This showed that the execution of the statement

\begin{equation}
\text{sum} = \text{sum} + \text{sx}(i) \times \text{sx}(i)
\end{equation}

accounted for approximately 15\% of the total execution time of the \texttt{snrm2} code and 43\% with the simple square-and-add routine. For \texttt{snrm2} approximately 30\% of the time was used in performing the tests at lines 25 and 26 in Figure 4. It should be noted that \texttt{rtp} uses code sampling to obtain its timings; care was thus taken to ensure that the results obtained were as independent as possible of the sampling frequency.

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|c|}
\hline
Compiler & mode & \texttt{snrm2} & square-and-add & \texttt{dot_product} & \texttt{sum} \\
\hline
Sun f77 & non-opt & 114.4 & 64.0 & – & – \\
Sun f77 & opt & 62.7 & 22.4 & – & – \\
Nag f90 & non-opt & 151.1 & 63.3 & 75.0 & 130.2 \\
Nag f90 & opt & 69.2 & 32.9 & 30.2 & 49.1 \\
Epc f90 & non-opt & 264.3 & 128.4 & 29.9 & 67.3 \\
Epc f90 & opt & 80.2 & 44.1 & 13.9 & 42.5 \\
\hline
\end{tabular}
\caption{Execution times in seconds for vector norm computations}
\end{table}

\section*{CONCLUSION}

We have looked at how the use of a combination of software metrics (knot and path counts) along with the number of executable lines of code allowed the identification of old Fortran code that was difficult both to understand and to test comprehensively. This would imply that the code would also be hard to maintain. Table IV provides a summary of the various versions of the routine generated along with the associated metric values.

The hand restructured Fortran 66 version, code 4, in Table IV, appeared to be more structured than the codes produced from the original SNRM2 using the code restructuring tools whose target language is Fortran 77. This was highlighted by the fact that both the knot and path counts were reduced to almost ‘optimal’ values when the same tools were applied to the hand-crafted code. This suggests that code 4, was a logically clearer implementation of the algorithm than the original code. The use of Fortran 90 allowed a significant improvement in the user interface.
Table IV. Summary of code versions and associated metrics

<table>
<thead>
<tr>
<th>Code Version</th>
<th>Language</th>
<th>LOC</th>
<th>Knots</th>
<th>Paths</th>
<th>Cyclomatic</th>
<th>GOTO’s</th>
<th>Labels</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. original</td>
<td>f66</td>
<td>44</td>
<td>41</td>
<td>1024</td>
<td>13:14</td>
<td>15</td>
<td>13</td>
</tr>
<tr>
<td>2. spag on 1.</td>
<td>f77</td>
<td>47</td>
<td>23</td>
<td>256</td>
<td>10:11</td>
<td>12</td>
<td>10</td>
</tr>
<tr>
<td>3. nag struct on 1.</td>
<td>f77</td>
<td>60</td>
<td>40</td>
<td>385</td>
<td>13:14</td>
<td>12</td>
<td>11</td>
</tr>
<tr>
<td>4. hand coded 1.</td>
<td>f66</td>
<td>43</td>
<td>17</td>
<td>256</td>
<td>11:16</td>
<td>15</td>
<td>10</td>
</tr>
<tr>
<td>5. spag on 4.</td>
<td>f77</td>
<td>48</td>
<td>4</td>
<td>96</td>
<td>11:16</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>6. nag struct on 4.</td>
<td>f77</td>
<td>48</td>
<td>4</td>
<td>65</td>
<td>11:16</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>7. hand coded 4.</td>
<td>f77</td>
<td>48</td>
<td>2</td>
<td>65</td>
<td>11:16</td>
<td>1</td>
<td>3</td>
</tr>
<tr>
<td>8. Fortran 90</td>
<td>f90</td>
<td>53</td>
<td>0</td>
<td>65</td>
<td>11:16</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

In addition we would assert that the reduction in the path count can be translated into a significant saving in the effort required to produce adequate test data for the code.

It is interesting to note that the cyclomatic complexity interval of the original unstructured code is contained within the interval for the best reported Fortran 77 version. Given that the metric was being applied to Fortran code, for which it was originally intended, and that the path count has been reduced by a factor of almost 16, the values obtained for the cyclomatic complexity clearly do not reflect the reduction in testing effort obtained by restructuring. This also reinforces the point made by Shepperd & Ince\textsuperscript{14} that cyclomatic complexity is insensitive to the structure of the software.

In the case of ‘dusty deck’ Fortran 66 code, automatic restructurers may be able to reduce both the knot and path counts although the extent to which they are successful is very dependent on the way in which the original code was structured. It is worth noting here that the metrics do not always, in themselves, completely reflect improvements; applying spag to the original code lead to a significant reduction in the metric values although the resultant code was still difficult to understand.

Similar reductions in both knot and path counts have also been obtained for the routine SROTMG (see Hopkins\textsuperscript{24} for details).

An analysis of the knot and path counts for the 96 Level 2 and Level 3 BLAS\textsuperscript{2526} both developed in Fortran 77, reveals no knots and a maximum path count of 6912 for a 140 line routine. These routines generally contain more executable statements than the Level 1 routines. However the path and knot counts indicate that they are likely to be easier to understand and test than several of the shorter BLAS Level 1 routines. This would suggest that using a combination of number of executable statements with path and knot counts may be helpful in identifying code that is likely to be difficult to understand and maintain.

The overheads of numerical robustness of code were considered and quantified for several commercial compilers; certainly savings would be made in safe cases where vector norm calculations form a substantial part of the computational effort. The final generic function illustrates how end-users may benefit from the backwards compatibility and the new facilities offered by Fortran 90 which allow important core routines, written in Fortran 66 and 77, to be successfully repackaged.

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considerably.

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